## Extra-exercise of Tepic 6

A population of potential consumers is uniformly distributed with density 1 along a segment of length L Two firms compete to sell a product that is homogeneous except for the location of the firm. Firm 1 is located at a distance of *a* from the left end of the segment and firm 2 at a distance of *a* from the right end of the segment. The utility that a consumer *j* obtains buying the product at firm *i* is given by  $U_{ji}=r-p_i-tx_{ij}$ , where  $p_i$  is the price set by firm i,  $x_{ij}$  is the distance along the segment between the location of consumer *j* and the location of firm *i*, and *t* is the transport cost per unit of distance.

- a. Obtain the demand for each one of the firms
- b. Calculate the own-price elasticity of demand of firm 1. How does this elasticity change when the transport cost changes?
- c. Suppose that the unit cost of production is identical for both firms and equal to *c*. Obtain the reaction functions for firms 1 and 2.
- d. Obtain the Nash equilibrium in prices.