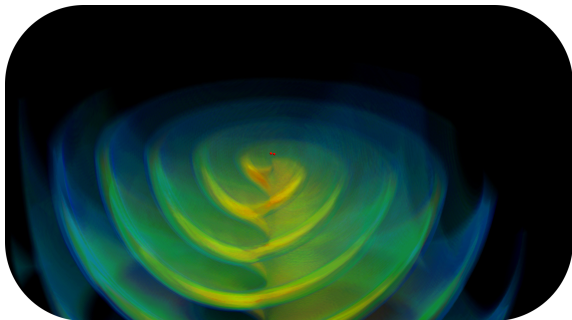


Simulating Generic Binary Neutron Star Mergers

Tim Dietrich

Albert Einstein Institute

December 14th 2016



BNS parameter space

Parameters:

- Mass M
- Mass ratio q
- Spin $\vec{S}^A, \vec{S}^B$
- EOS

BNS parameter space

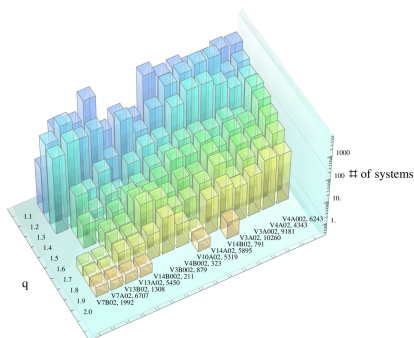
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Mass ratio: most observed BNS have comparable masses around $\sim 1.35M_{\odot}$
in situ models predict mass ratios up to $q \approx 1.8$

Recent observation of two $q \approx 1.3$ BNS systems

$\Rightarrow$ high-mass ratios are possible



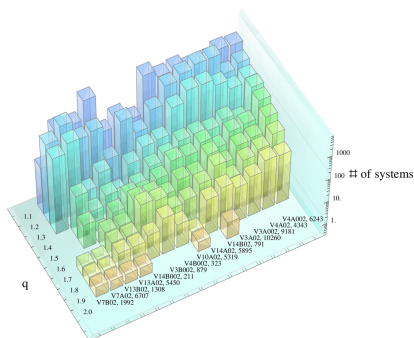
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Spin:

single NS observed up to 716Hz
 $(\chi \sim 0.3 - 0.6)$

BNS observed up to 44Hz

$\Rightarrow$ NS are spinning objects

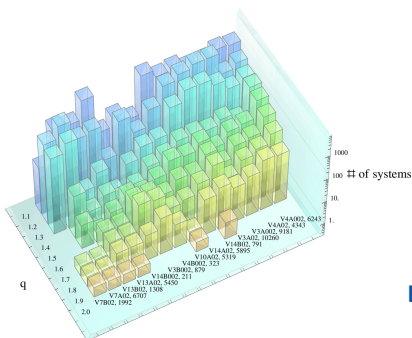
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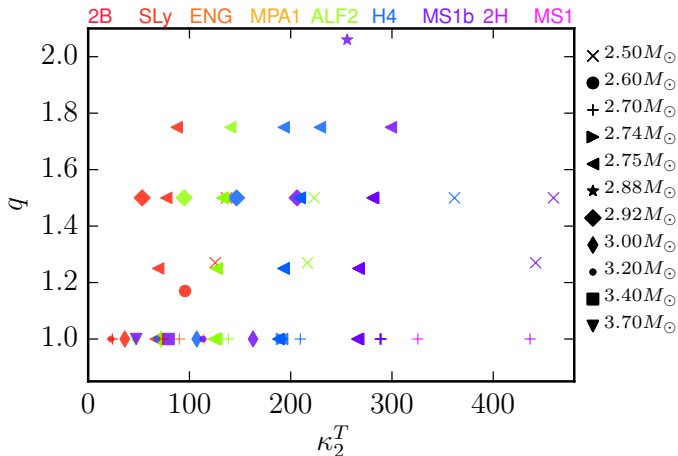
Investigation of BNS parameter space

BNS parameter space

Mass	$M = M^A + M^B$
Mass ratio	$q = M^A / M^B$
EOS	

BNS parameter space

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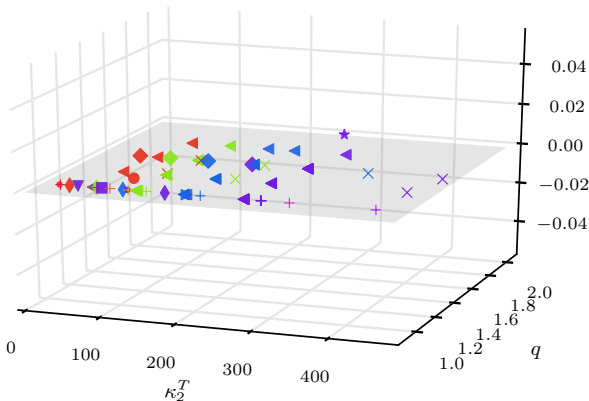
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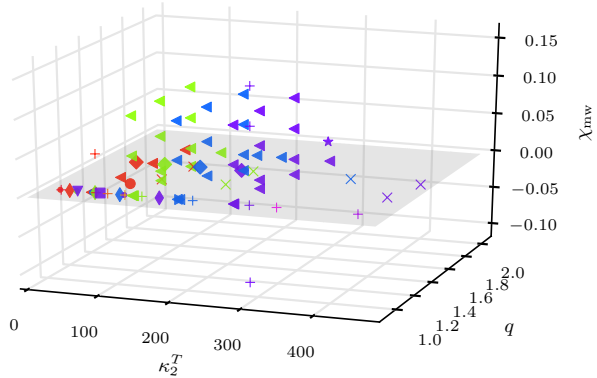
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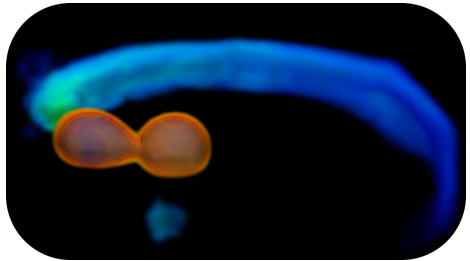


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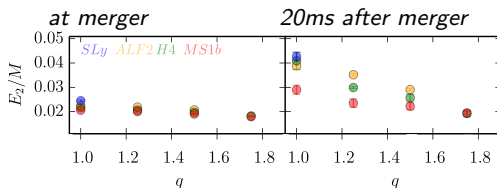


Effect of the mass-ratio



Effect of the mass-ratio: GW signal

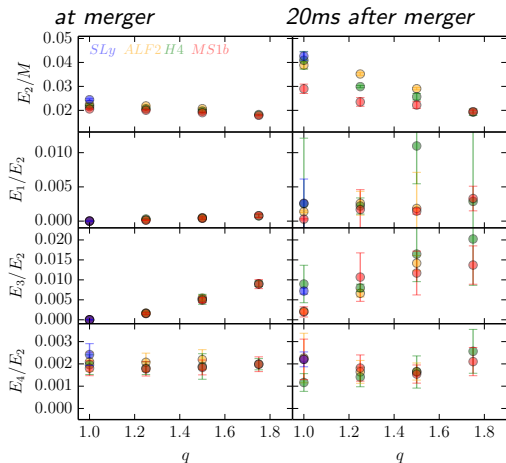
Amount of radiated energy



- released energy decreases for increasing q
- subdominant modes become important for increasing q
- excitation of all modes in postmerger independent of q

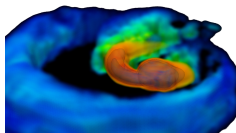
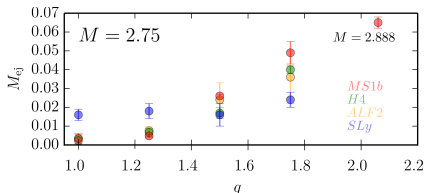
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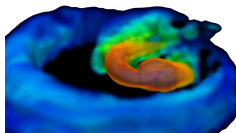
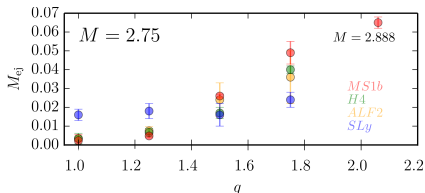
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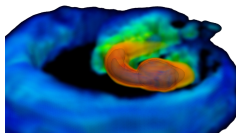
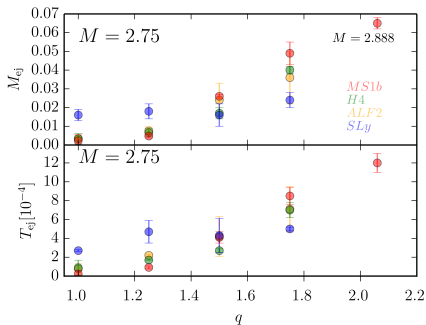
- ejecta mass almost linear in q
- kinetic energy almost linear in q
- ejecta velocity in orbital plane approx. constant
- ejecta velocity perpendicular to orbital plane decreases

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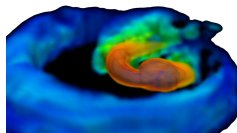
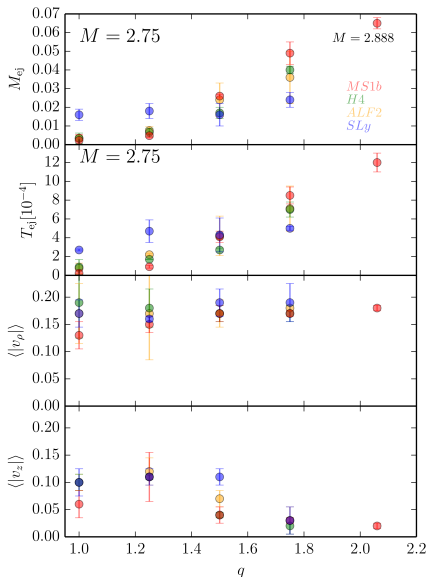
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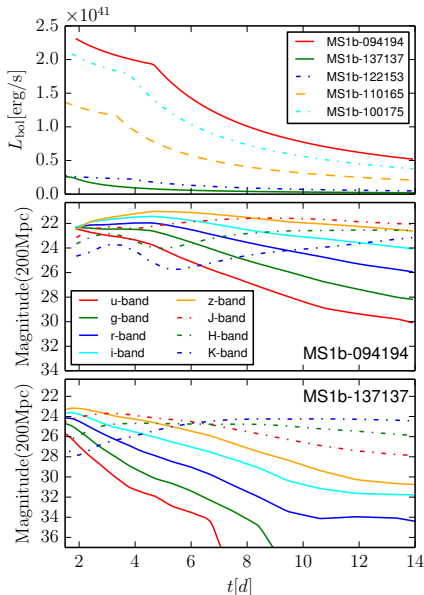
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Effect of the mass-ratio: EM counterparts



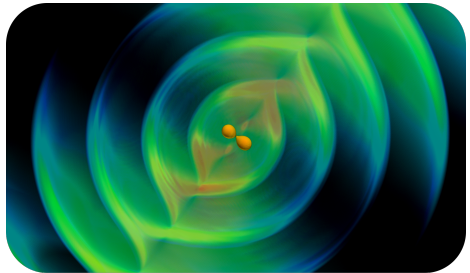
• kilonovae:

- unequal mass ratios more luminous
- peak luminosity at later times for large q
- temperature at peak smaller for large q

• radio bursts:

- higher fluency for larger q
- peak time months/years later for large q

Effect of the Spin

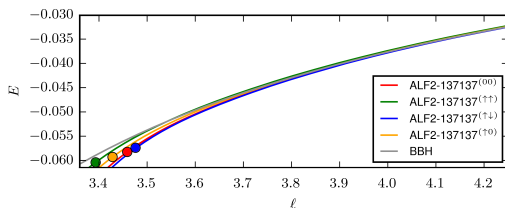


Effect of the Spin: conservative dynamics

$E(\ell)$

E ... binding energy

ℓ .. specific orbital angular momentum

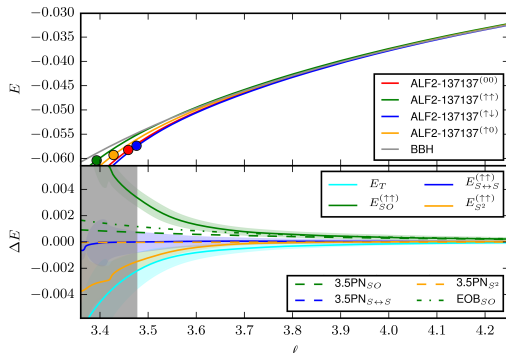


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$$E \approx \underbrace{e_0}_{\text{point particle}} + \underbrace{e_T}_{\text{tidal}} + \underbrace{e_{SO}}_{\text{spin-orbit}} + \underbrace{e_{S \leftrightarrow S}}_{\text{spin-spin}} + \underbrace{e_{S^2}}_{\text{self spin}}$$

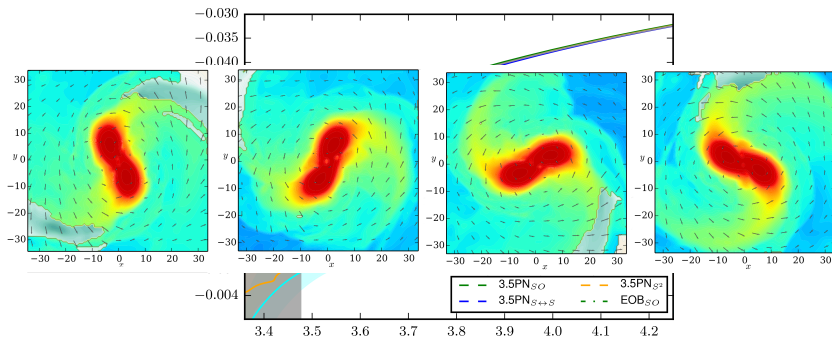
$\Rightarrow$ for $\chi \sim 0.1$ **spin-orbit-term dominant** up to merger

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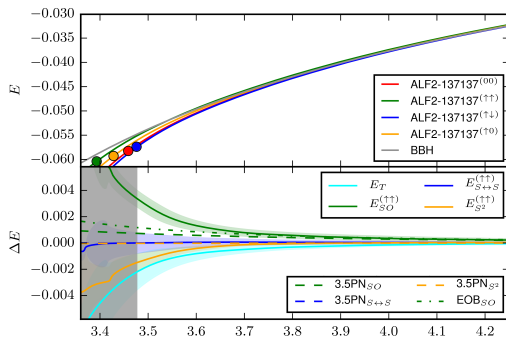
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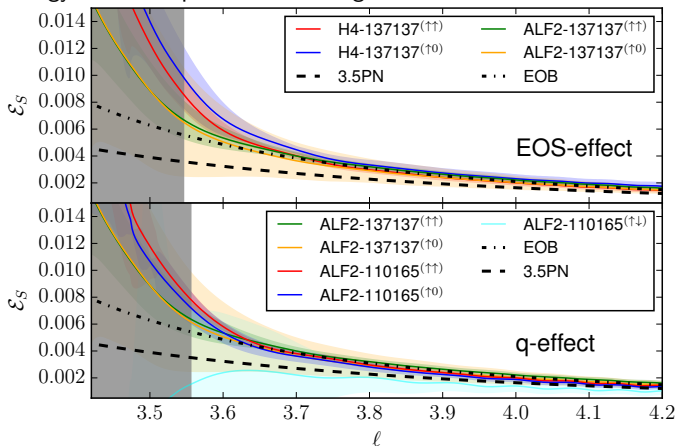
$\Rightarrow$ spins **have to** be included for modeling binary pulsar systems

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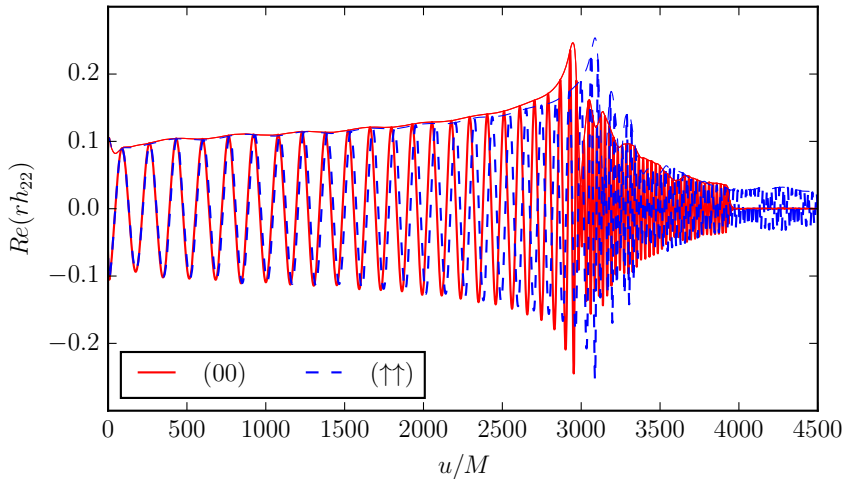


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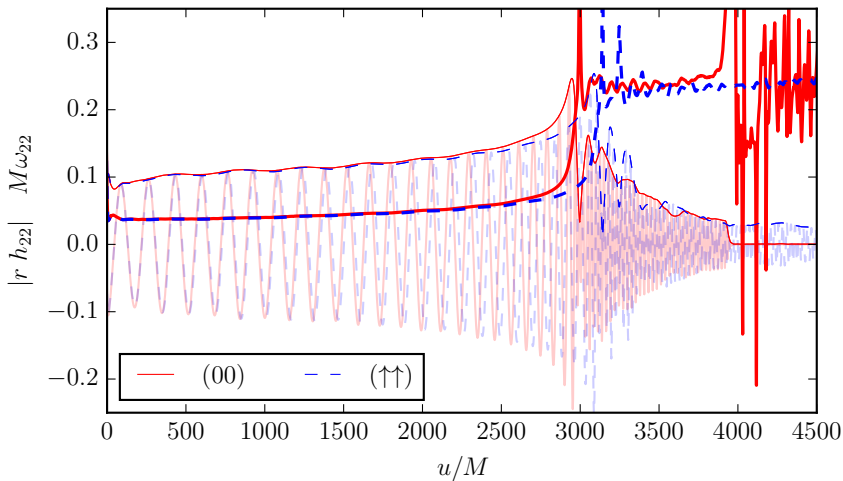
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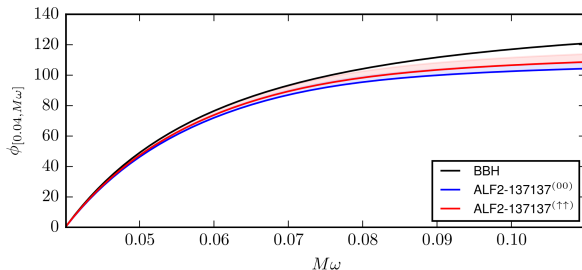


Effect of the Spin: GW

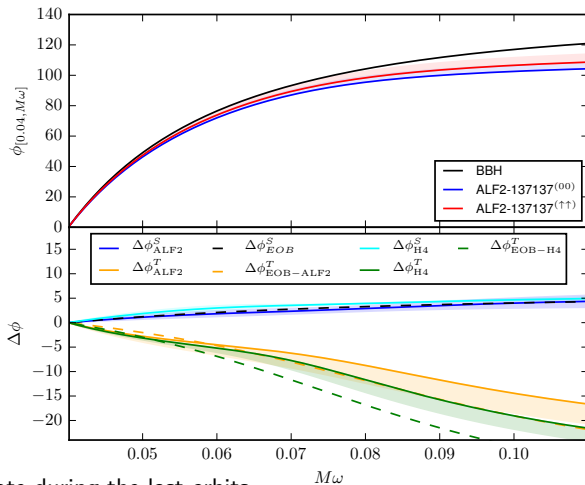


$$\phi(t), M\omega(t) \Rightarrow \phi(M\omega)$$

Effect of the Spin: GW

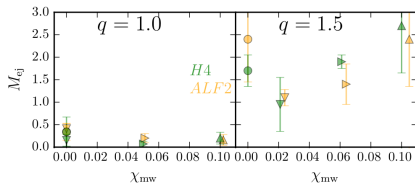


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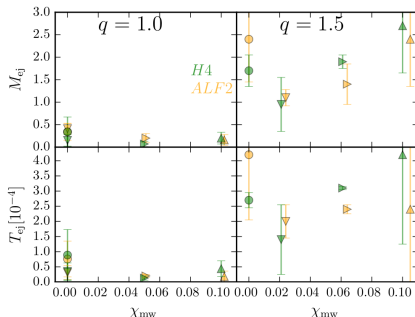
- tidal effects dominate during the last orbits
- neglecting spin would create biases in parameter estimation

Effect of the Spin: Ejecta & EM counterparts



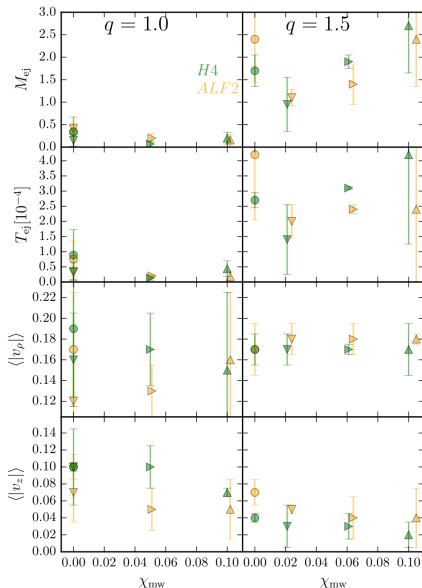
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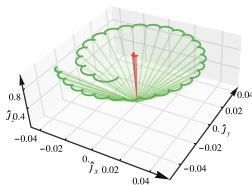
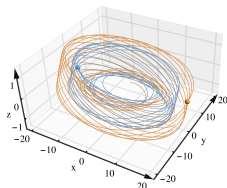


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Effect of the Spin: Precession

$M_A = 1.35M_\odot$ and $M_B = 1.11M_\odot$ for SLy-
EOS

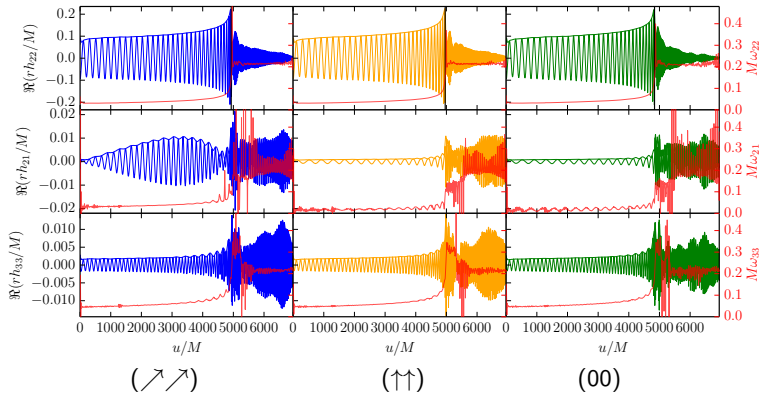
	χ^A	χ^B
$(\nearrow \nearrow)$	0.13	0.16
$(\uparrow \uparrow)$	0.08	0.09
(00)	0.00	0.00



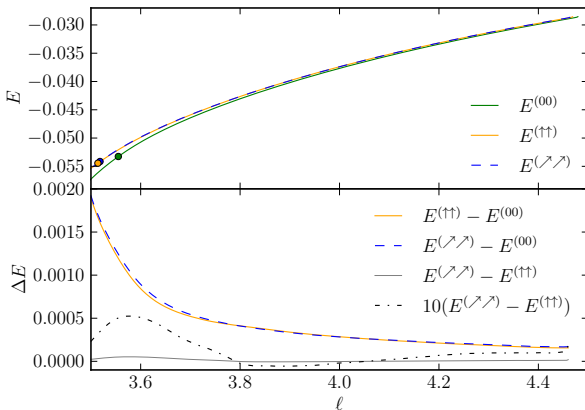
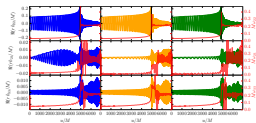
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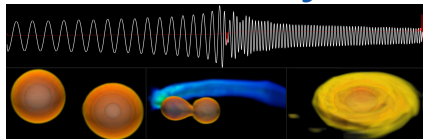
Effect of the Spin: Precession



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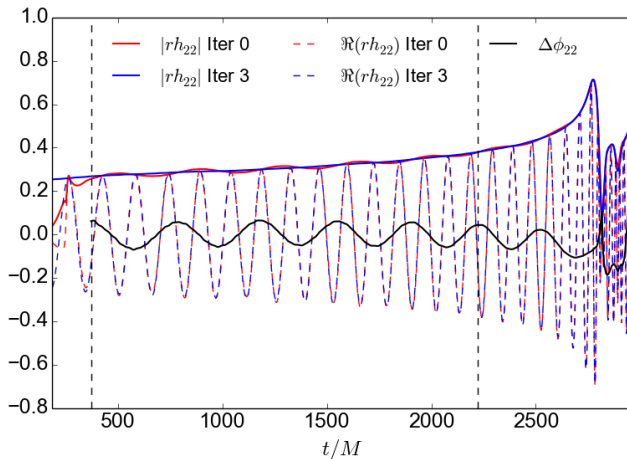
Improving Waveform accuracy



Improving the accuracy of our results

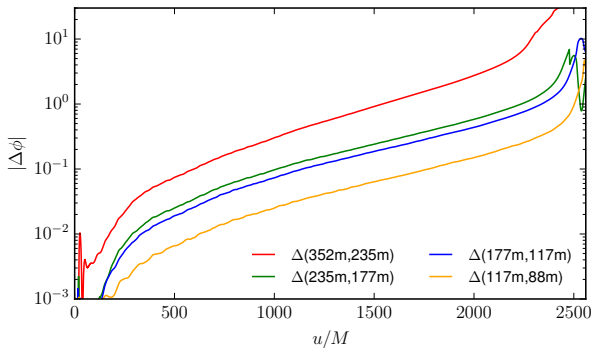
- (1) eccentricity reduced data for GW modeling
- (2) implemented different flux and reconstruction methods $\Rightarrow$ clean convergence across multiple resolutions

Eccentricity reduced data



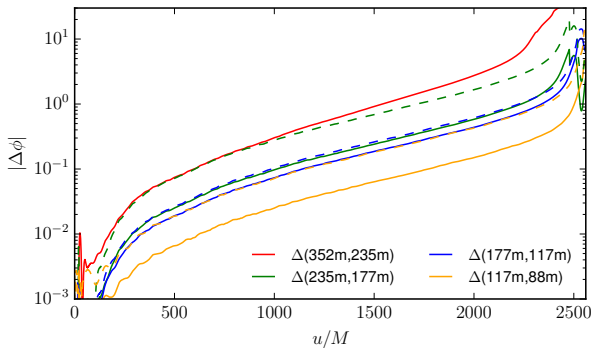
- “real” systems will have negligible eccentricity
- low-eccentricity needed for accurate NR - AR work

Clean Convergence



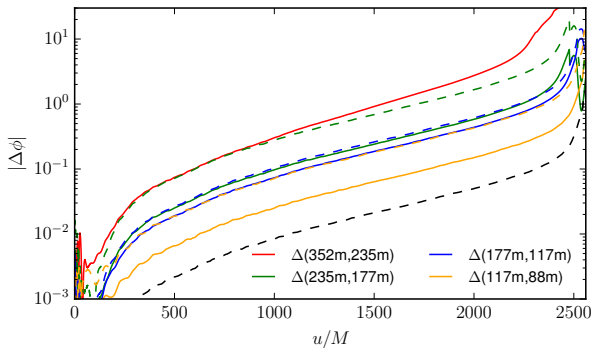
- dominant error in BNS waveforms caused by finite resolution
- consistent convergence order across multiple resolutions and over time needed for error estimate

Clean Convergence



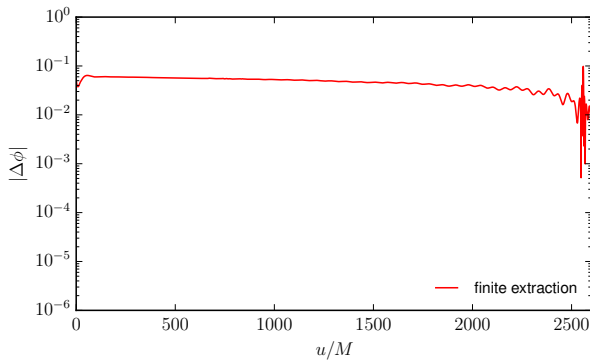
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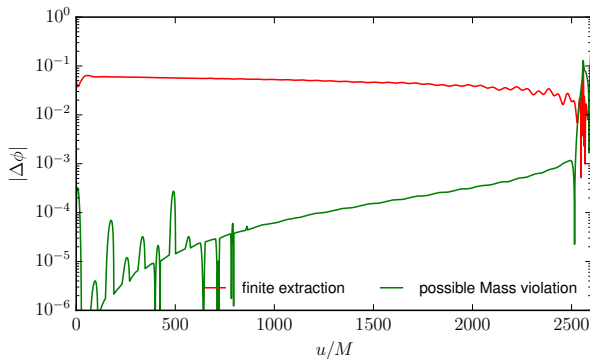


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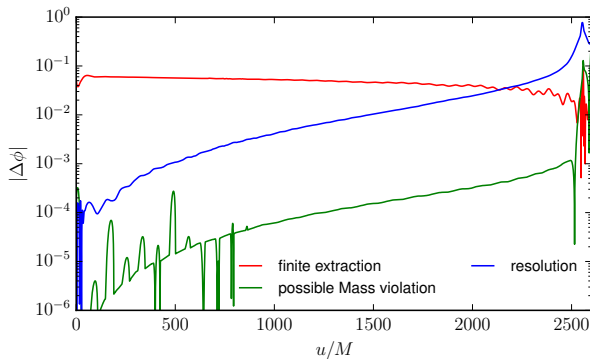
Proper Error Estimate and NR/AR comparisons



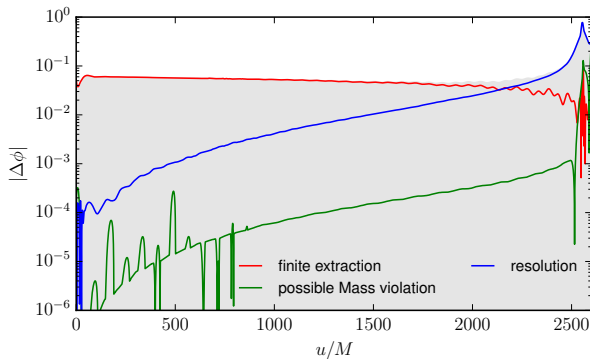
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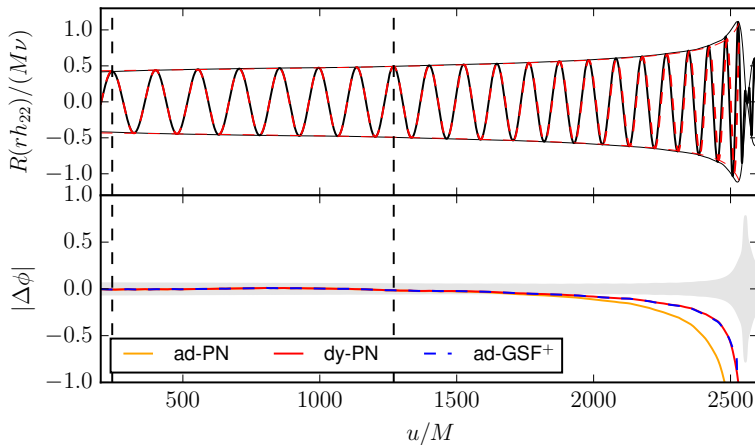
Proper Error Estimate and NR/AR comparisons



Proper Error Estimate and NR/AR comparisons



Proper Error Estimate and NR/AR comparisons



Summary

- Improvements in the construction of our initial data
- Large parameter space study regarding mass-ratio and spin
 - ejecta mass and luminosity increase for large q and aligned spin
- first precessing BNS merger
 - influence of precession small compared to spin-orbit effect
- improving accuracy and robust error budget allows further NR/AR improvements

