

Black Hole Deconstruction

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Based on work with F. Denef, D. Gaiotto, A. Strominger and X. Yin

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1. Introduction and Motivation

The D4-D0 Black Hole

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The D4-D0 Black Hole

Macroscopically

Type IIA supergravity on CY_3 gives 4d $N = 2$ supergravity.

- ▶ Branes on non trivial cycles give 4d black holes charged under the 4d $U(1)$ vectorfields.
- ▶ Wrap a D4 on a holomorphic four cycle P and add q_0 D0's.
⇒ D4-D0 black hole

Bekenstein-Hawking Entropy

$$S = \frac{A}{4} = 2\pi \sqrt{q_0 \frac{P^3}{6}}$$

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Microscopically

The Entropy can be computed microscopically (Maldacena, Strominger, Witten 97)

- ▶ The 4d black hole corresponds to a black string in 5d.
Near horizon: $\text{AdS}_3 \times S^2$
- ▶ One can calculate the entropy microscopically using $\text{AdS}_3/\text{CFT}_2$
CFT is a reduction of M5 worldvolume theory

Interpretation of the degrees of freedom in the **supergravity regime?**

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Quantum mechanics of D0's in near-horizon region of D4-D0.

(Gaiotto, Strominger, Yin 04)

- ▶ Near horizon: $\text{AdS}_2 \Rightarrow$ superconformal quantummechanics
- ▶ Large number of D0's give non-Abelian configurations
D2's wrapping the horizon S^2 dominate entropy

Counting groundstates agrees with horizon entropy!

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This is the generator of global time, not of Poincaré time
- ▶ We will deconstruct the D4-D0 into **zero entropy** bits
- ▶ Bonus: near geometry becomes **global** AdS

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Multi Center Black Holes

Multi center black holes in 4d $N = 2$ SUGRA

(Denef 00; Bates, Denef 03)

- ▶ The centers can carry both electric and magnetic charge:

$$\Gamma = (p^0, p, q, q_0)$$

- ▶ Metric: $ds^2 = -S^{-1}(dt + \omega)^2 + S dx^i dx^i$

Solution is given in terms of harmonic functions

$$H^\Lambda = \sum_a \frac{p_a^\Lambda}{r_a} + h^\Lambda \quad \Lambda \in \{0, 1\}$$

$$H_\Lambda = \sum_a \frac{q_a^\Lambda}{r_a} + h_\Lambda$$

E.g. $S(p^0, p, q, q_0) \rightarrow S(H^0, H^1, H_1, H_0)$

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Molecular-like **bound** states

- ▶ N-1 stability conditions

$$\sum_{b \neq a} \frac{\langle \Gamma_a, \Gamma_b \rangle}{r_{ab}} = \langle h, \Gamma_a \rangle \quad \langle \Gamma_a, \Gamma_b \rangle \equiv -p_a^0 q_b^b + p_a q^b - q^a p_b + q_0^1 p_b^0$$

- ▶ For two centers:

$$r_{12} = \frac{\langle \Gamma_1, \Gamma_2 \rangle}{\langle h, \Gamma_1 \rangle}$$

Through the constants h the equilibrium distance depends on the asymptotic Kähler moduli.

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Relation to 5d

(Gaiotto, Strominger, Yin 05; Behrndt, Cardoso, Mahapatra 05)

Applying the standard **Type IIA / M-theory** connection:

Type IIA on CY_3	\longleftrightarrow	M-theory on CY_3
	\Updownarrow	
4d multi-centered black holes	\longleftrightarrow	5d black holes and black rings
D6 black hole	\longleftrightarrow	gravitational monopole (Taub-NUT)
D4 black hole	\longleftrightarrow	M5 black string/ring
D2 black hole	\longleftrightarrow	M2 black hole
D0 black hole	\longleftrightarrow	gravitational wave

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Deconstruction: D4-D0 \rightarrow D6- $\overline{\text{D6}}$ -D0

Setup

The system of our interest:

- ▶ Bound state of purely fluxed D6, purely fluxed $\overline{\text{D6}}$ and n D0's.
- ▶ Simple D6 $\Gamma = (1, 0, 0, 0)$

\Rightarrow worldvolume magnetic flux F induces lower brane charges

$$\Gamma = e^F = \left(1, F, \frac{F^2}{2}, \frac{F^3}{6}\right)$$

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▶ n D0's $\Gamma_3 = (0, 0, 0, -n)$

Total charge

$$\Gamma_t = (0, P, 0, \frac{P^3}{24} - n)$$

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All have zero entropy!

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Scaling limit

To connect to the $D4-D0$ black hole we take a scaling limit.

- ▶ Redefine $x = \lambda \tilde{x}$, then take the limit $\lambda \rightarrow 0$ while keeping \tilde{x} fixed.
- ▶ This amounts to dropping the constants in the harmonic functions.
- ▶ Physically the centers fall inside an infinitely deep throat

For an asymptotic observer **indistinguishable** from a single black hole

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The equilibrium distances are now given by

$$r_{ab} = c \langle \Gamma_a, \Gamma_b \rangle$$

► Not always possible!

$$\langle \Gamma_1, \Gamma_2 \rangle + \langle \Gamma_2, \Gamma_3 \rangle \geq \langle \Gamma_3, \Gamma_1 \rangle \quad \text{and cyclic permutations}$$

In our case: $n \geq \frac{p^3}{12}$

Equilibrium distances

$$\frac{p^3}{12} \frac{1}{R_6} = \frac{n}{\sqrt{R_0^2 + R_6^2}}$$

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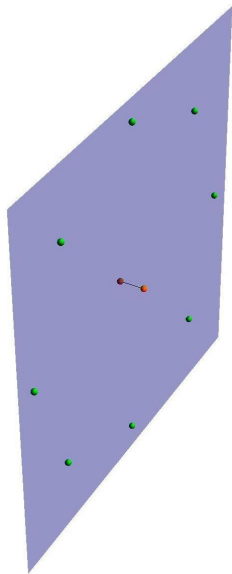
Pair of **bound** $D6-\overline{D6}$

- ▶ n $D0$'s in bound orbits

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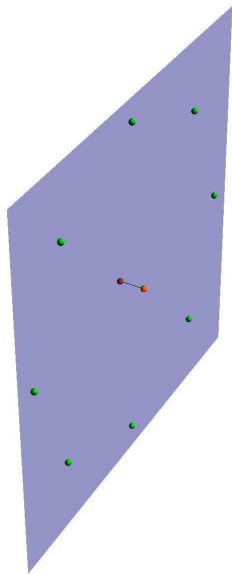
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Different regions

We can now distinguish two interesting regions

They are naturally interpreted in the 5d picture

▶ Far Region: quotient of Poincaré $AdS_3 \times S_2$

Not so surprising: near horizon geometry of the lifted $D4-D0$

▶ Near Region: global $AdS_3 \times S_2$

Rather surprising

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Near region

D6- $\overline{\text{D6}}$ vs Global $\text{AdS}_3 \times \text{S}_2$

- ▶ In 5d: Taub-NUT and Anti-Taub NUT \Rightarrow non-trivial S^2
- ▶ Flux p sources magnetic flux on this S^2
- ▶ Use **prolate spheroidal coordinates**

$$|x - x_6| = R_6(\cosh \rho + \cos \eta)$$

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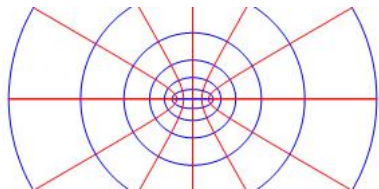


Figure: Prolate coordinates

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Reintroducing the D0's

Idea: **reintroduce** the D0's as probes in the **near region**

Quantummechanics

- ▶ Superconformal
- ▶ Natural time generator $\sim L_0$
- ▶ As before we expect non-Abelian configurations

By analogy to GSY we reproduce the BH entropy.

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Introducing D2's

Where can the D2's sit?

- ▶ Obvious candidate in the 5d picture: the near S^2

\sim Particle spinning in AdS_3

\rightarrow angular momentum $J = -\frac{p^3}{3} \sinh^2 \rho_*$

- ▶ The near S^2 extends to a SUSY cycle in the full geometry
- ▶ This S^2 is contractible at infity \Rightarrow no conserved M2-charge

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Where can the D2's sit?

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\sim Particle spinning in AdS_3

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Ellipsoidal D2 with electric and magnetic worldvolume flux

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The entropy is reproduced by quantizing this system and counting ground states.

Along the way

- ▶ $D6-\overline{D6}$ lifts to global $AdS_3 \times S^2$
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Outlook

There still are some steps missing!

- ▶ The **Myers effect** needs to be understood more explicitly for this configuration.
- ▶ It would be interesting to understand **backreaction** of M2/D2 branes.

(Denef, VdB, Vercoocke in progress)

Related questions

(De Boer, Denef, El-Showk, Messamah, VdB in progress)

- ▶ What about non scaling systems?
- ▶ Relation to $\text{AdS}_3/\text{CFT}_2$?