

Les matemàtiques i la dinàmica de les malalties infeccioses

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May 16, 2020

MACARTHUR ON ECOLOGY

Stephen D. Fretwell

Division of Biology, Kansas State University, Manhattan, Kansas 66506

Every word of God is tested.

Proverbs 30:5

PROLOGUE

Scientists are responsible for truth, knowledge, wisdom, and understanding.

Truth is what is—it is the underlying reality of all existence. Knowledge is what we think we know about truth. Knowledge, however, is always an imperfect assessment, and is always subject to revision and improvement. The realization that there are discrepancies and weaknesses in knowledge is wisdom. Wisdom leads to a process, called the philosophy of science, through which knowledge is modified to better fit the truth. Philosophy means the love of wisdom, and doctors of philosophy are supposed, before all else, to be experts in wisdom. Understanding, as defined in Job (28:28), is the effort to avoid evil. We may think of understanding as what we use in order to adequately apply our wisdom and our knowledge in guiding our actions. While applied scientists seek understanding, basic scientists seek knowledge.

Dr. Robert MacArthur has made a dramatic impact on ecology because, to him, all of this was second nature.

Qué pretende la investigación científica?

“... First, to permit an adequate *description* of the things and events that are the objects of scientific investigation; second, to permit the establishment of general laws or theories by means of which particular events may be *explained* and *predicted*”

C.G. Hempel (1965: 139, emphasis original),
Aspects of Scientific Explanation

The Two Realms of Science

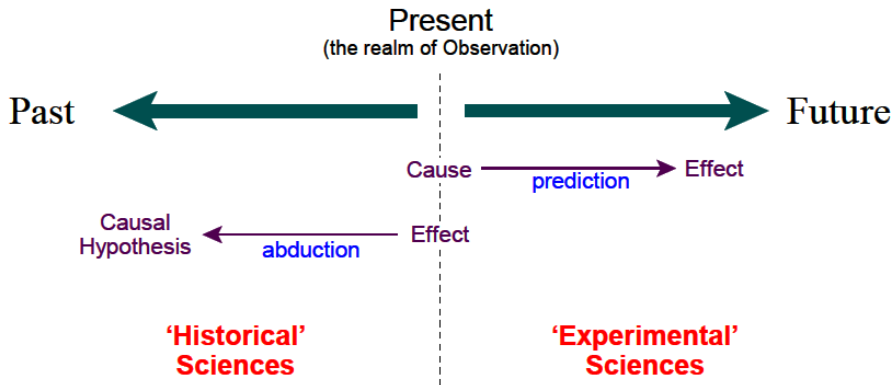
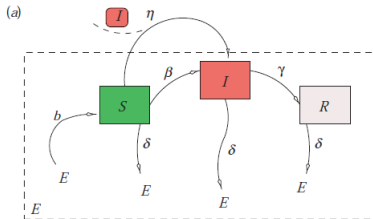


Figura adaptada del curso
"The Philosophy of Biological Systematics"
Kirk Fitzhugh
Natural History Museum, Los Angeles, USA.



$$\begin{aligned}\frac{dS}{dt} &= -\beta \frac{I}{N} S \\ \frac{dI}{dt} &= \beta \frac{I}{N} S - \gamma I \\ \frac{dR}{dt} &= \gamma I\end{aligned}$$

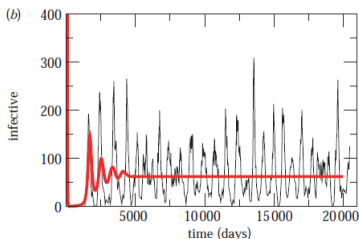
The force of infection: $\lambda = \hat{\beta} b \frac{I}{N}$

A l'inici: $S \approx N$,

$$\frac{dI}{dt} = \hat{\beta} b \frac{I}{N} S - \gamma I$$

$$\frac{dI}{dt} = (\hat{\beta} b - \gamma) I$$

$$R_0 = \frac{\hat{\beta} b}{\gamma}$$



Alonso, McKane & Pascual 2007. Interface

Stochastic amplification in epidemics

$$R_0$$

- Número d'infeccions que cada infectat és capaç de crear mentre està infectat en una població completament susceptible

$$R_0 = (\text{Taxa d'encontre}) (\text{Infectivitat}) (\text{Temps d'infecciositat})$$

- Número d'infeccions que cada infectat és capaç de crear mentre està infectat

$$R_{eff} = (\text{Taxa d'encontre}) \frac{S}{N} (\text{Infectivitat}) (\text{Temps d'infecciositat})$$

- "How do mathematicians model infectious disease outbreaks?" by Robin Thomson
(<https://livestream.com/oxuni/thompson>)
- 3blue1brown on youtube
Youtube: <https://youtu.be/gxAa02rsdIs>
Home page: <https://www.3blue1brown.com>
- "Modeling infectious disease dynamics: The spread of the coronavirus SARS-CoV-2 has predictable features" by Sarah Cobey
<http://science.sciencemag.org/> on May 16, 2020
- Mosquito alert
<http://www.mosquitoalert.com/ca/>

Índice

- 1 Introducción
- 2 Covid19
- 3 Les malalties transmeses per mosquits y el canvi climàtic

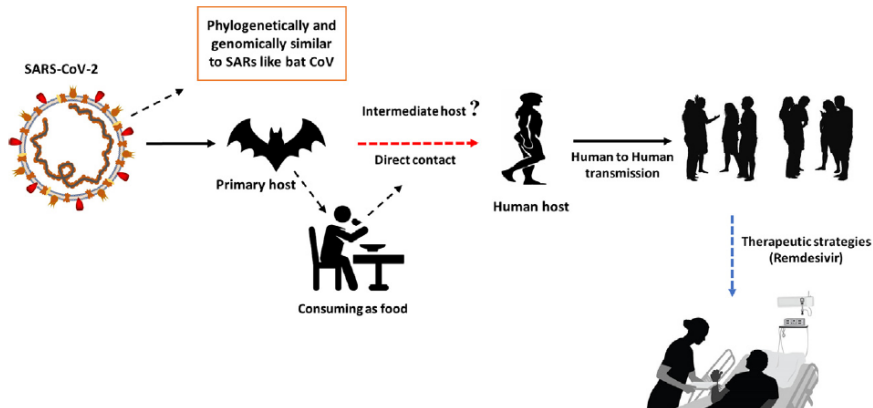


Figura de M.A. Shereen et al. Journal of Advanced Research 24 (2020) 91–98

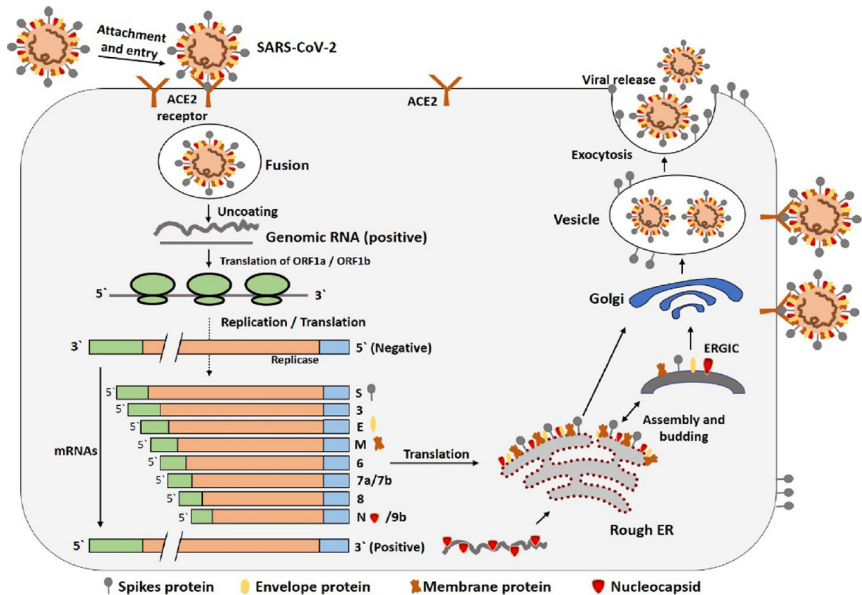
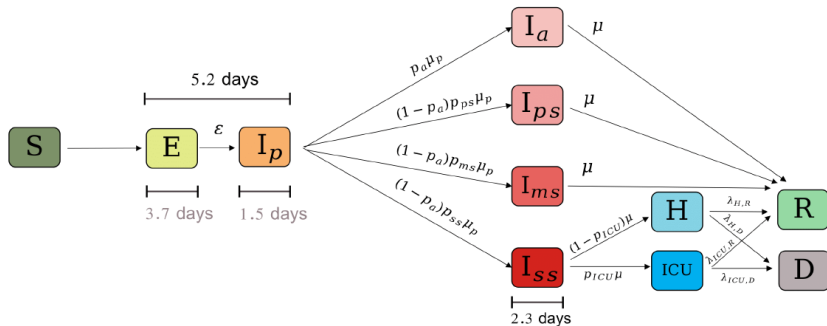


Figura de M.A. Shereen et al. Journal of Advanced Research 24 (2020) 91–98

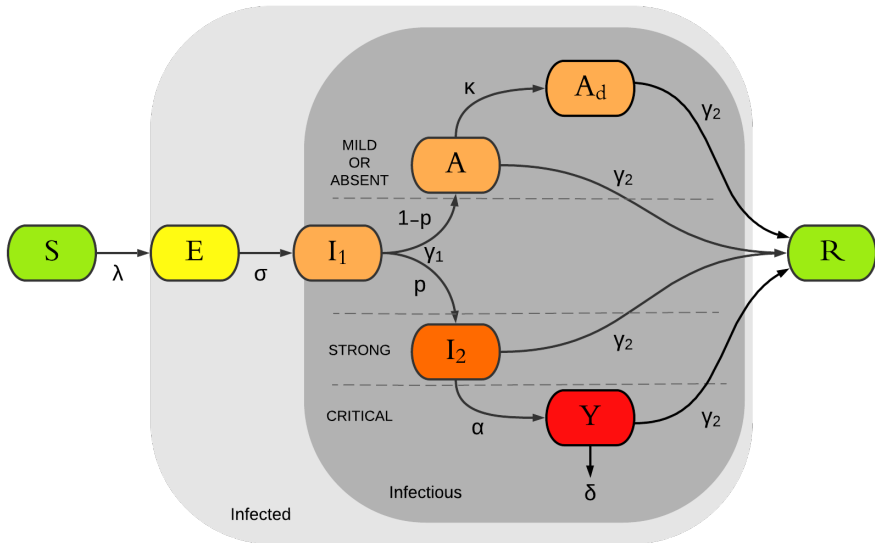
Modelo Francés



Expected impact of lockdown in Île-de-France and possible exit strategies

Laura Di Domenico *et al*

medRxiv preprint doi: <https://doi.org/10.1101/2020.04.13.20063933>



A metapopulation model for covid19 transmission
David Alonso and Frederic Bartumeus
En preparaci3n

Model Parameter	Symbol
Demographic and movement-related parameters	
Population size of the i -th age class at the j -th city	P_{ij}
Movement rate from city k into city j	μ_{jk}
Disease transmission parameters	
Contact rate between age group k and i	β_{ik}
Detectability rate of asymptomatics	κ
Average infectivity	b
Pre-symptomatic infectivity factor	ϕ
Isolation effectiveness of strong cases	ϵ_I
Isolation effectiveness of serious cases	ϵ_Y
Rate of appearance of infectious ability	σ
Rate of appearance of symptoms	γ_1
Age-dependent probability for strong symptoms	p_i
Age-dependent rate of appearance of serious symptoms	α_i
Age-dependent disease-induced mortality	δ_i
Rate of recovery	γ_2

Impacto de las medidas de distanciamiento social sobre la expansión de la epidemia de COVID-19 en España (CSIC)

Objetivos:

- Integración de datos masivos a tiempo real de movilidad humana y encuestas geolocalizadas en modelos de transmisión de covid19.
- La investigación propuesta permitirá comprender mejor los efectos de las medidas de restricción de movilidad y distanciamiento social sobre la dinámica epidemiológica que rige la propagación de la enfermedad.
- El proyecto se respalda en herramientas matemáticas y computacionales, desarrolladas por los distintos miembros del equipo de trabajo, algunas ya en marcha.

PI: José Javier Ramasco (IFISC) & Frederic Bartumeus (CEAB)



GOBIERNO DE ESPAÑA



MINISTERIO DE CIENCIA E INNOVACIÓN



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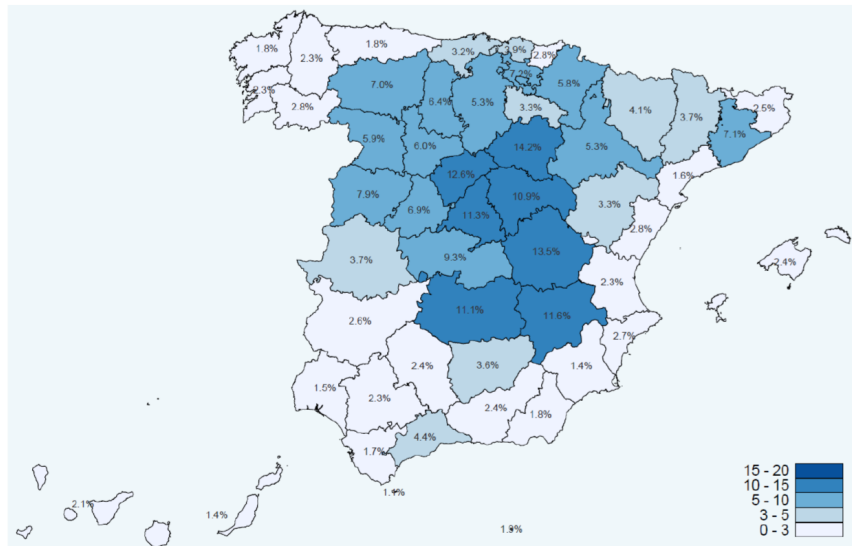


MINISTERIO DE SANIDAD

Consejo Interterritorial
SISTEMA NACIONAL DE SALUD

Instituto de Salud Carlos III

Mapa provincial de Anticuerpos IgG anti SARS-Cov2





Aedes aegypti biting *Homo sapiens*
(source: upload.wikimedia.org)

- 
- Environmental change
 - Socio-economic factors
 - Emergence of infectious diseases

Aedes aegypti biting *Homo sapiens*
(source: upload.wikimedia.org)

Anopheles mosquitoes

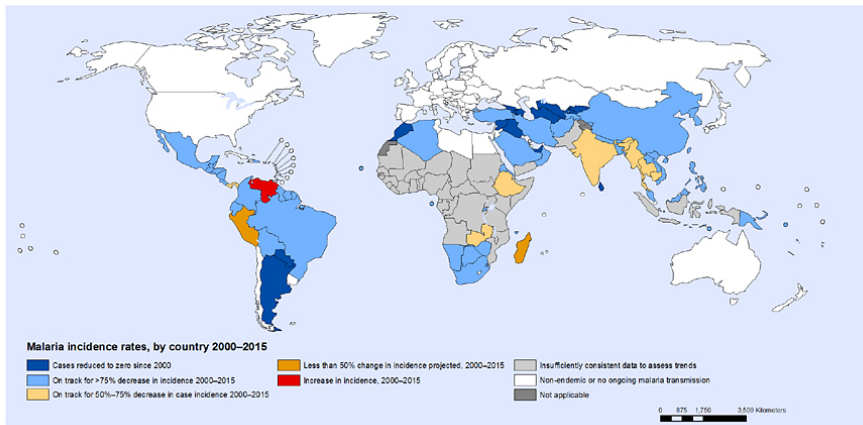


Anopheles albimanus
(source: www.answers.com)



Anopheles gambiae
(source: entomology.ucdavis.edu)

Projected changes in malaria incidence rates, by country, 2000–2015



The boundaries and names shown and the designations used on this map do not imply the expression of any opinion whatsoever on the part of the World Health Organization concerning the legal status of any country, territory, city or area or of its authorities, or concerning the delimitation of its frontiers or boundaries. Dotted and dashed lines on maps represent approximate border lines for which there may not yet be full agreement.

Data Source: World Malaria Report 2015
Map Production: Global Malaria Programme
World Health Organization



World Health
Organization

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Cases

216 million

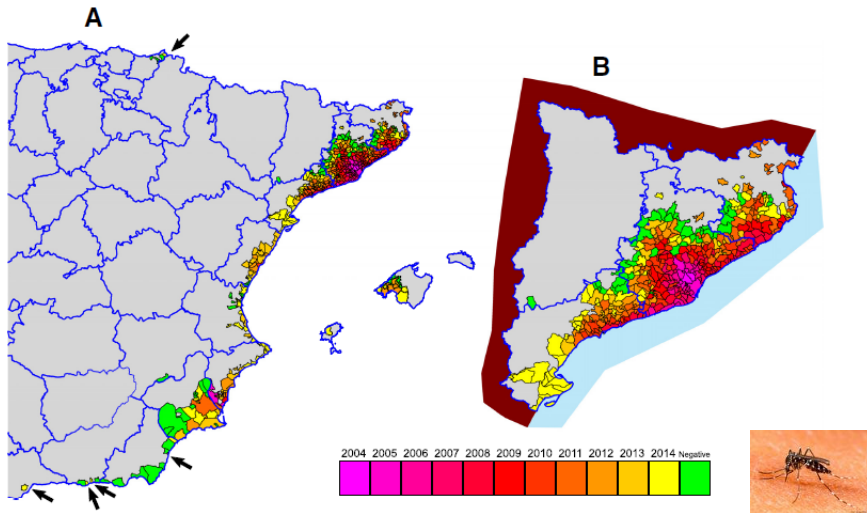
Deaths

445 000

Funding

2.7 billion \$ (2016)

The Invasion of Tiger Mosquito in Spain (2004-2014)

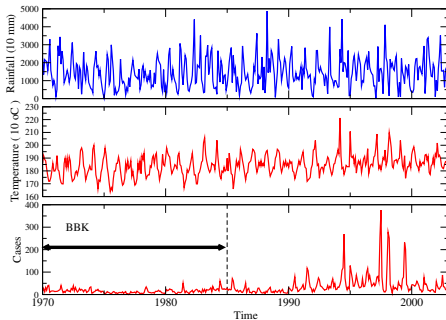


Chikungunya: Prevention and Control

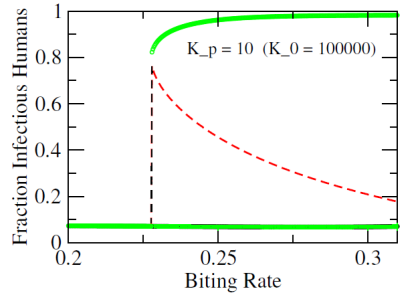
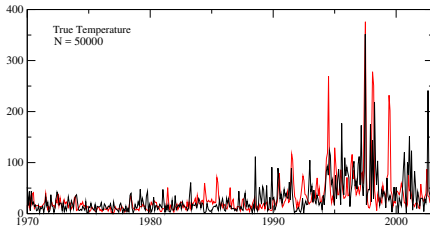
- Imported Chikungunya cases since 2008
- Autochthonous transmission in Italy and France
- Chikungunya Outbreak of Dengue in 2013 in Portugal

Data from simulation

Palmer *etal* (in prep)



PREDICTED (best solution) vs EMPIRICAL MONTHLY CASES
Fitting the whole time series (black) vs empirical data (red)



Alonso, D., Bouma, M. J., & Pascual, M. (2011)

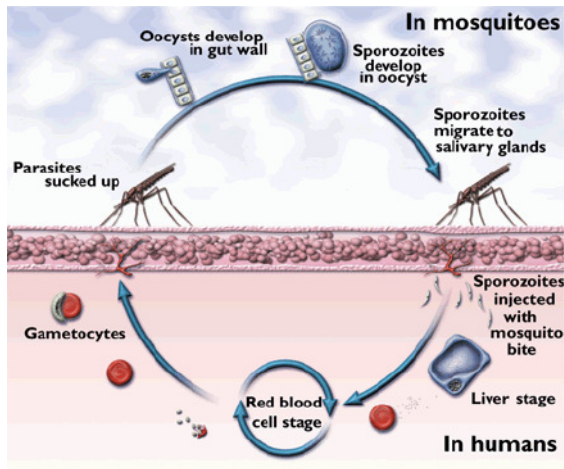
Proceedings. Biological Sciences. The Royal Society

Alonso, D., Dobson, A., & Pascual, M. (2019)

Phil. Trans. R. Soc. B 374

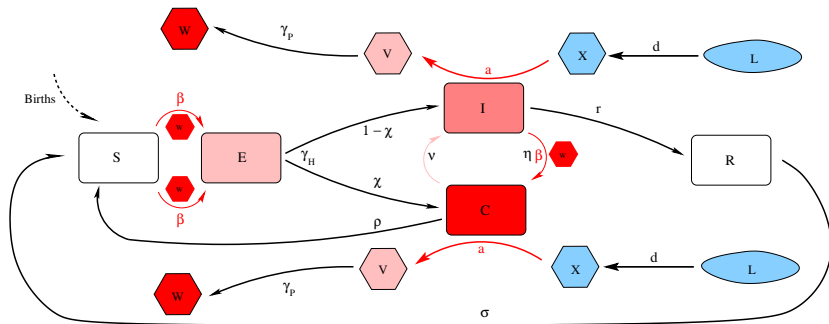


Human - Mosquito - *Plasmodium*



(source: www.cbu.edu)

Human-Mosquito coupled model



Alonso, D., Bouma, M. J., & Pascual, M. (2011)

Proceedings. Biological Sciences. The Royal Society

Human model

β , the force of infection

$$\frac{dS}{dt} = B - \beta S + \sigma R - \delta S + \rho C$$

$$\frac{dE}{dt} = \beta S - \delta E - \gamma E$$

$$\frac{dI}{dt} = (1 - \xi) \gamma E - \eta \beta I + \nu C - r I - \delta I$$

$$\frac{dR}{dt} = -\sigma R + r I - \delta R$$

$$\frac{dC}{dt} = \xi \gamma E + \eta \beta I - \nu C - \rho C - \delta C$$

Human model

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Human model: Population dynamics

Simple demography:

$$\frac{d(S + E + I + R + C)}{dt} = B - \delta (S + E + I + R + C)$$

where $N = S + E + I + R + C$.

Constant population assumption:

$$B = b N$$

where $b = \delta$. Therefore,

$$\frac{dN}{dt} = b N - \delta N = 0$$

Human model: Population dynamics

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Human immunity

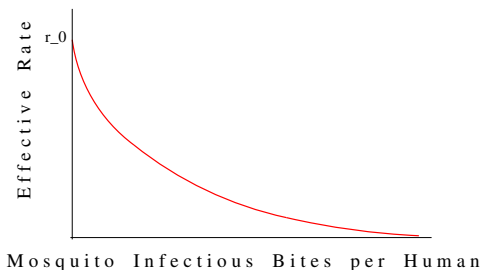
- The rate of loss of immunity, σ , and the recovery rate, r are related to the intensity of disease transmission.
- If the frequency of infectious bites increases both the recovery rate, r , and the loss of immunity rate, σ , tend to decrease.
- The rate at which infectious bites per human arrive is

$$\Lambda = a \frac{W}{N}$$

$$\sigma(\Lambda) = \frac{\Lambda}{\exp(\Lambda/\sigma_0) - 1}$$

$$r(\Lambda) = \frac{\Lambda}{\exp(\Lambda/r_0) - 1}$$

Dietz 1979; Aron and May 1982



Human model: parameters

6	Human turnover	δ
7	Incubation rate	γ
8	Immunity loss rate	σ_0
9	Recovery from I	r_0
10	Recovery from C	ρ
11	Recovery from C to I	ν
12	Probability $I \rightarrow C$	η
13	Probability $S \rightarrow C$	ξ

The force of infection:

$$\beta = b a \frac{W}{N} + \beta_0$$

Human model: parameters

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The force of infection:

$$\beta = b a \frac{W}{N} + \beta_0$$

Mosquito model: Population dynamics

L , larval stage and M adult stage

$$\begin{aligned}\frac{dL}{dt} &= f M \left(\frac{K - L}{K} \right) - \delta_L L - d_L L \\ \frac{dM}{dt} &= d_L L - \delta M\end{aligned}$$

Mosquito carrying capacity is controlled by water availability.

$$\frac{dK}{dt} = K_A p - K_E K$$

Mosquito model: Population dynamics

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Mosquito model: parameters

1	Fecundity	f
2	Carrying capacity	K
3	Larval development	d_L
4	Larval mortality	δ_L
5	Adult mortality	δ_M

Mosquito carrying capacity is controlled by water availability...

$$\frac{dK}{dt} = K_A p - K_E K$$

Mosquito model: Infectious dynamics

$$\begin{aligned}
 \frac{dL}{dt} &= f M \left(\frac{K-L}{K} \right) - \delta_L L - d_L L \\
 \frac{dX}{dt} &= -c a y X - \delta_M X + d_L L \\
 \frac{dV}{dt} &= +c a y X - \gamma_P V - \delta_M V \\
 \frac{dW}{dt} &= \gamma_P V - \delta_M W
 \end{aligned}$$

where y is the fraction of infectious humans:

$$y = \frac{C+I}{H}$$

Mosquito model: Infectious dynamics

$$\begin{aligned}
 \frac{dL}{dt} &= f M \left(\frac{K-L}{K} \right) - \delta_L L - d_L L \\
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Mosquito model: Population dynamics

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where y is the fraction of infectious humans:

$$y = \frac{C + I}{N}$$

14	<i>Plasmodium</i> Incubation rate	γ_P
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Mosquito model: Parameter Response Curves

The model incorporates 5 response curves for 5 different parameters (temperature-driven parameters):

- Development rate of the mosquito larvae, d_L :

$$d_L = 0.00554 T - 0.06737$$

- Development rate of the *Plasmodium* parasite, γ_P
- Death rate of adult mosquitoes, δ_M
- Death rate of mosquitoes larvae, δ_L
- Gonotrophic cycle and mosquito fecundity, a and F

Mosquito model: temperature-driven parameters

- Larva development, d_L
- *Plasmodium* development, γ_P
- Adult and larval survival, δ_M , δ_L
- Biting rate, a

$$f = F a$$

where F is the number of eggs per female.

Effective temperature experimented by adult mosquitoes:

$$T_e = T_o + (1 - x) \Delta T$$

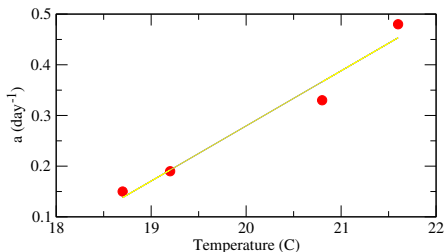
Mosquito model: temperature-driven parameters

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Gonotrophic cycle



Effective temperature experimented by adult mosquitoes:

$$T_e = T_o + (1 - x) \Delta T$$

Afrane, Y. A., B. W. Lawson, A. K. Githeko and G. Yan (2005)

J. Med. Entomology

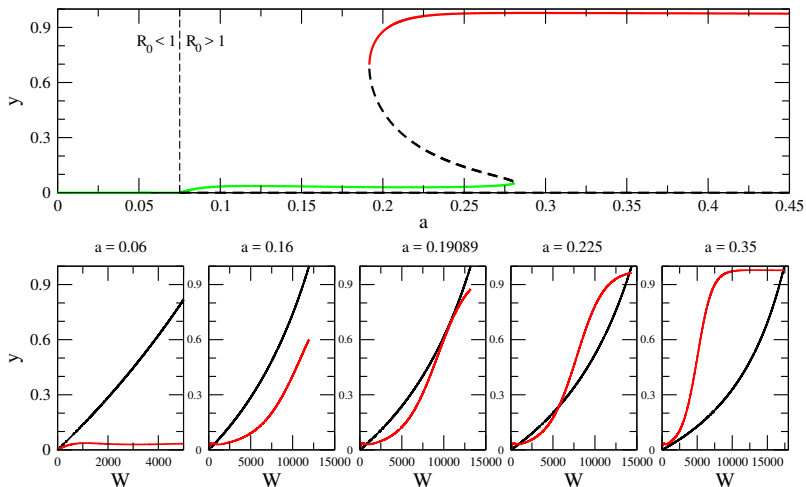
Temperature and Adult Mosquitoes

“...that if a mosquito is to become infective, it must spend all its time inside an occupied hut. It probably makes flights to a pool of water for oviposition, but rapidly return to the warm shelter of the hut”

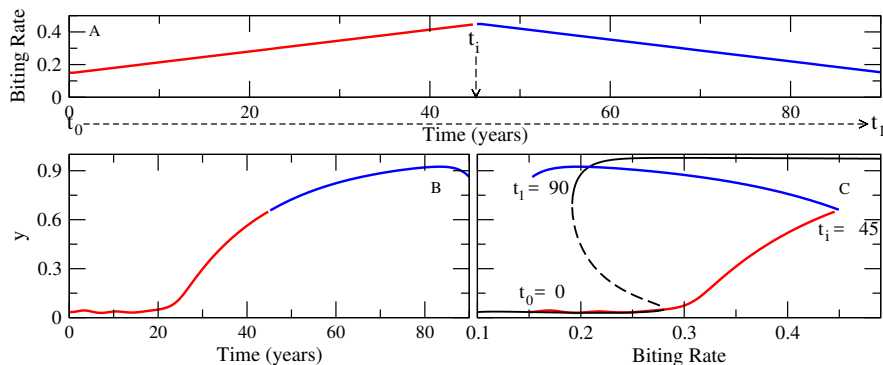
“It is apparently only because *A. gambiae* and *A. funestus* are essentially hut insects that malaria occurs at all at places over 1500 m. or so”

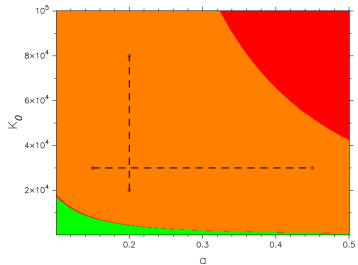
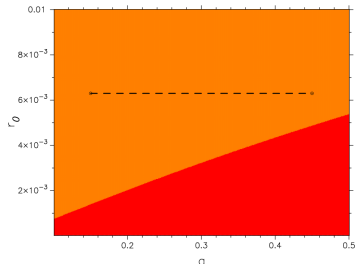
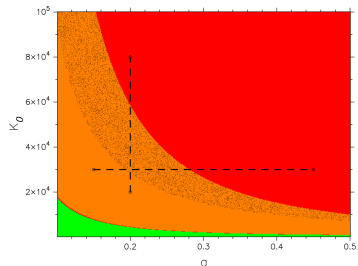
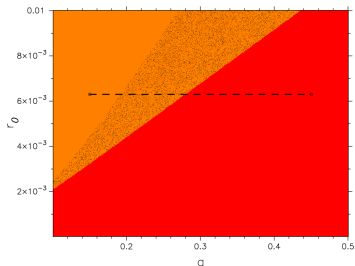
Garnham, P. (1948). The incidence of malaria at high altitudes.
J. Natl. Mal. Soc., 7, 453 275-284.

Saddle-Node Bifurcation



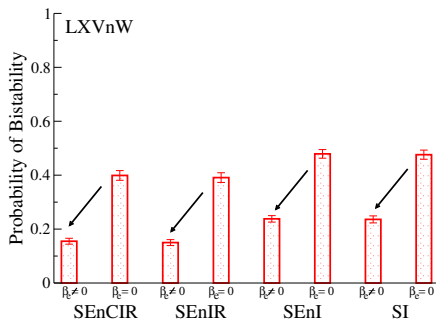
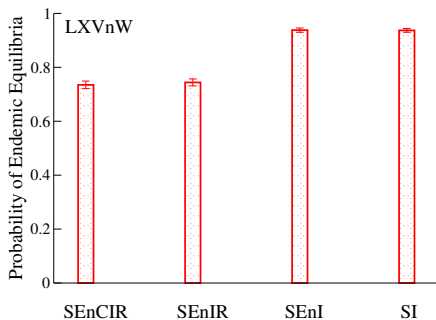
Hysteresis Cycle

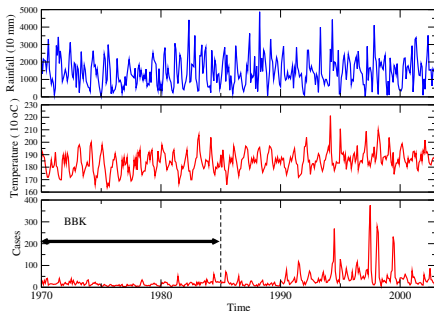




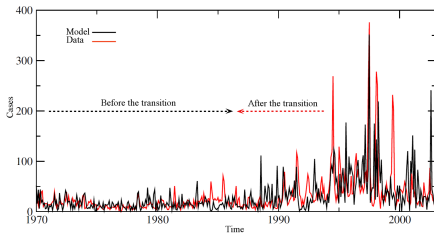
Green: Free Disease; Orange: Damped Oscillations; Red: Sink Node; Shaded: Bistability

Exploring parameter space across models of different structural complexity.

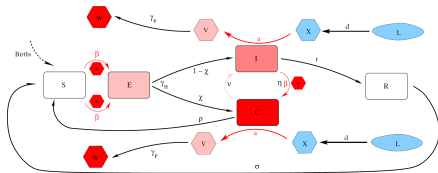




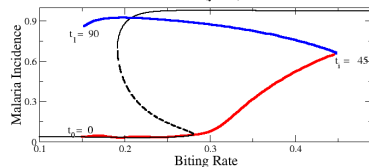
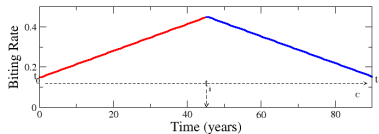
(a) Data



(c) Model Prediction



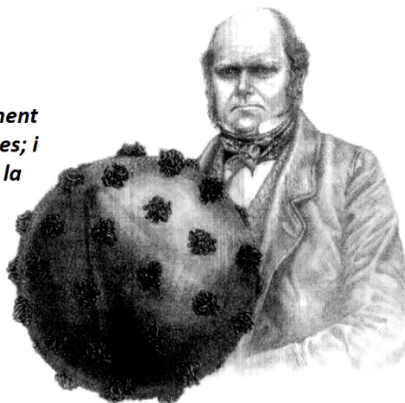
(b) Model



(d) Hysteresis

“Quan una espècie augmenta desordenadament en un període curt, sovint apareixen epidèmies; i aquí tenim un filtre limitant, independent de la lluita per la vida.”

Charles Darwin
On the Origin of Species



de Xavier López-labrador "Nou coronavirus: qui t'avisa no et vol mal"

"The world is stranger than we can imagine and surprises are inevitable in science. Thus, we found, for example, that pesticides increases pests, antibiotics can create pathogens, agricultural development creates hunger, and flood control leads to flooding. But some of these surprises could have been avoided if the problems had been posed big enough to accomodate solutions in the context of the whole"

"Les sorpreses en ciència són inevitables. Així, per exemple, trobem que els pesticides incrementen las plagues, els antibiòtics poden crear patògens més perillosos, la tecnificació de l'agricultura crea fam y el control de les inundacions condueix a inundacions majors. Tanmateix, la majoria d'aquestes sorpreses podrien evitar-se si analitzéssim els probleme en un context més ampli." (R. Levins)

T. Awerbuch, A. E. Kiszeweski, and R. Levins (2002). "Surprise, non-linearity, and complex behavior" (chap 4) a: Environmental Change, Climate and Health: Issues and Research Methods editat per P. Martens, A. J. McMichael. Cambridge University Press