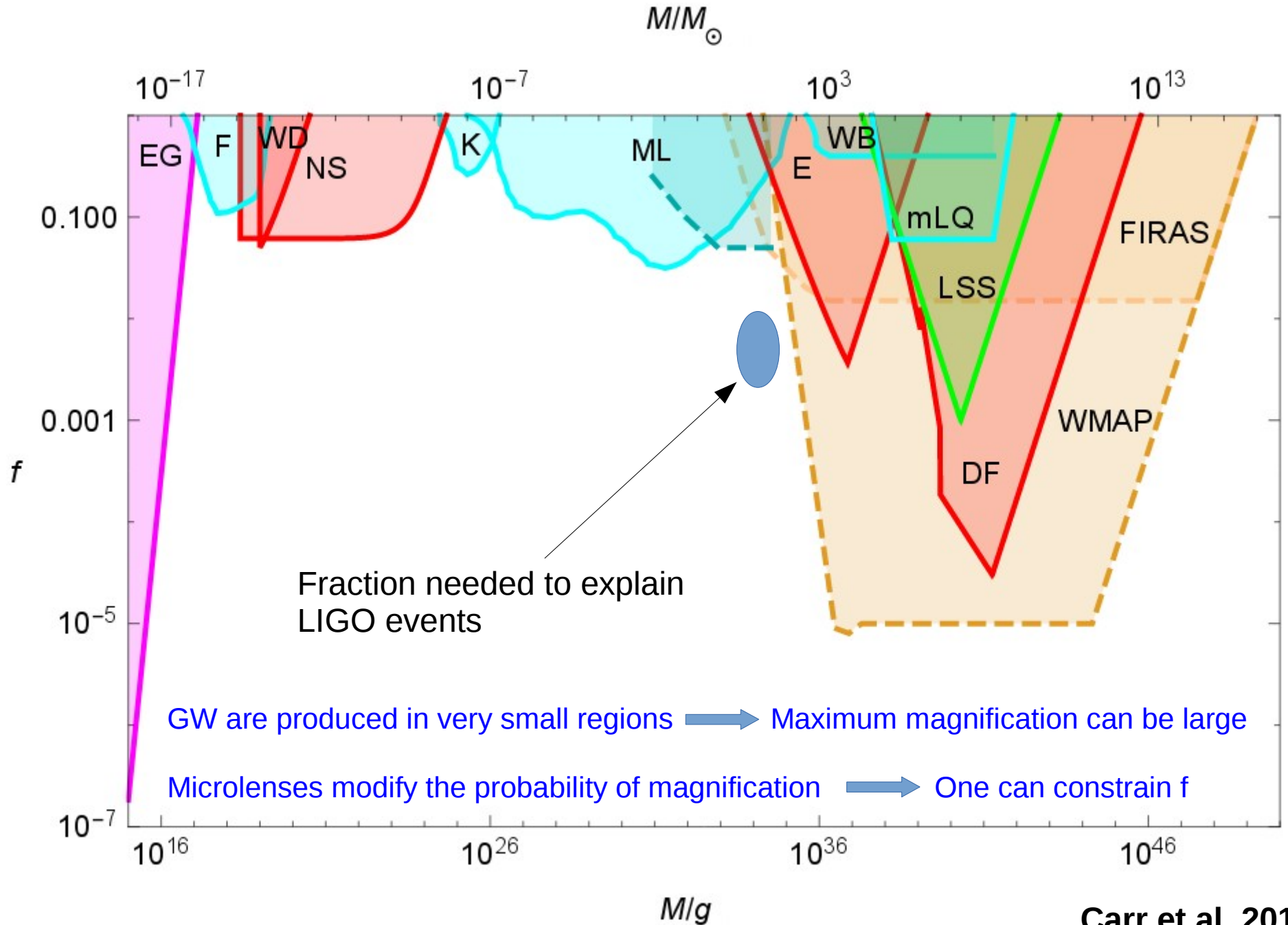


# Constraining Compact DM with lensed GWs

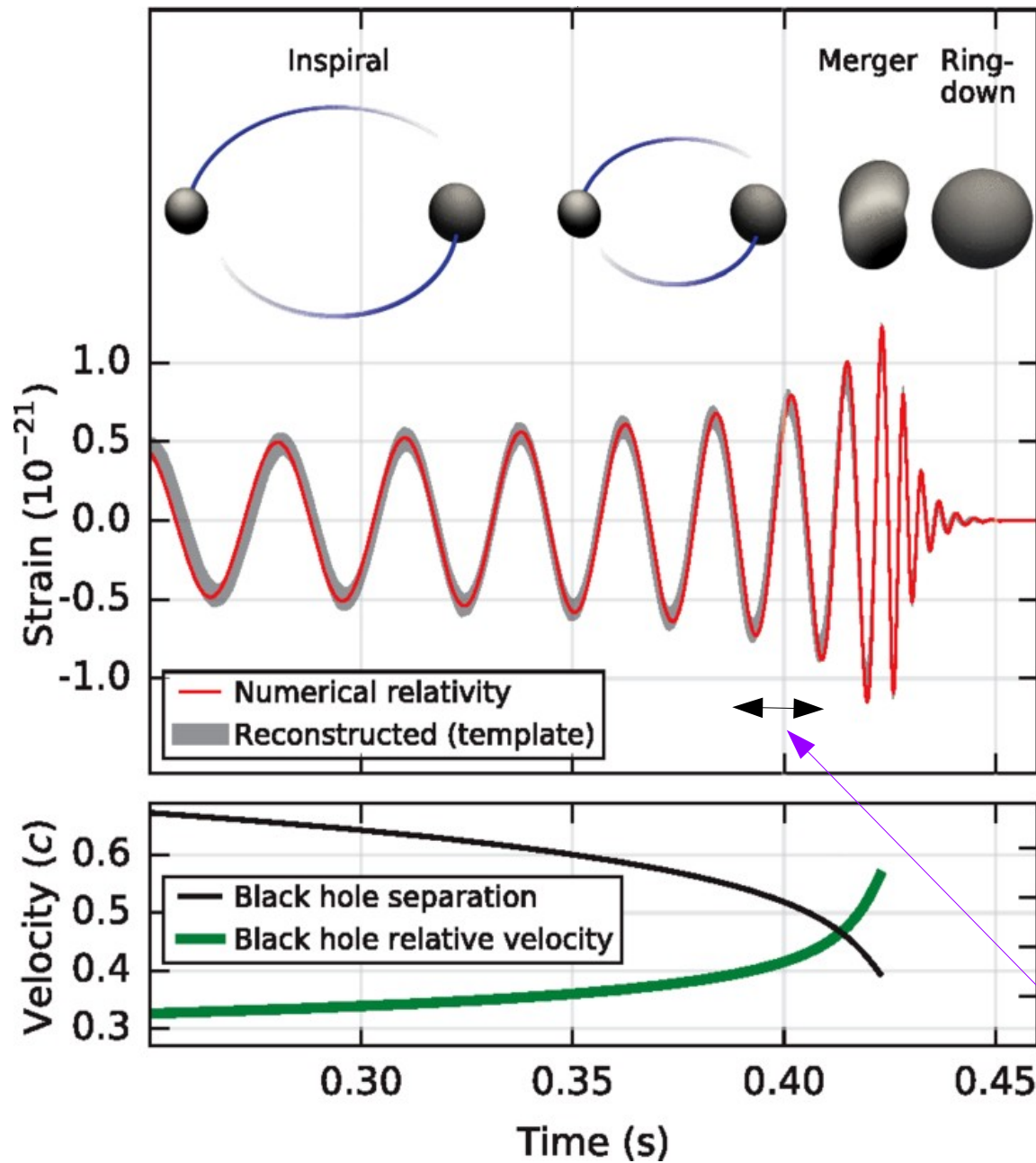


Jose M. Diego  
jdiego@ifca.unican.es

# Constraints on the total mass fraction in the form of PBH



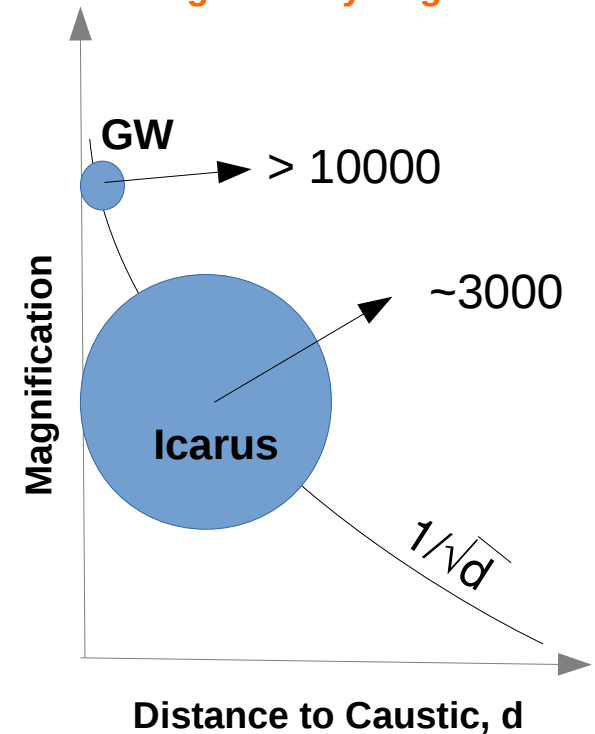
# Gravitational Waves



## Very small source

Subject to very large magnifications

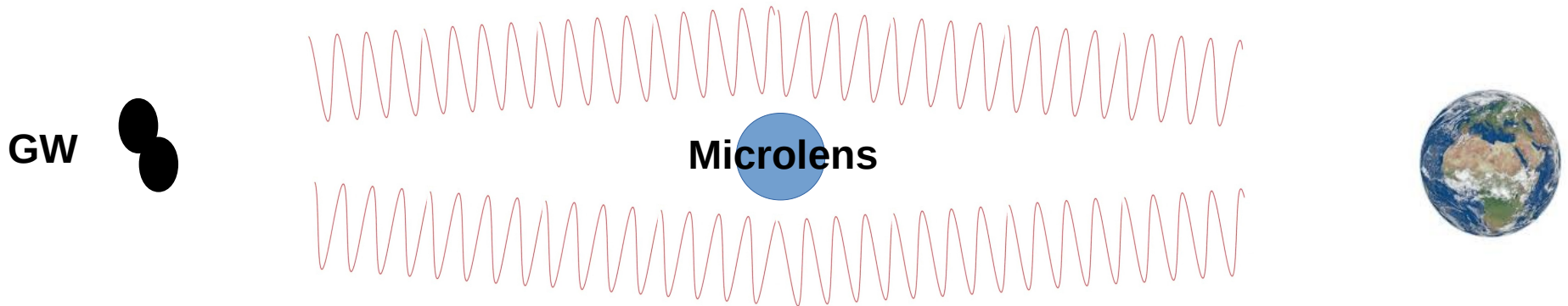
“Smaller objects can be magnified by larger factors”



Period  $\sim$  millisecond

## MOTIVATION

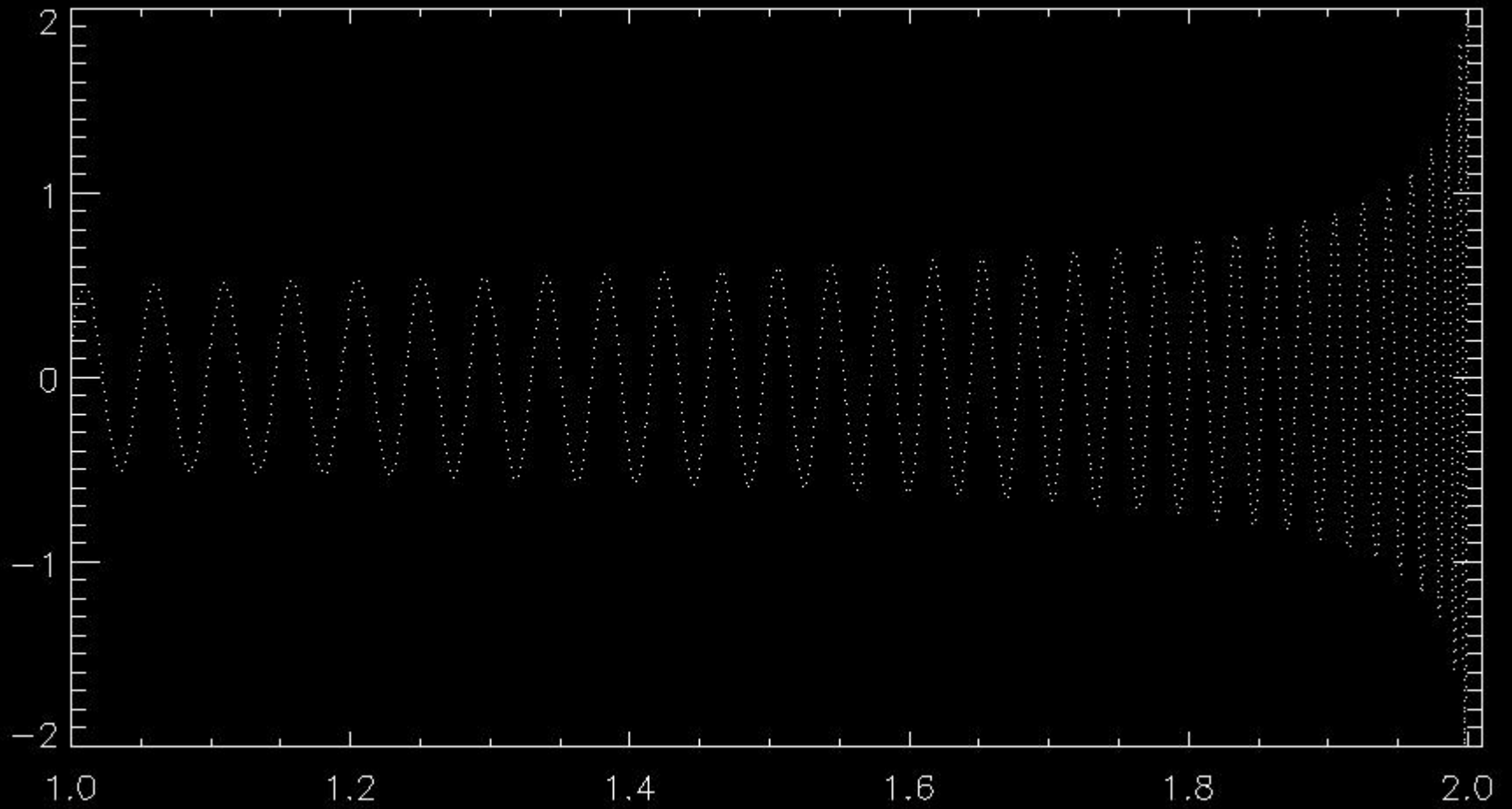
Since the period of GW is of order 1 millisecond, microlensing by objects which introduce time delays of order 1 millisecond will result in interference between the multiple microlensed images.



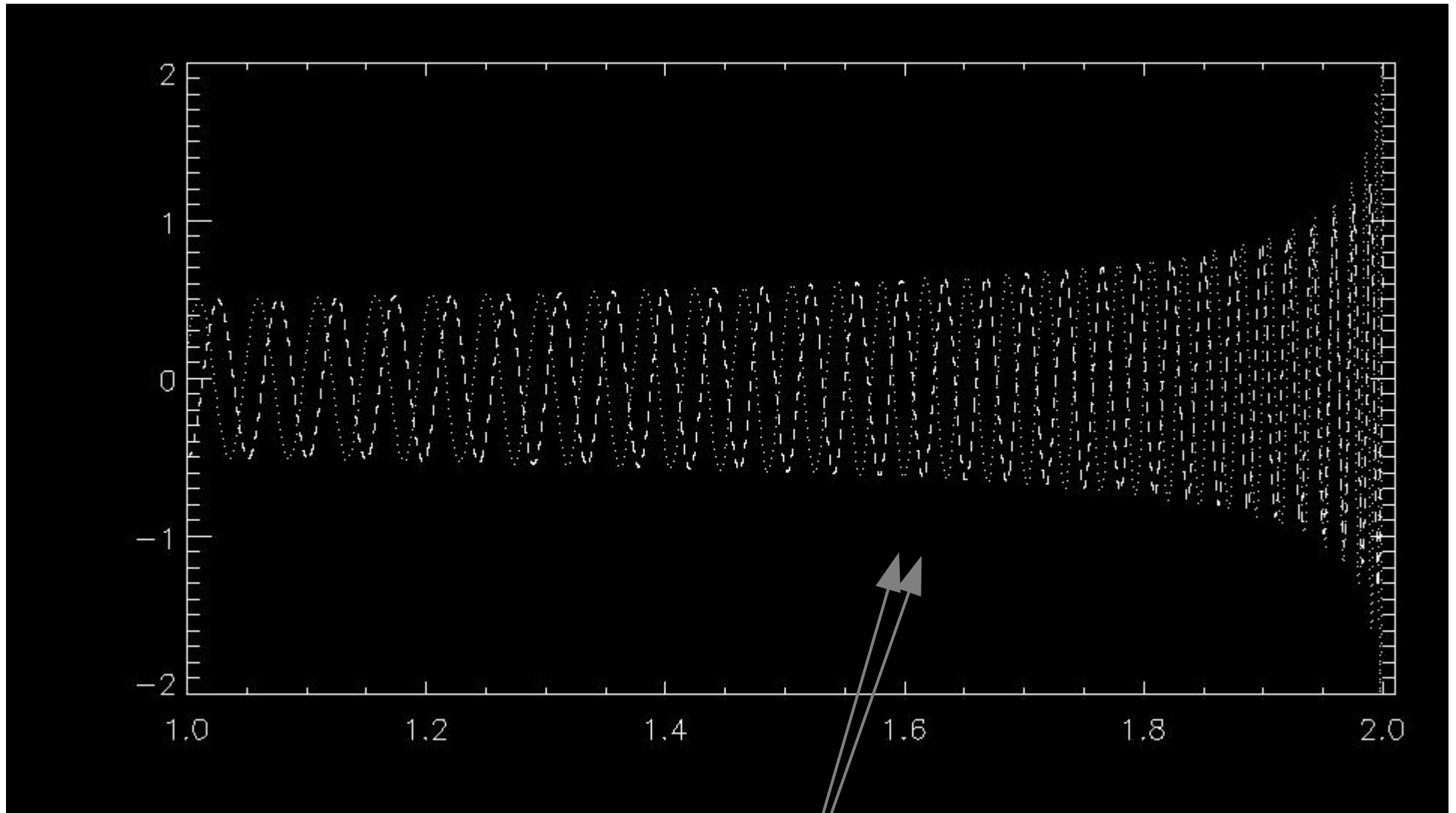
PBHs at cosmic distances with masses a few tens of solar masses, can produce such time delays.



# Interference of GW

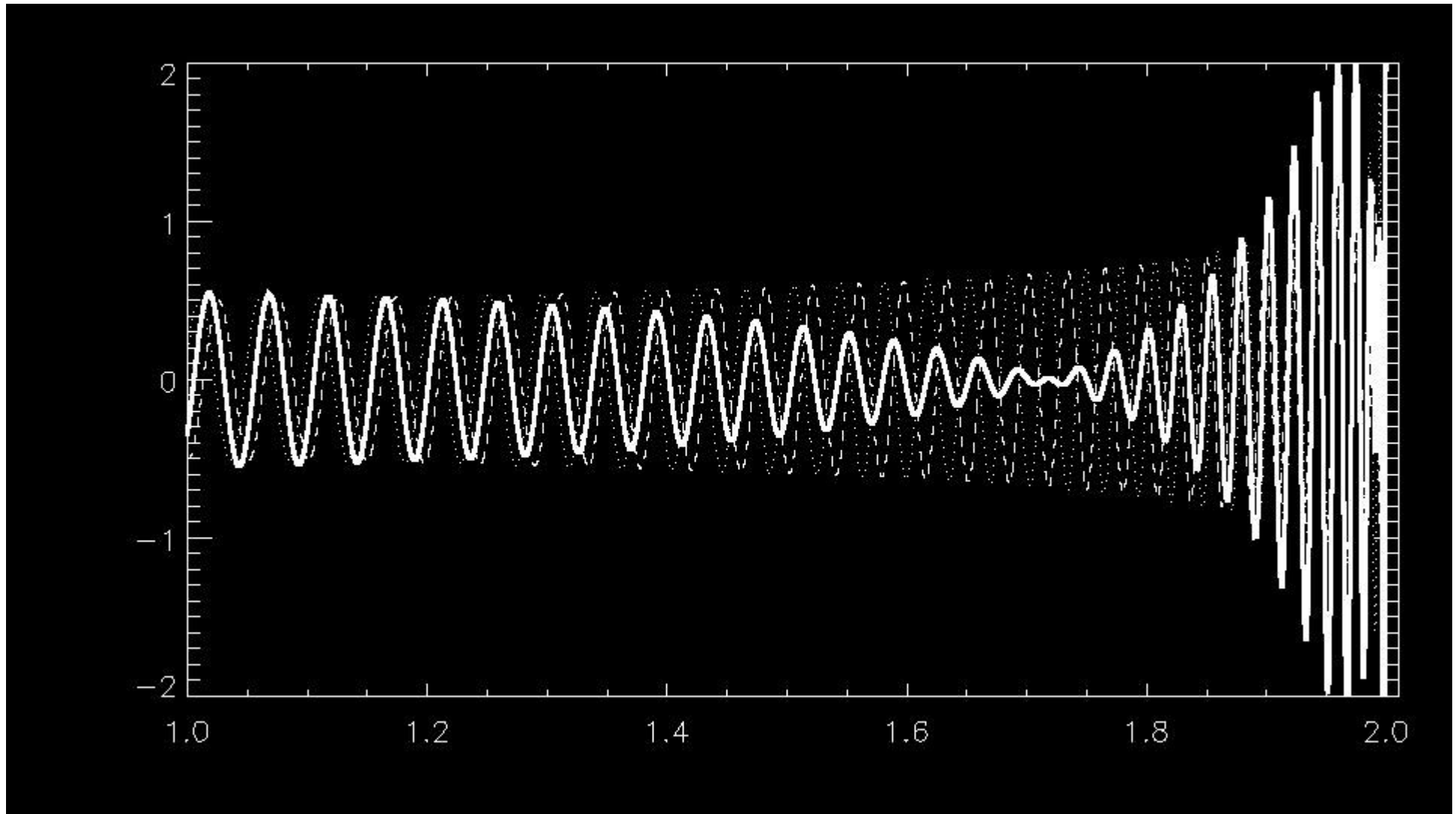


# Interference of GW



Relative shift proportional to the mass of the microlens

# Interference of GW



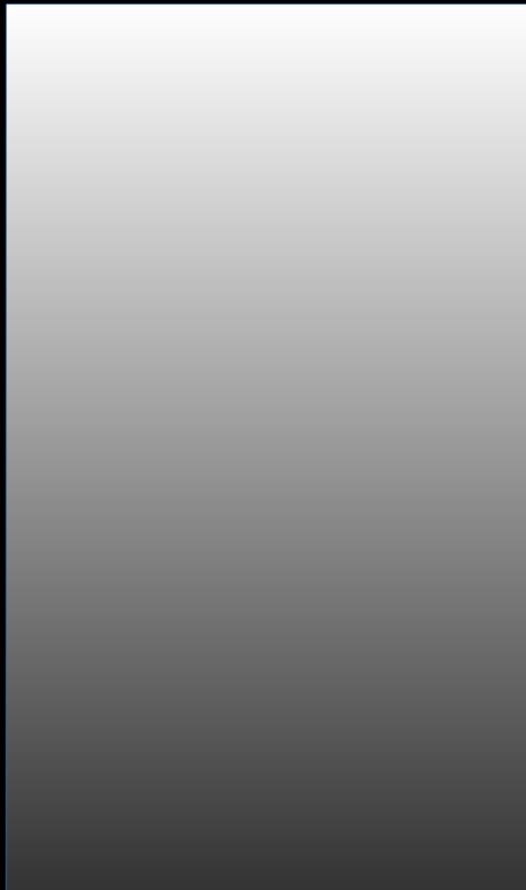
**Magnification depends on Frequency**

**Assume wave optics and solve diffraction integral in Fourier space**

**Looks like misalignment of spins**

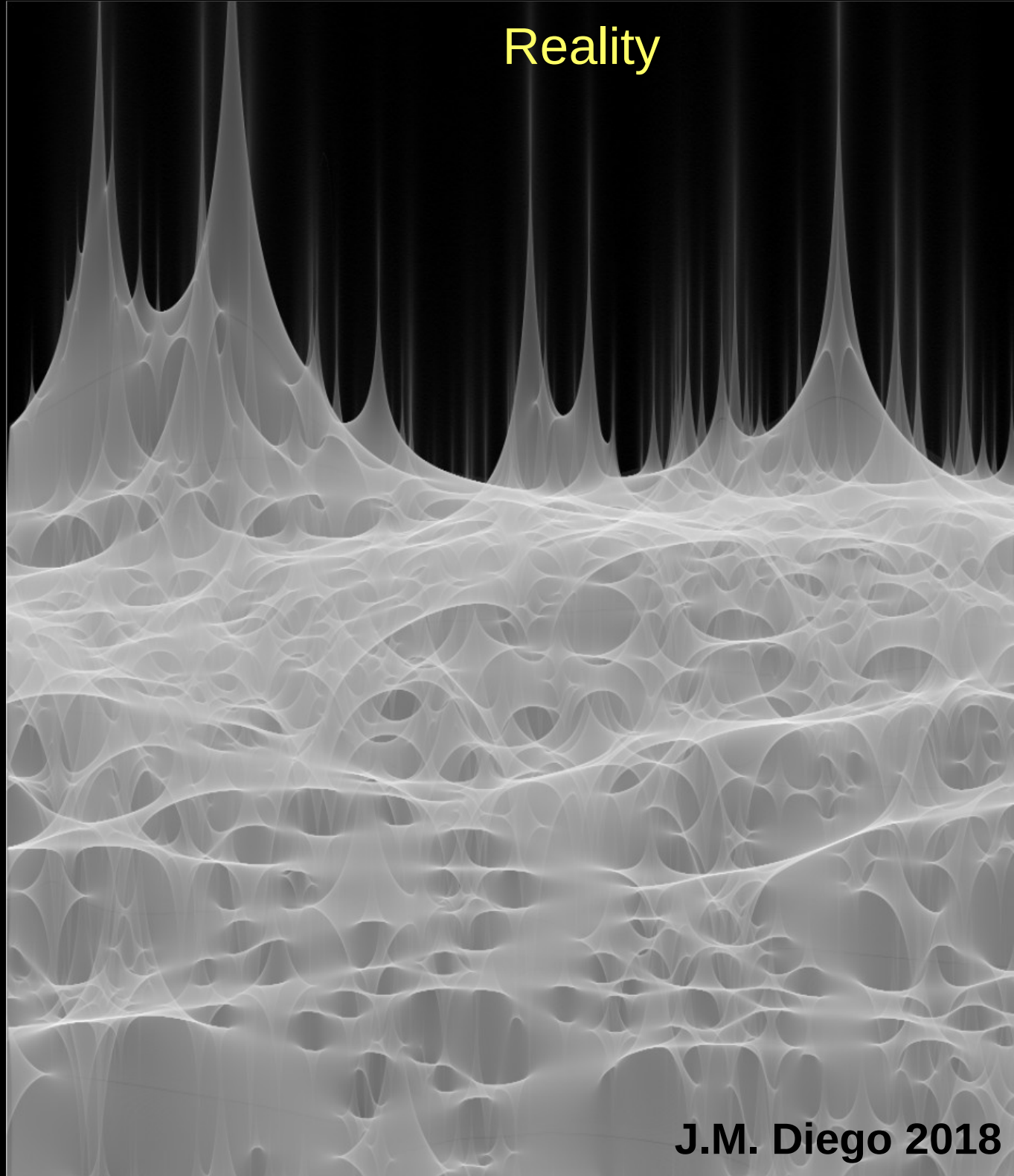
# “Classic” View

Caustic region  
without microlenses



**VS**

# Reality

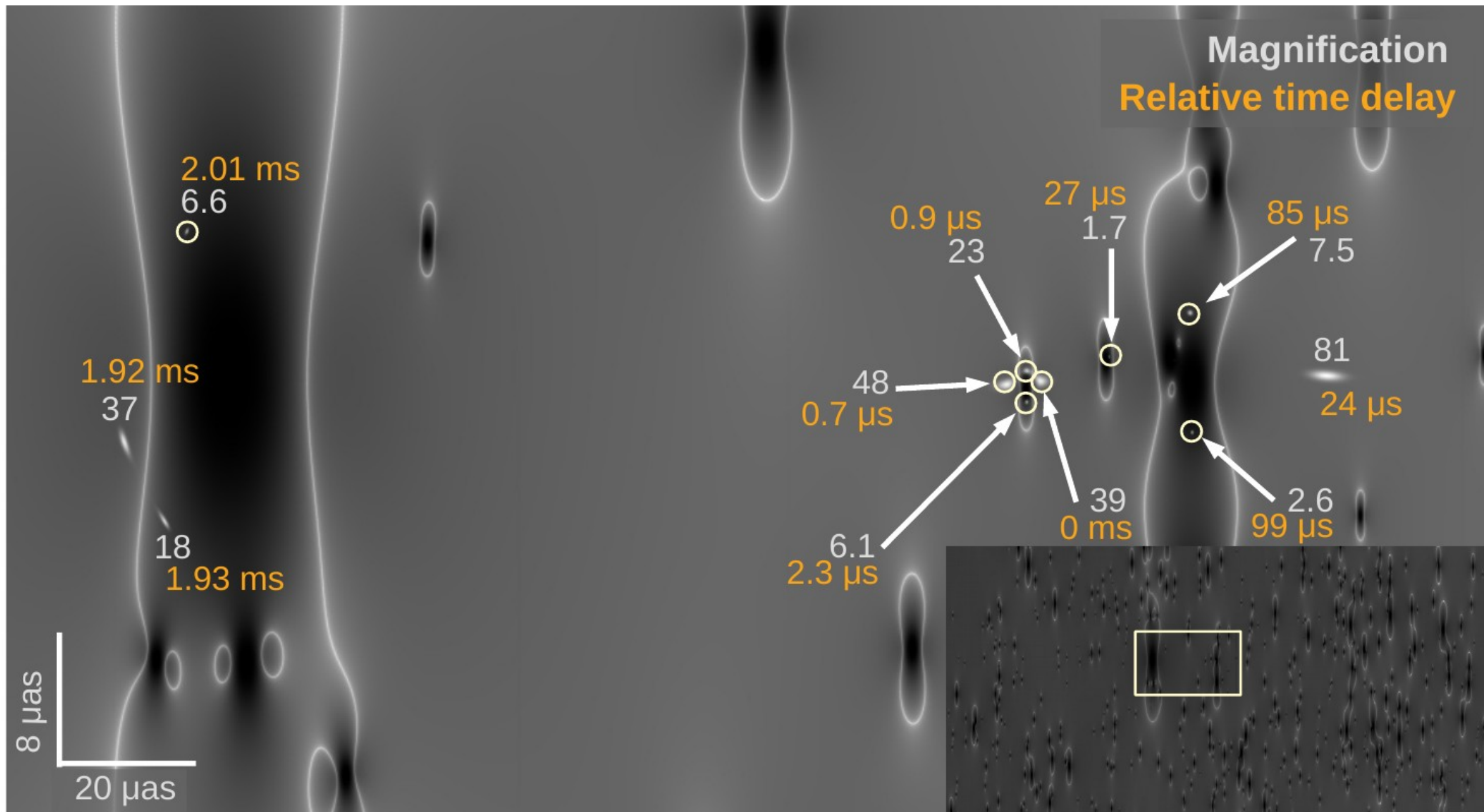


**J.M. Diego 2018**



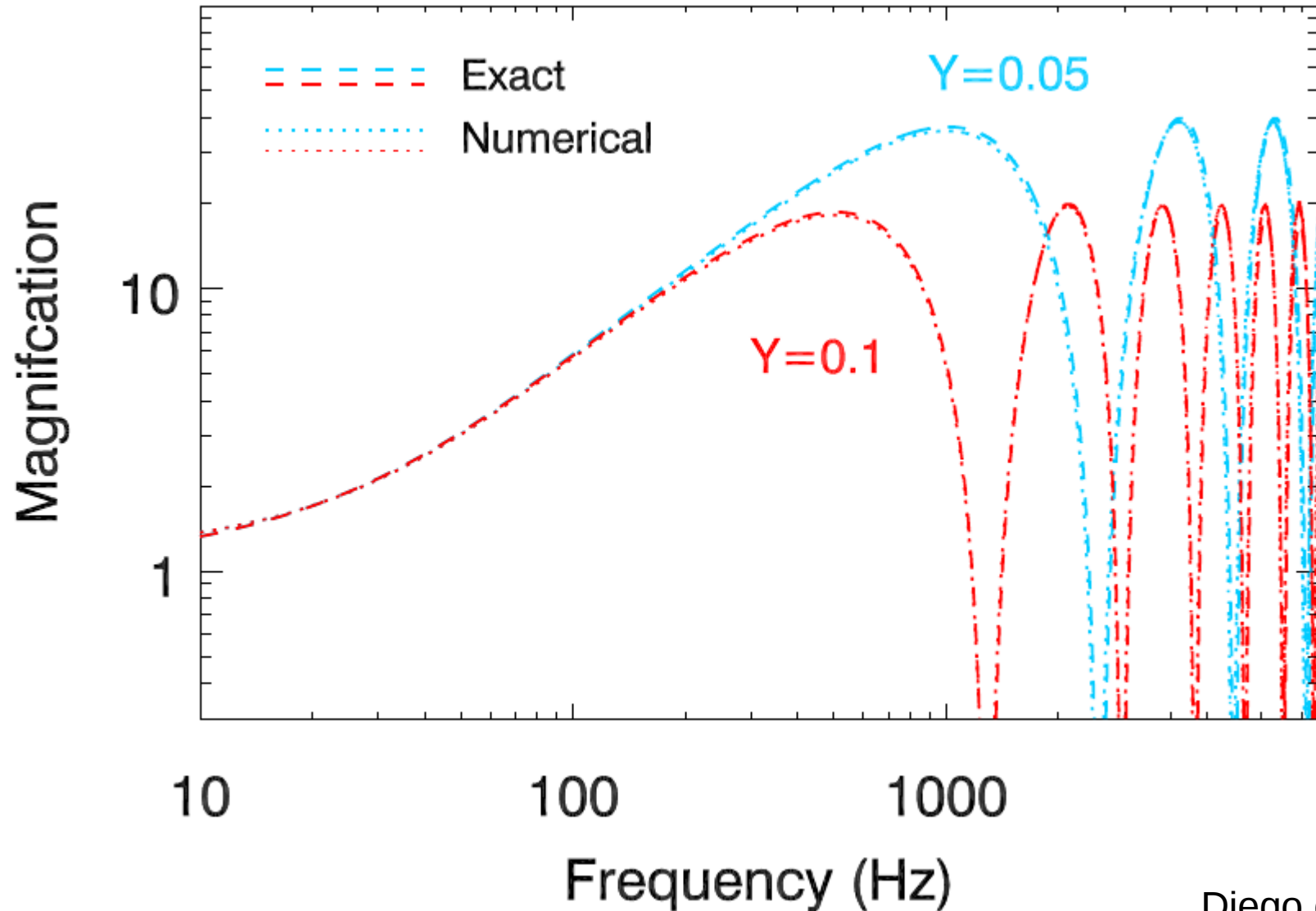
# If lensing is degenerate with the mass, how can this be tested?

**Micro-lensing of highly magnified GW is not only possible, is unavoidable.  
Then, interference effects should be observable at LIGO frequencies.**



# Diffraction integral

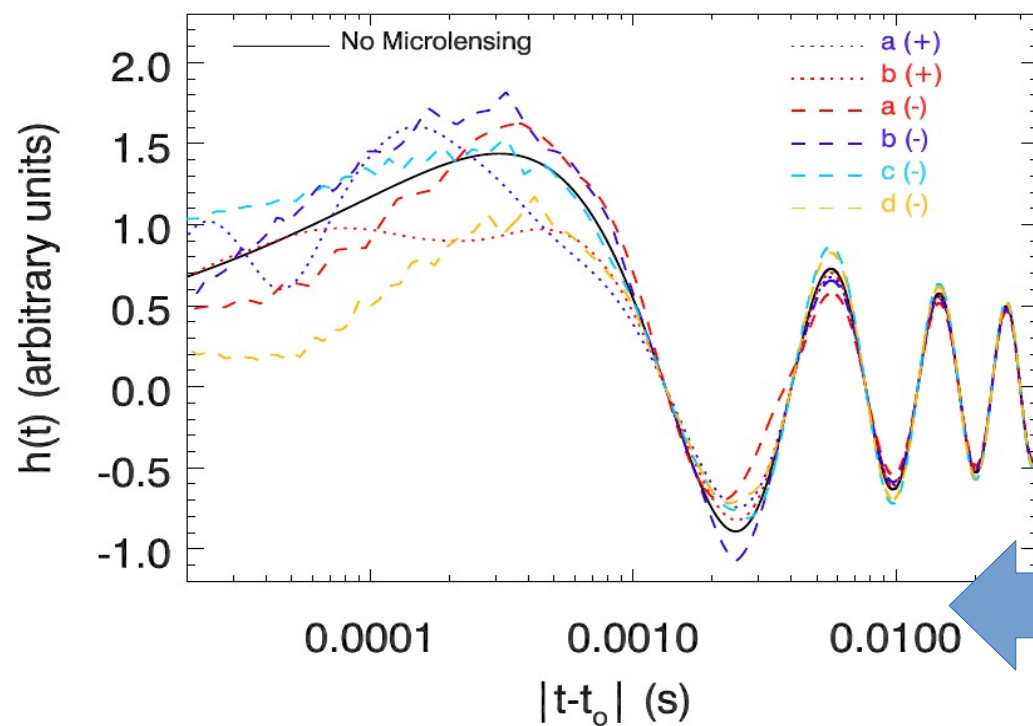
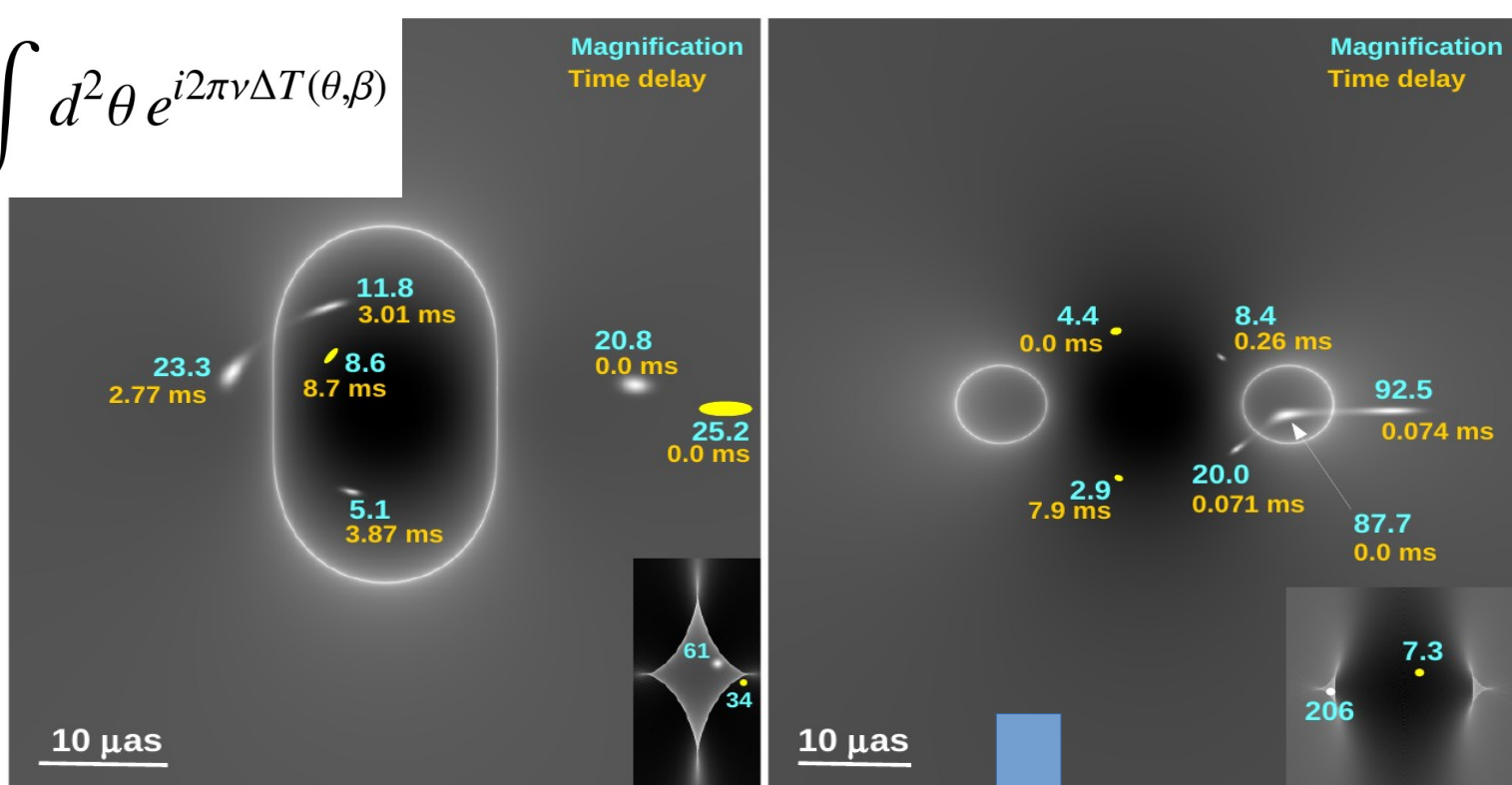
$$F(w, \beta) = A_o \frac{\nu}{2\pi i} \int d^2\theta e^{i2\pi\nu\Delta T(\theta, \beta)}$$



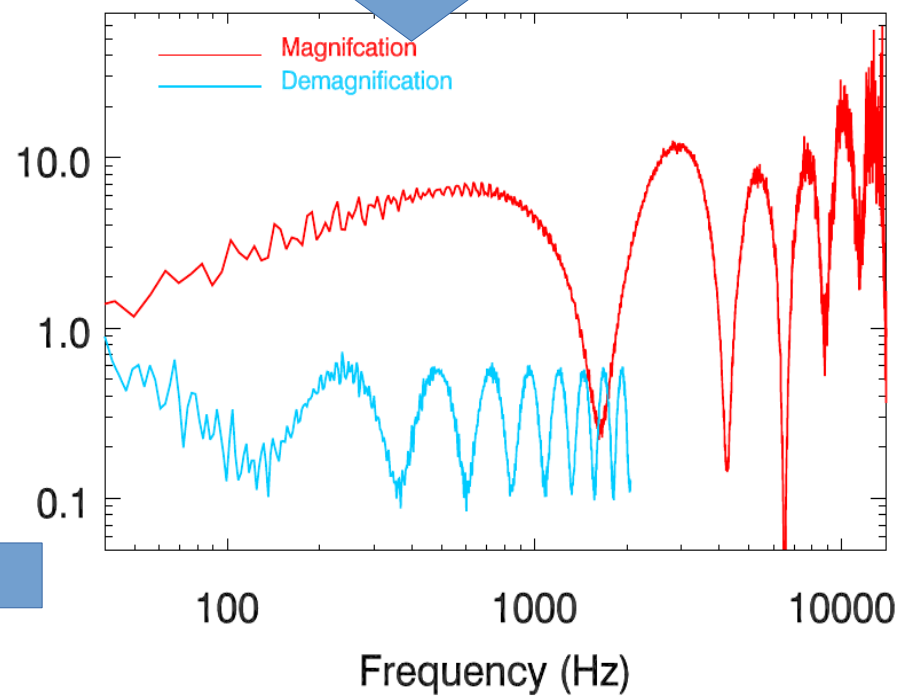
# Diffraction integral

$$F(w, \beta) = A_o \frac{\nu}{2\pi i} \int d^2\theta e^{i2\pi\nu\Delta T(\theta, \beta)}$$

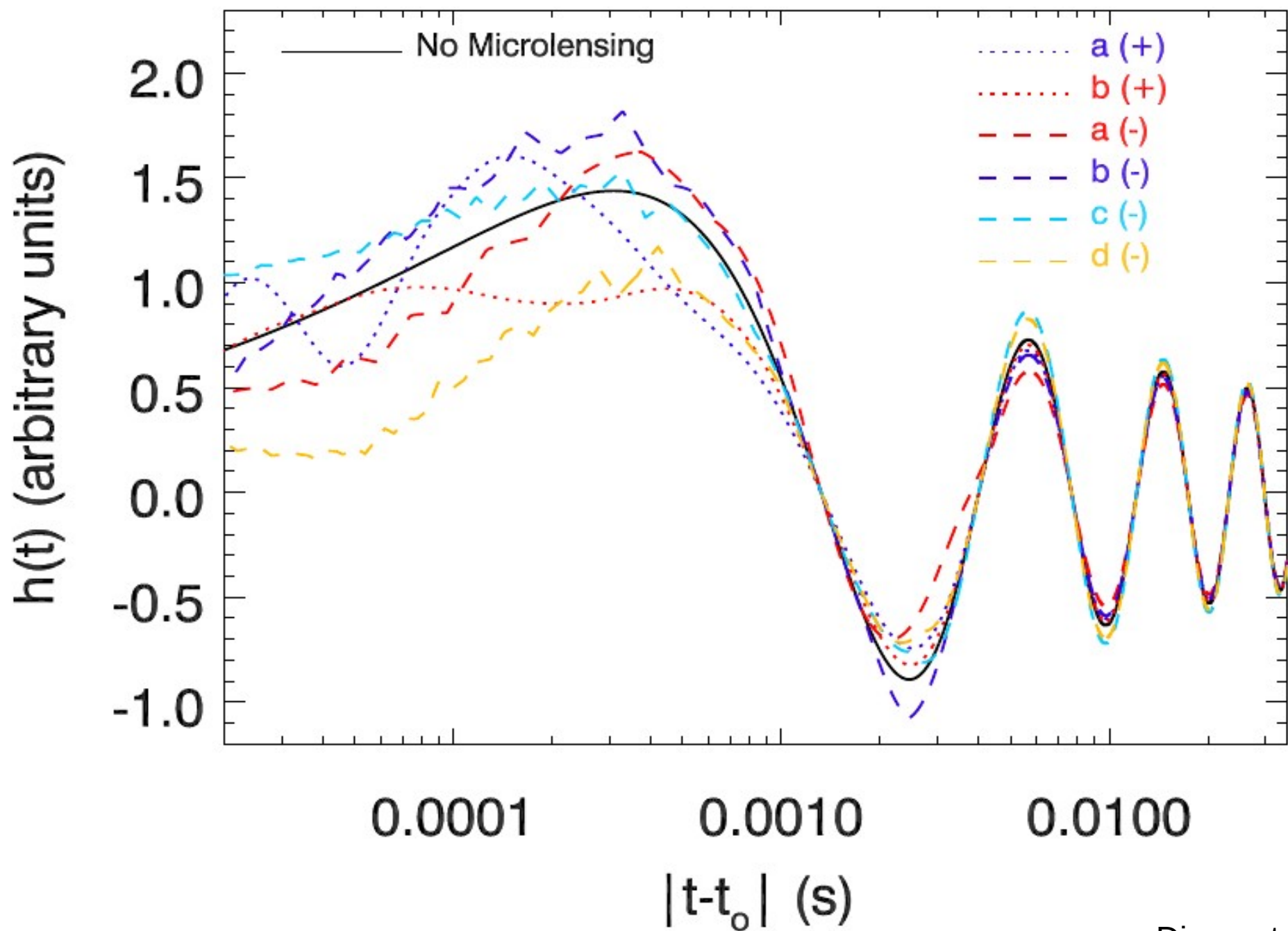
Diego et al. 2019



Relative Magnification

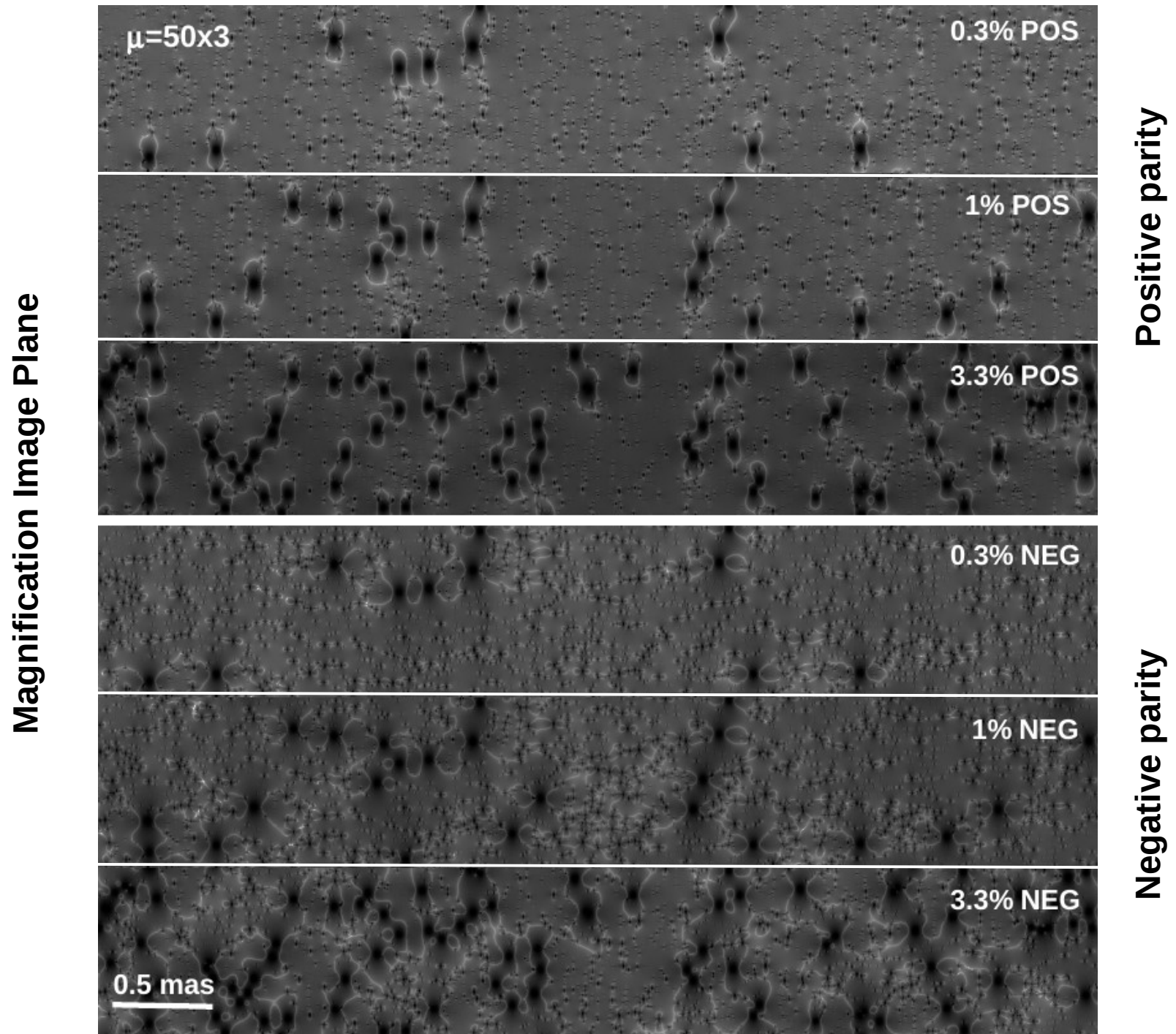


# Effects on the strain (from stellar/remnants microlenses)

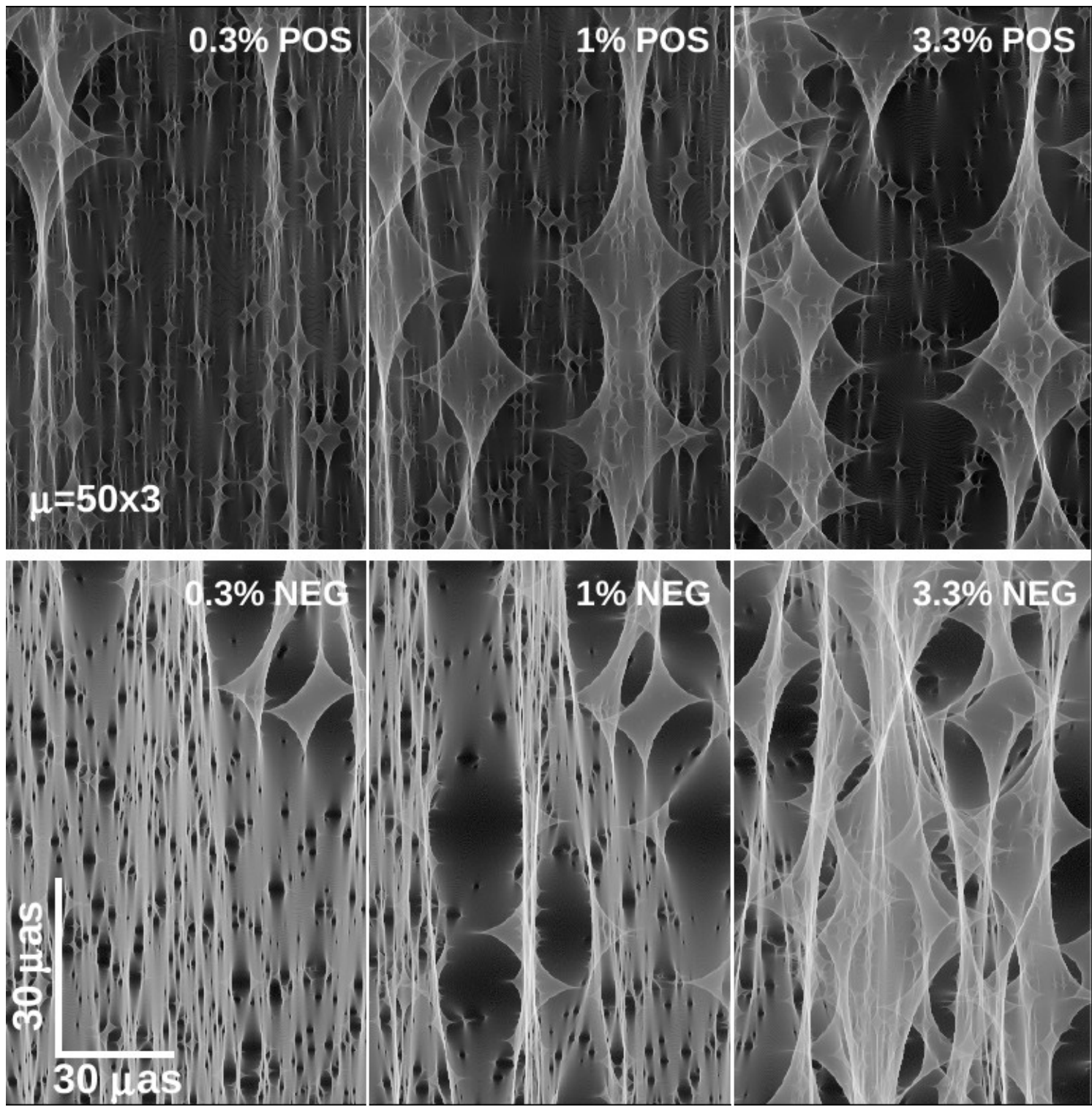




# Microlensing by 30 M<sub>⊙</sub> PBH near critical curves of galaxies and clusters



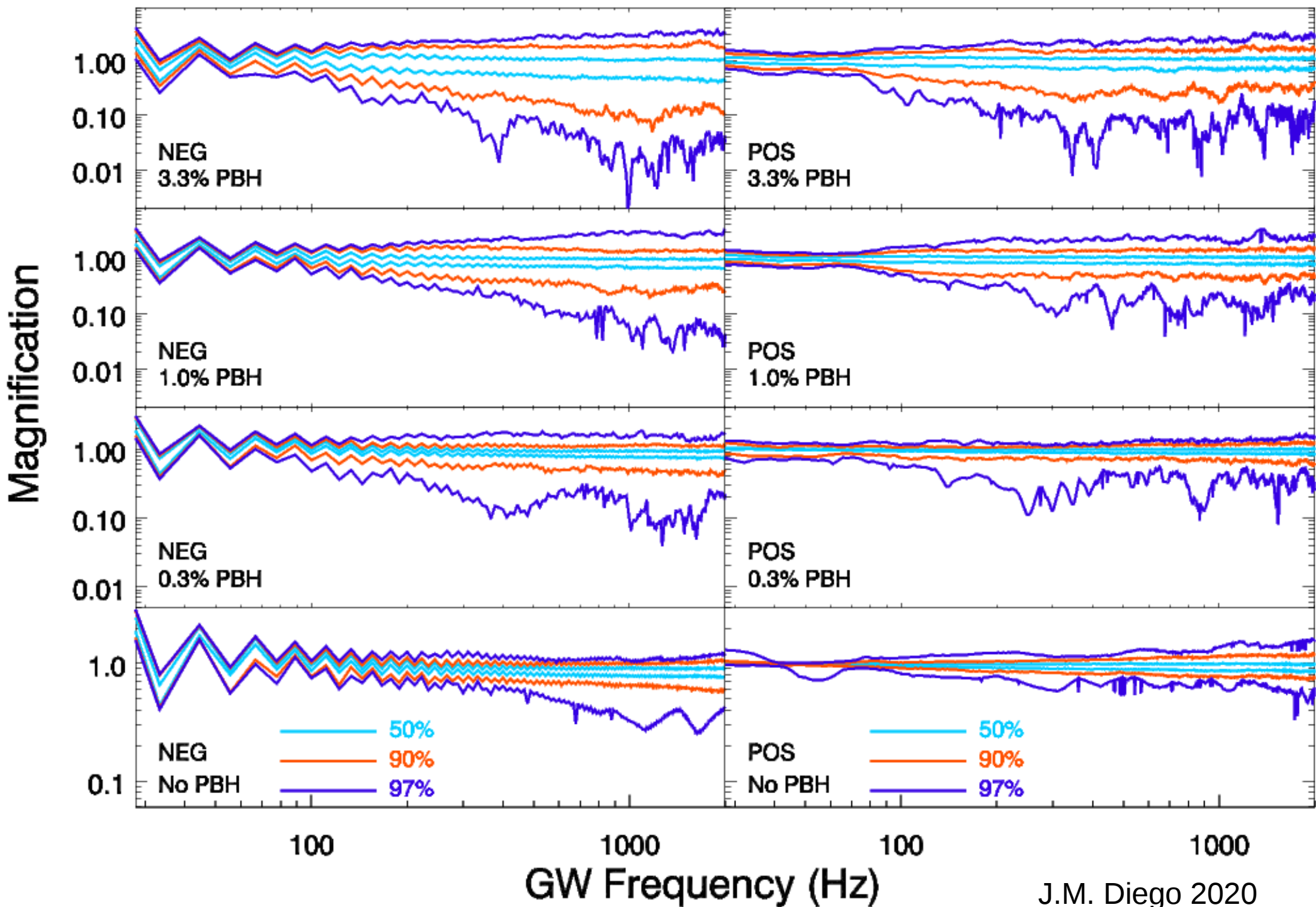
**Magnification Source Plane**



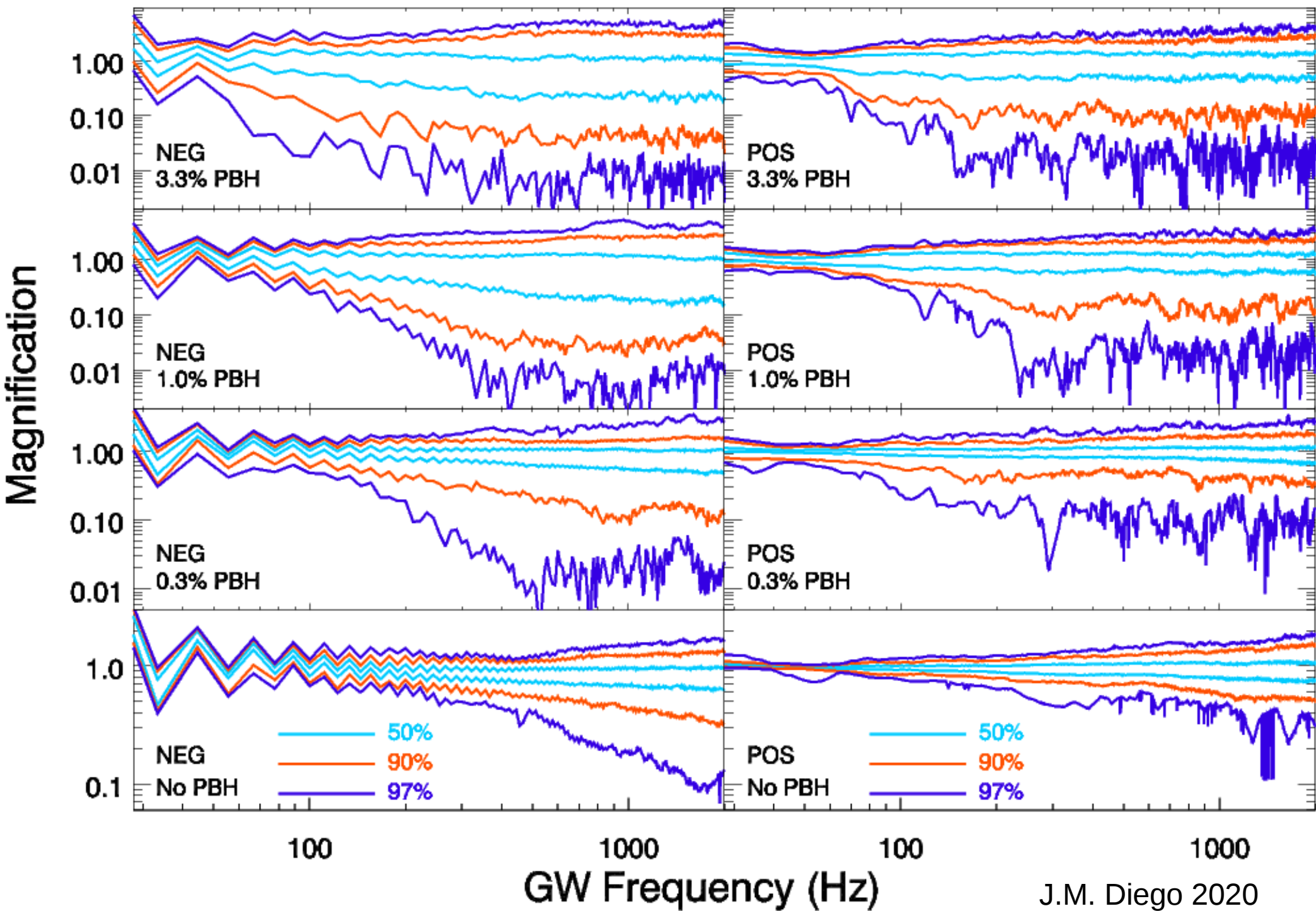
**Positive parity**

**Negative parity**

# PROBABILITY OF DISTORTION (macromodel magnification = 10x3)

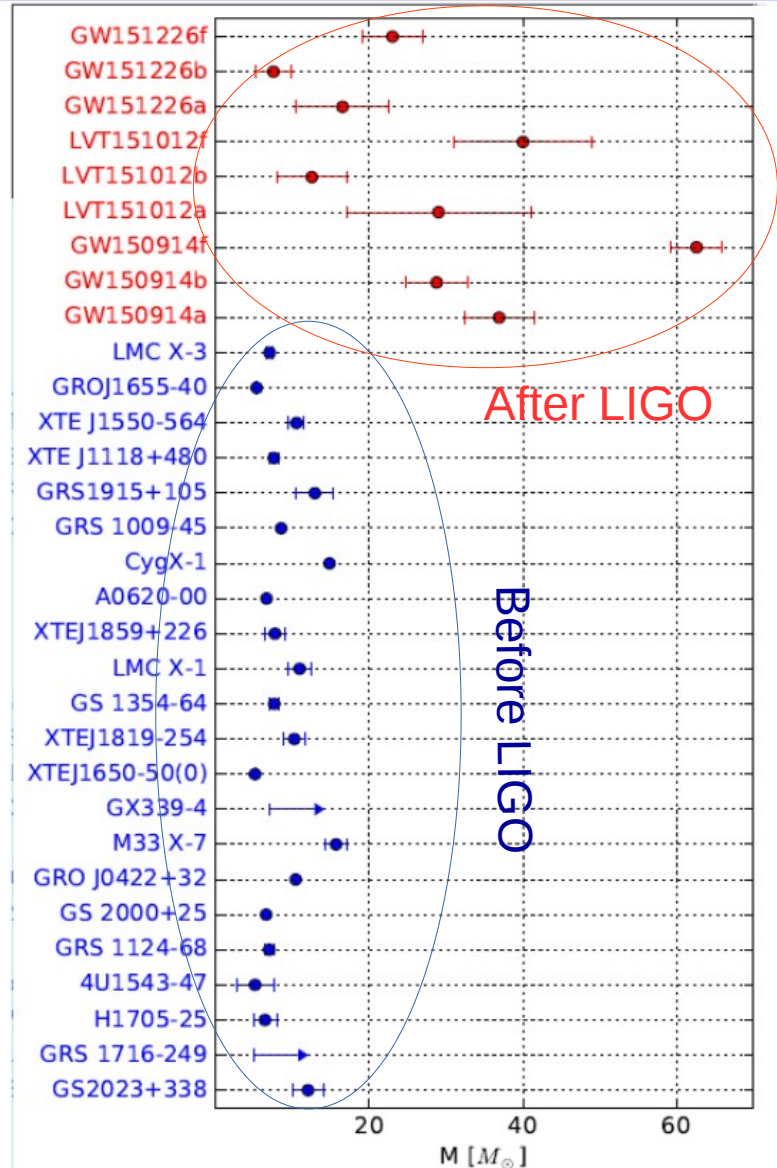
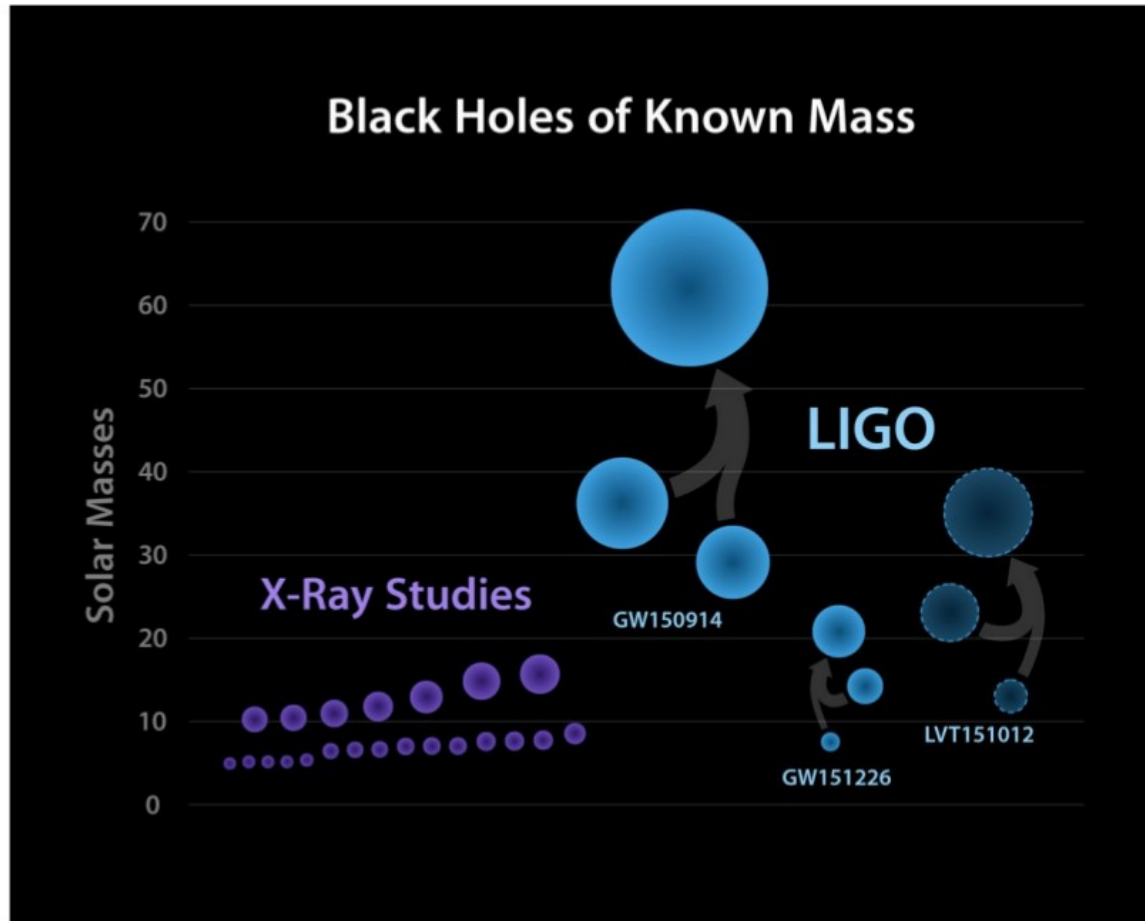


# PROBABILITY OF DISTORTION (macromodel magnification = 50x3)





# Is LIGO already seeing Lensed GWs?



Credit: Marie Anne Bizourad & LIGO collaboration

# Is LIGO already seeing Lensed GWs?

Observed

$$M = M_c(1+z)$$

Inferred

$$h(t) \sim \text{sqrt}(\mu) (M^{5/6}/D(z)) F(t, M, \theta)$$

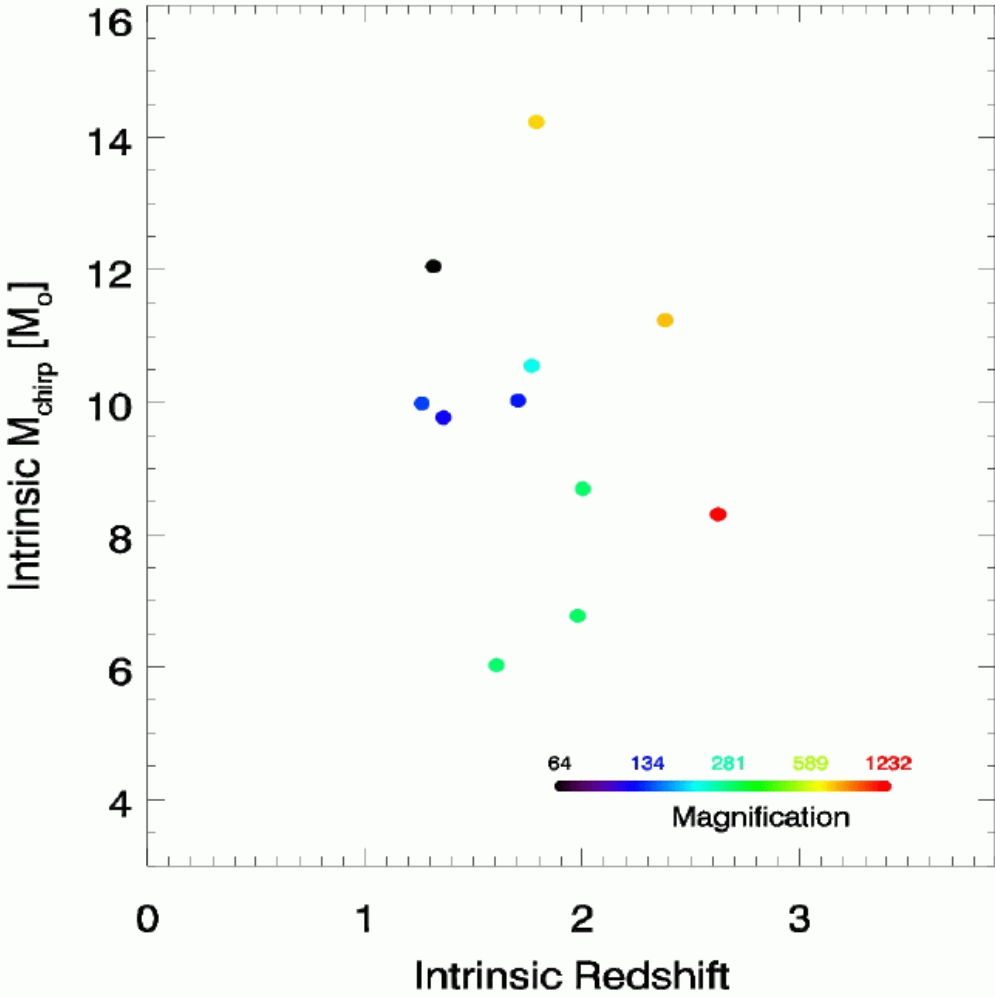
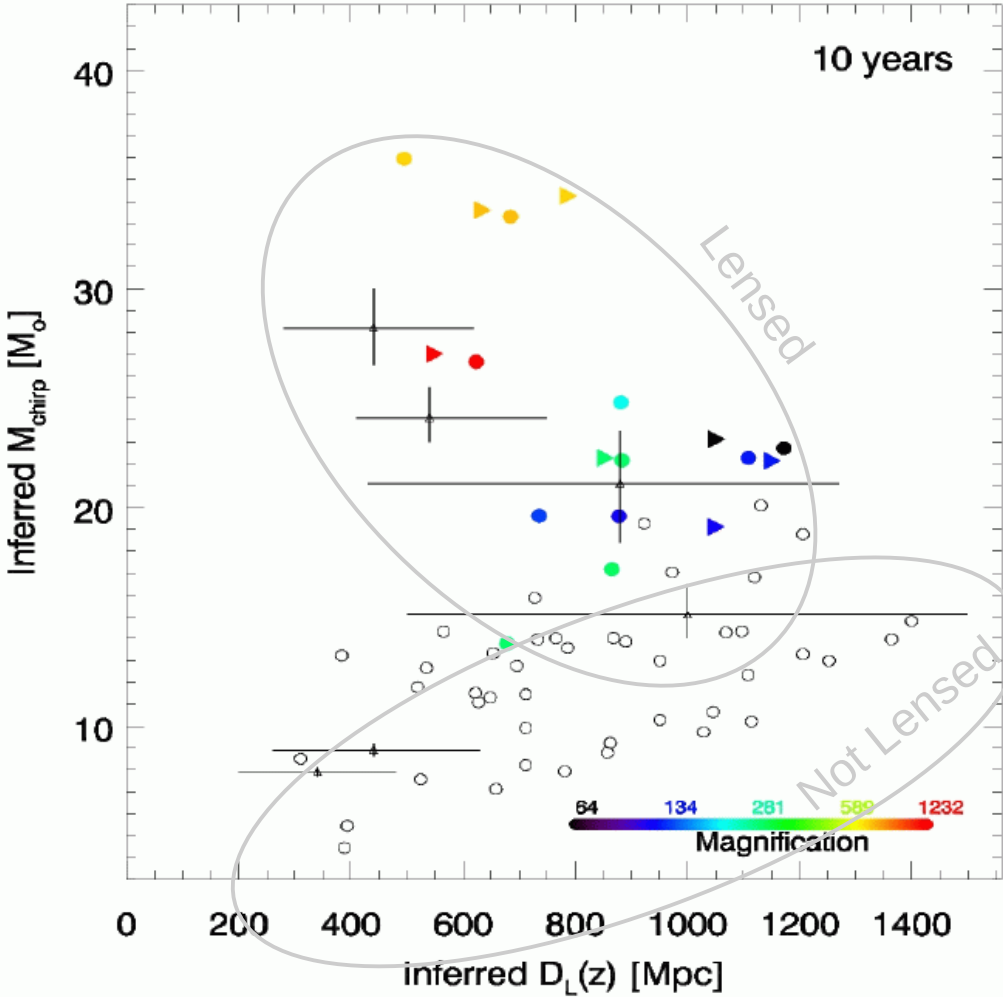
$$D(z_{\text{est}}) = D(z_{\text{true}}) / \text{sqrt}(\mu)$$

**IF** an event at high  $z$  is magnified by a large factor,  $\mu$ , then if lensing is ignored, it will appear as a much closer event with a larger mass.

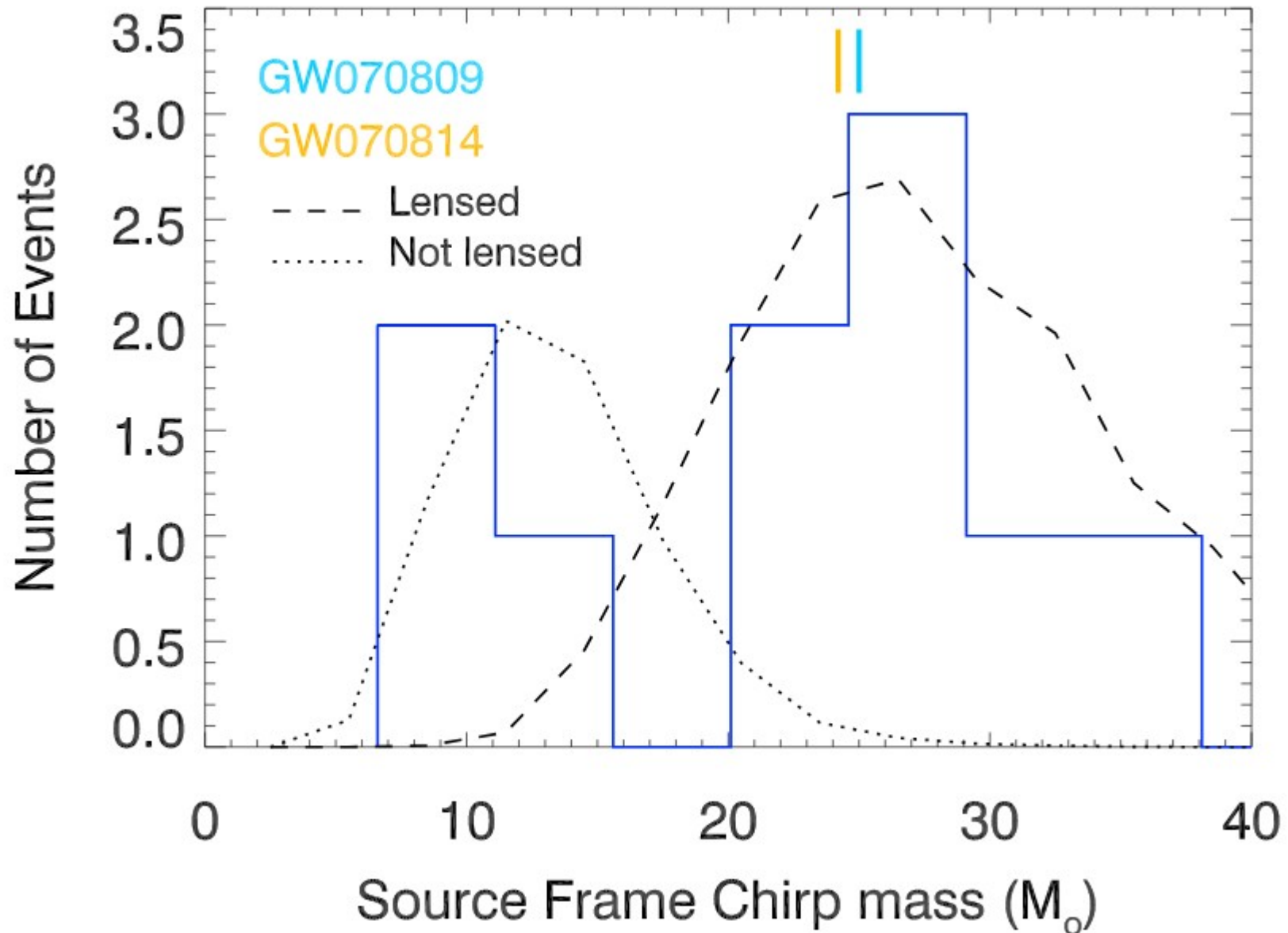
Then, **IF** the probability of lensing is reasonable, some of the LIGO events may be actually **distant** lensed events with **smaller masses**

Unlike other events (SNe, GRB, etc) all sky is observed at once. The only limitations are dictated by the geometric factor,  $\theta$ .

# LENSING INTERPRETATION OF LIGO DETECTIONS



# Lensing predicts also a bimodal mass function





# Is LIGO already seeing Lensed GWs?

DRAFT VERSION 14 MAY 2021

Typeset using L<sup>A</sup>T<sub>E</sub>X twocolumn style in AASTeX62

Search for lensing signatures in the gravitational-wave observations from the first half of LIGO-Virgo's third observing run

THE LIGO SCIENTIFIC COLLABORATION AND THE VIRGO COLLABORATION

(Dated: 13 May 2021)

## ABSTRACT

We search for signatures of gravitational lensing in the gravitational-wave signals from compact binary coalescences detected by Advanced LIGO and Advanced Virgo during O3a, the first half of their third observing run. We study: 1) the expected rate of lensing at current detector sensitivity and the implications of a non-observation

# Is LIGO already seeing Lensed GWs?

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Typeset using L<sup>A</sup>T<sub>E</sub>X twocolumn style in AASTeX62

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## Evidence for lensing of gravitational waves from LIGO-Virgo

J.M. Diego\*

*Instituto de Física de Cantabria (CSIC-UC) Edificio Juan Jordá. Avda Los Castros s/n. 39005 Santander, Spain.*

T. Broadhurst

*Department of Theoretical Physics, University of the Basque Country UPV-EHU, 48040 Bilbao, Spain.  
Donostia International Physics Center (DIPC), 20018 Donostia, The Basque Country, Spain.  
IKERBASQUE, Basque Foundation for Science, Alameda Urquijo, 36-5 48008 Bilbao, Spain.*

G. Smoot

*IAS TT & WF Chao Foundation Professor, IAS,  
Hong Kong University of Science and Technology,  
Clear Water Bay, Kowloon, 999077 Hong Kong, China.  
Paris Centre for Cosmological Physics, Université de Paris, emertius,  
CNRS, Astroparticule et Cosmologie, F-75013 Paris, France A,  
10 rue Alice Domon et Leonie Duquet, 75205 Paris CEDEX 13, France.  
Donostia International Physics Center (DIPC), 20018 Donostia, The Basque Country, Spain.  
Physics Department and Lawrence Berkeley National Laboratory,  
University of California, emeritus Berkeley, 94720 CA, USA.*

(Dated: June 8, 2021)

Recently, the LIGO-Virgo Collaboration (LVC) concluded that there is no evidence for lensed gravitational waves (GW) in the first half of the O3 run [1], claiming “We find the observation

# CONCLUSIONS

PBH are a candidate for DM which become popular after LIGO detected a relatively abundant of BH with  $>20 M_{\odot}$

LIGO  $\rightarrow$  IF the rate of events at  $z \sim 2$  is in the range of  $10^4$ , the low frequency events observed by LIGO are (likely) gravitationally lensed WG at  $z > 1$  with BH masses  $\sim 10 M_{\text{sun}}$ .

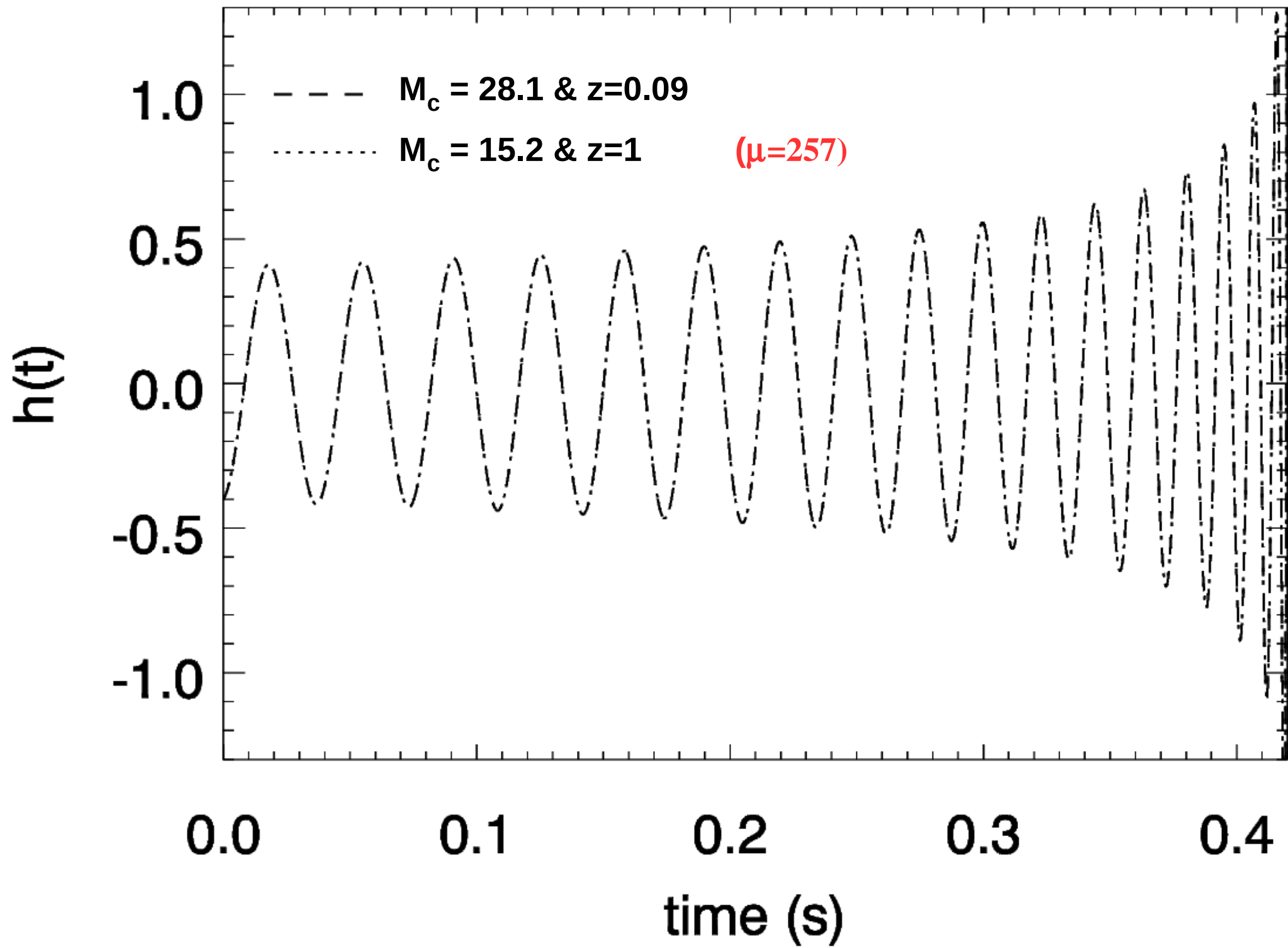
Lensing at high magnification should be affected by microlensing and interference (pattern needs to be incorporated in templates)

Microlensing can set limits on the abundance of BH (including PBH)

Images with negative parity should show interference signs more often

LIGO may be already observing strongly lensed GWs. Detailed analyses of their strains may reveal microlensing signatures from intervening compact dark matter structures.

# **Extra Slides**



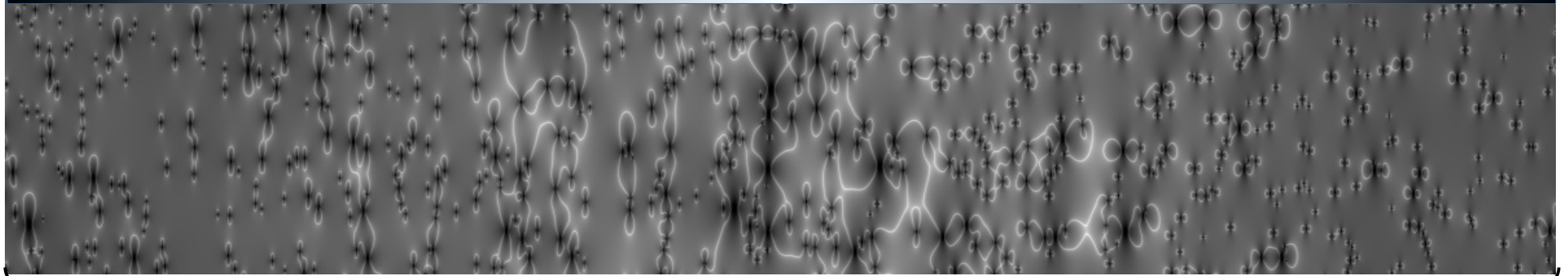


# Microlensing at extreme macromodel magnification

Image Plane

Images with  
Negative parity

Images with  
Positive parity

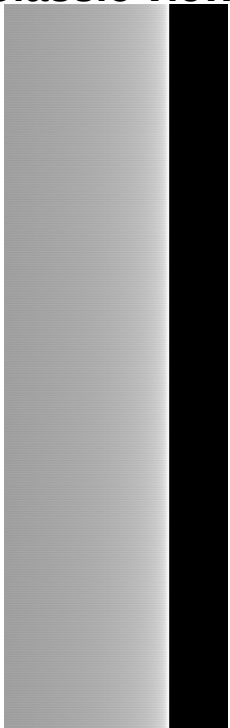


Classic view

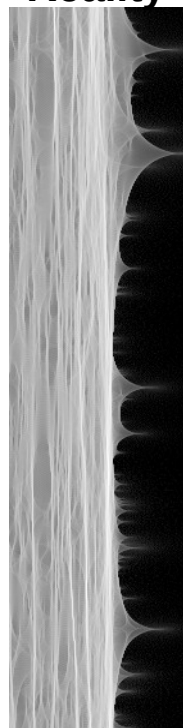
Reality

vs

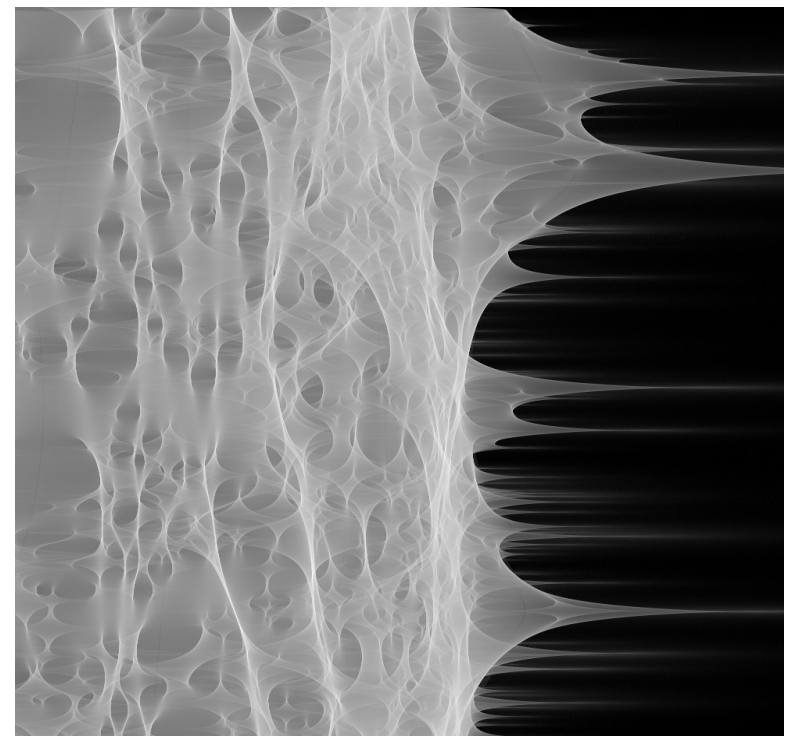
Source Plane  
Smooth model



Microlens model



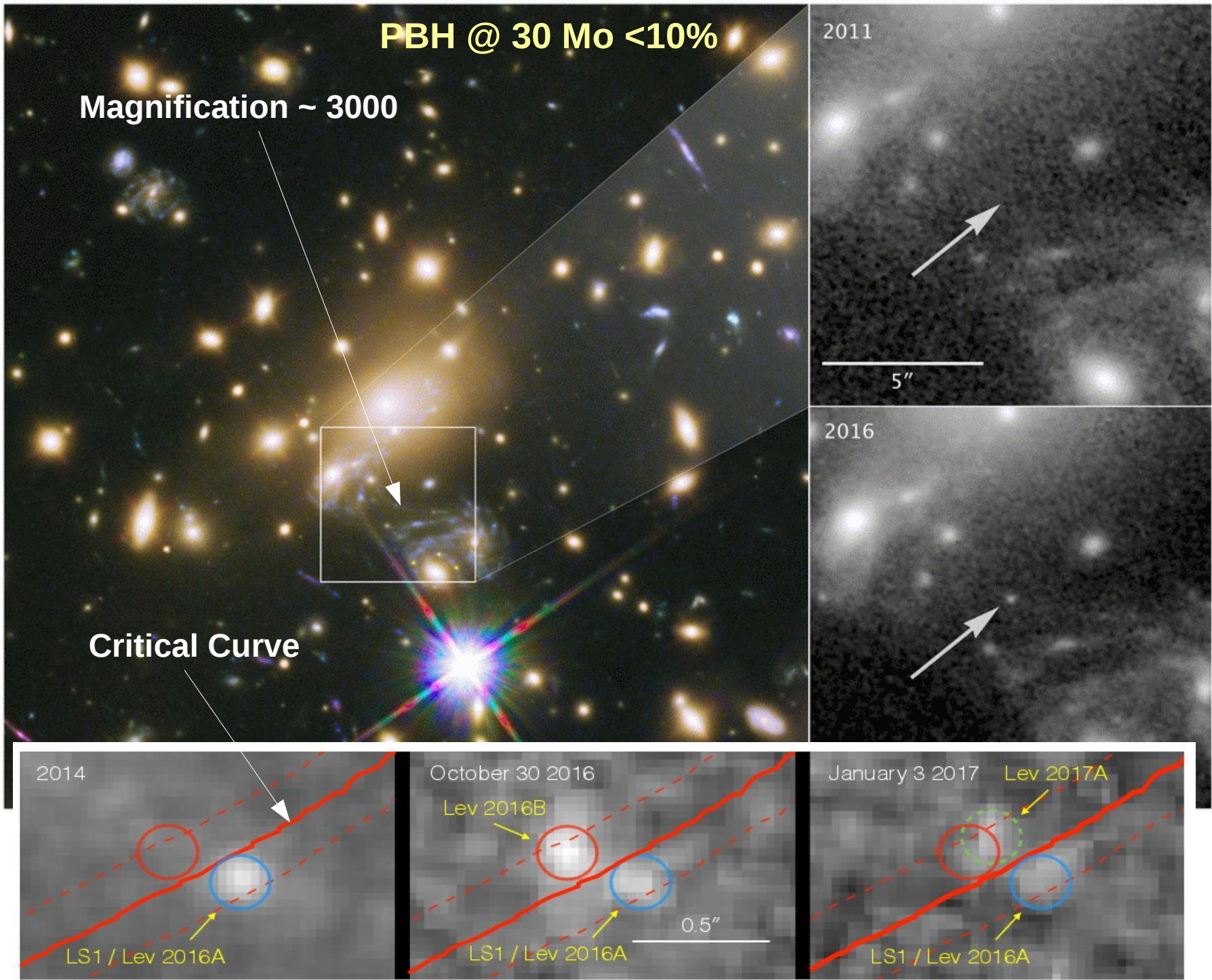
x10



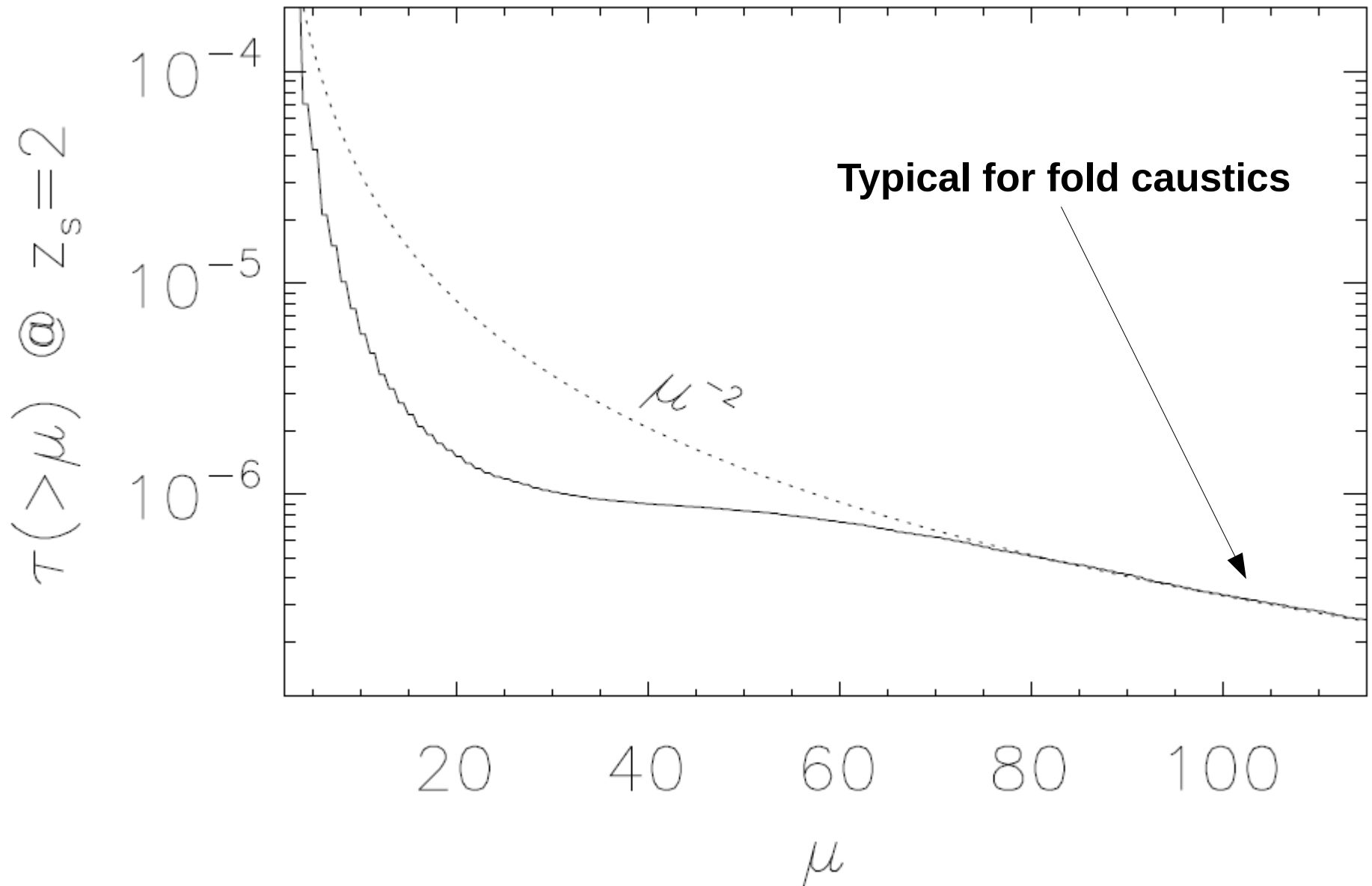
More microlenses → More distortion

# The Icarus Event

P. Kelly, J.M. Diego et al 2018, Nature Ast. 2, 334-342  
Diego, J.M., Kaiser, N. et al. 2018, Apj, 857, 25



# Net probability by all halos & at all redshifts for a source at $z=2$





# A back of the envelope calculation

Probability of having magnification larger than 100 :  $\sim 3E-7$

Volume between  $z=1.9$  and  $2.1$  :  $\sim 100 \text{ Gpc}^3$

Rate of events at  $z=2$  :  $\sim 3E4 /(\text{yr Gpc}^3)$   
Compare with  $\sim 10^6$  per  
yr &  $\text{Gpc}^3$  for SNe



Total Number of events between  $z=1.9$  and  $2.1$  :  $3E6$  per year

Total Number of  $\mu > 100$  events between  $z=1.9$  and  $2.1$  :  $\sim \mathbf{1}$  per year

**Rate needs to be of order  $10^4$  for lensing hypothesis to work**

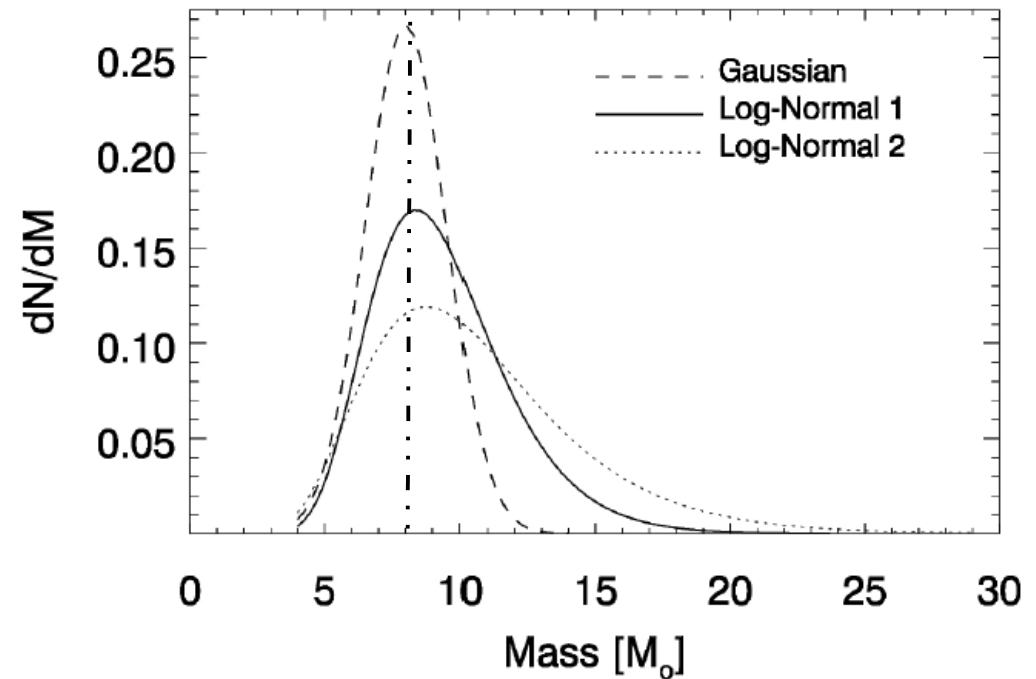
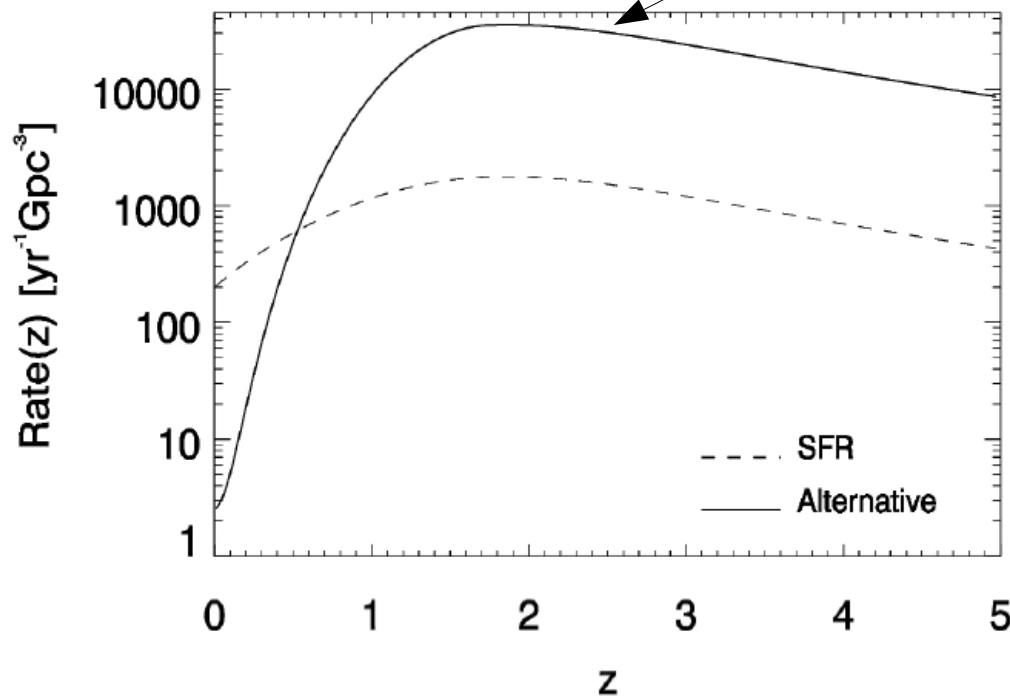
**We do not know what the actual rate is !**

# Model elements: Rates and BBH mass function

Basic assumption is that the rate of events at high- $z$  is high to compensate the small probability for lensing

Mass function is assumed to be “natural”, that is, consistent with observational constraints from our Galaxy

>1 order of magnitude smaller than SNe rate

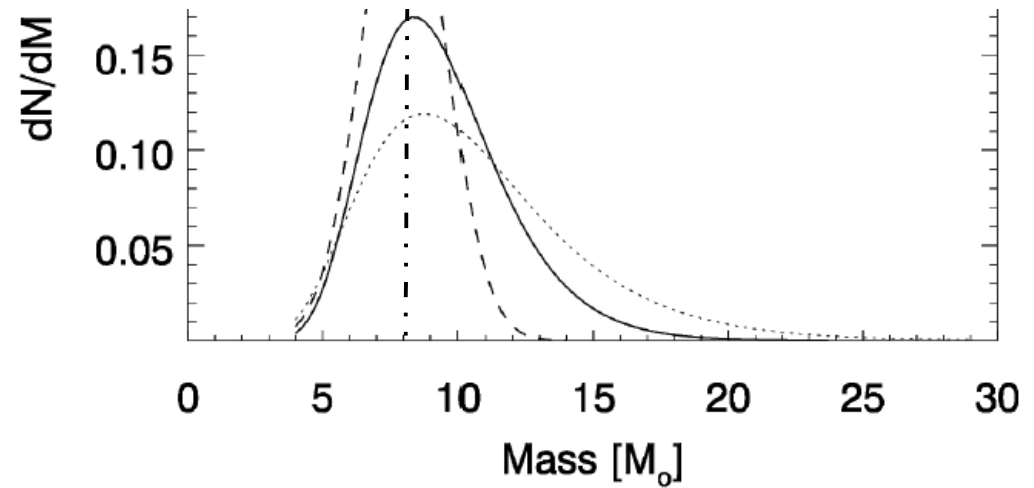
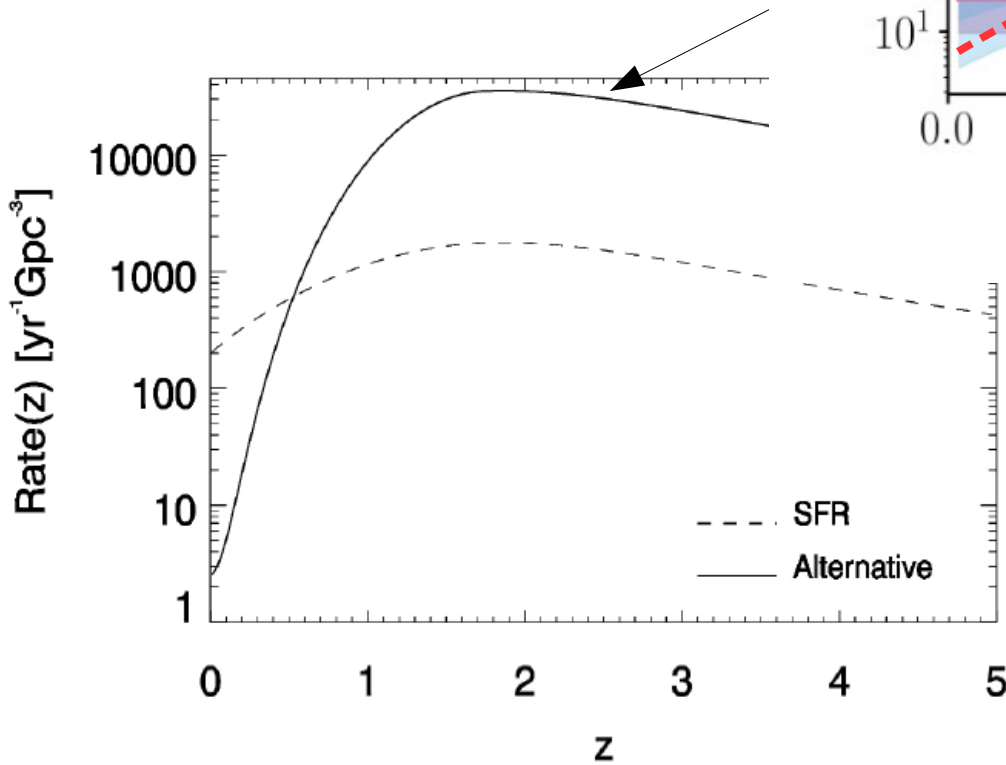
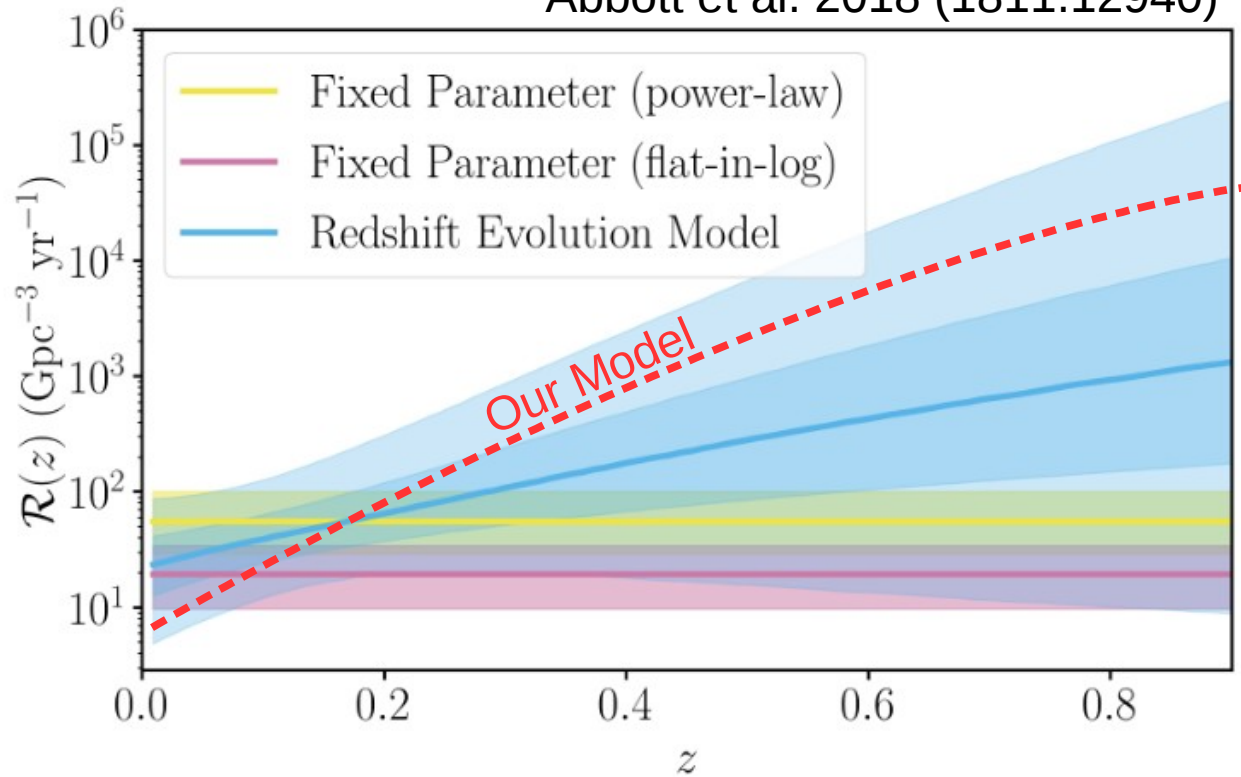




# Model elements:

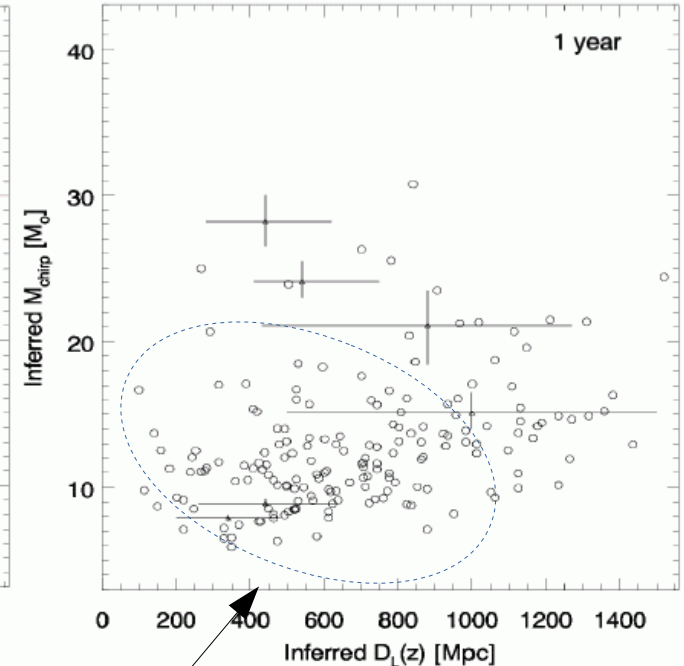
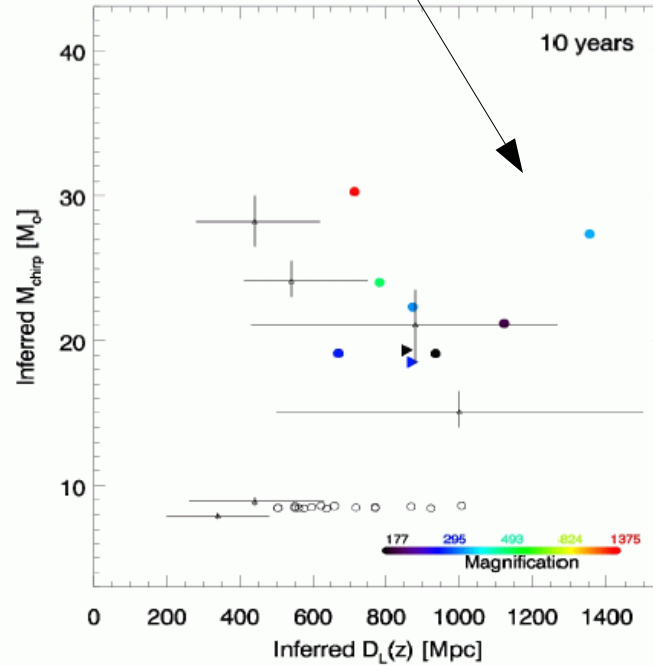
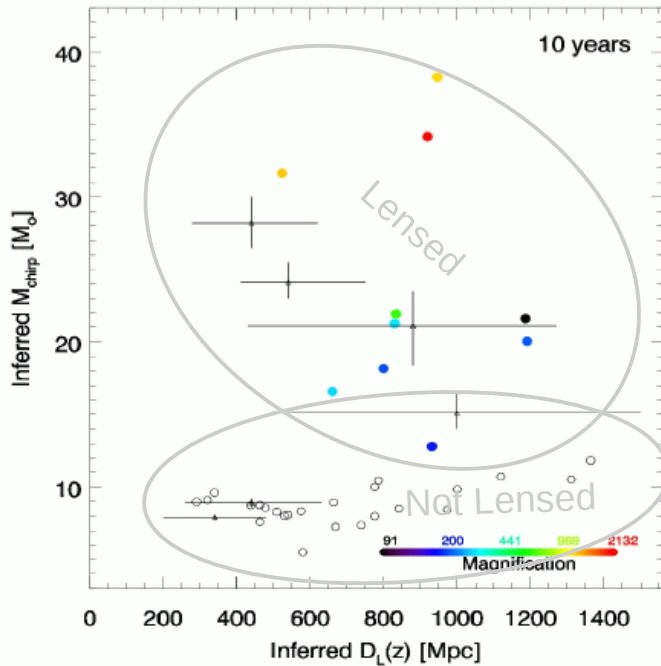
Basic assumption is that the rate compensates the small probability

Mass function is assumed to be observational constrains from c



## Strong Evolution + Monochromatic MF

A simple monochromatic mass function already does a decent job at reproducing the data



## Strong Evolution + Gauss MF

A Gaussian mass function goes in the right direction

## Modest Evolution + Broad MF

Many events should have been detected by LIGO in this regime. Where are they?

