



# Frequency shifters

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Università di Trento

# NanoScience Lab, U of Trento (I)



2 full professors (Lorenzo Pavesi, Marina Scarpa)

1 assistant professor (Zeno Gaburro)

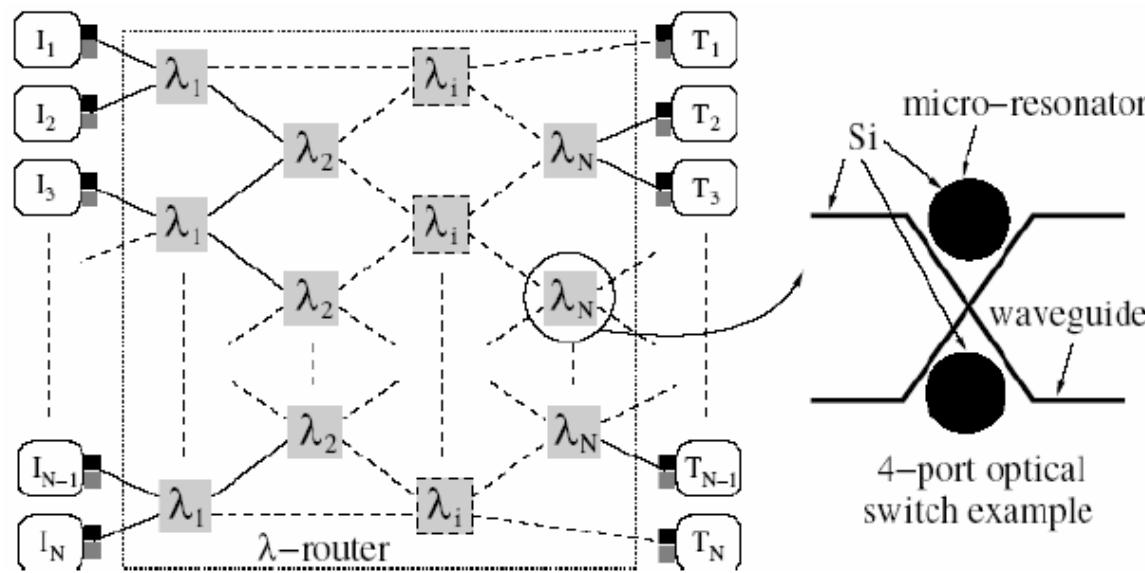
5 postdocs

5 phd students

4 master students

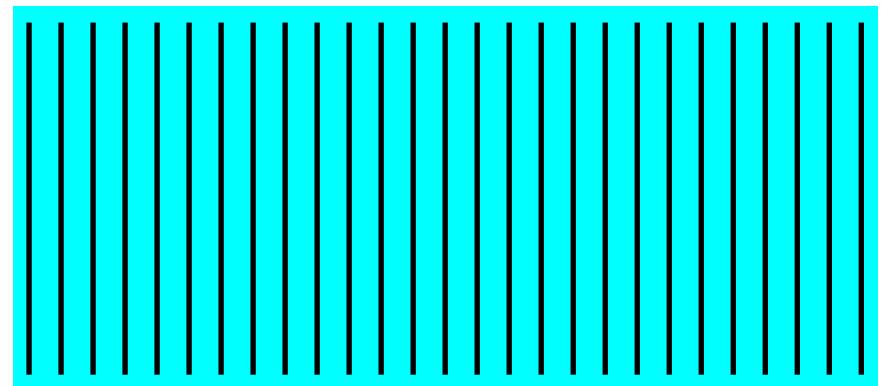
Motivation:

Considering **experimental** activity in **optics**  
**(non-BEC)** related to this workshop



*WADIMOS Project (7th EU FP)*  
*ICT = Information and Communication Technologies*  
*Wavelength Division Multiplexed Photonic Layer on CMOS*

# Time refraction



$$k_2 = k_1 n_2/n_1; \quad \omega_2 = \omega_1$$

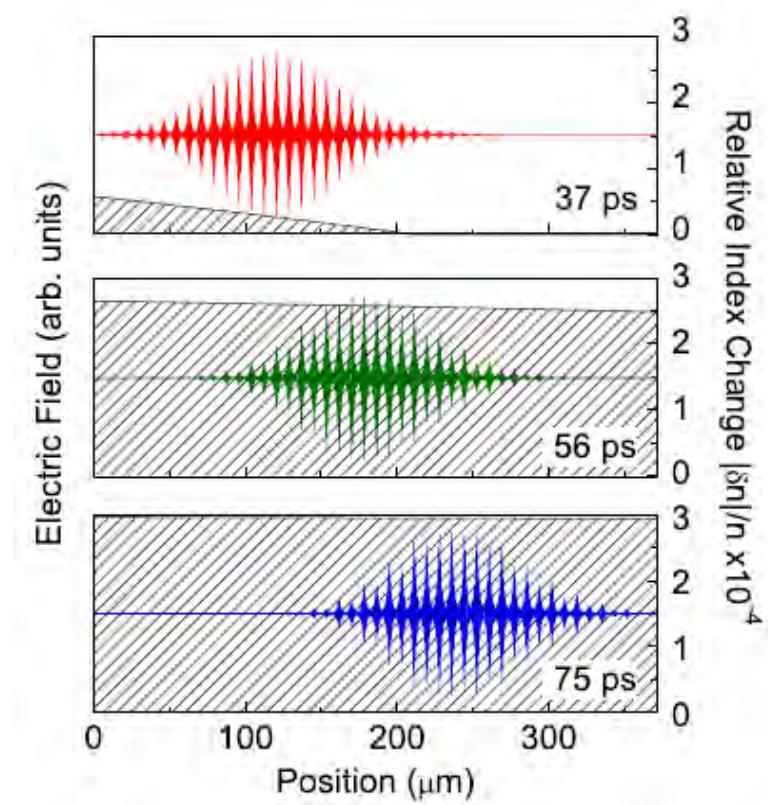
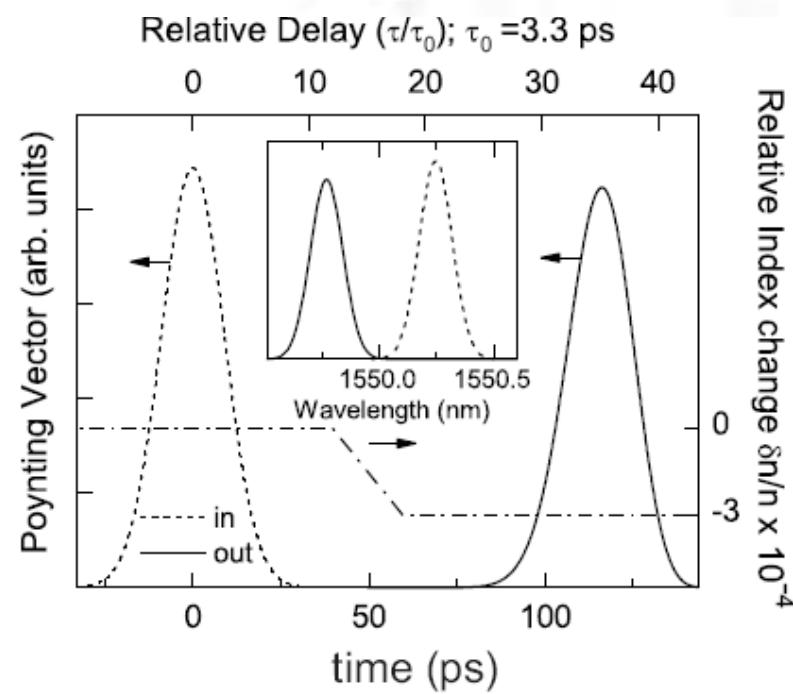
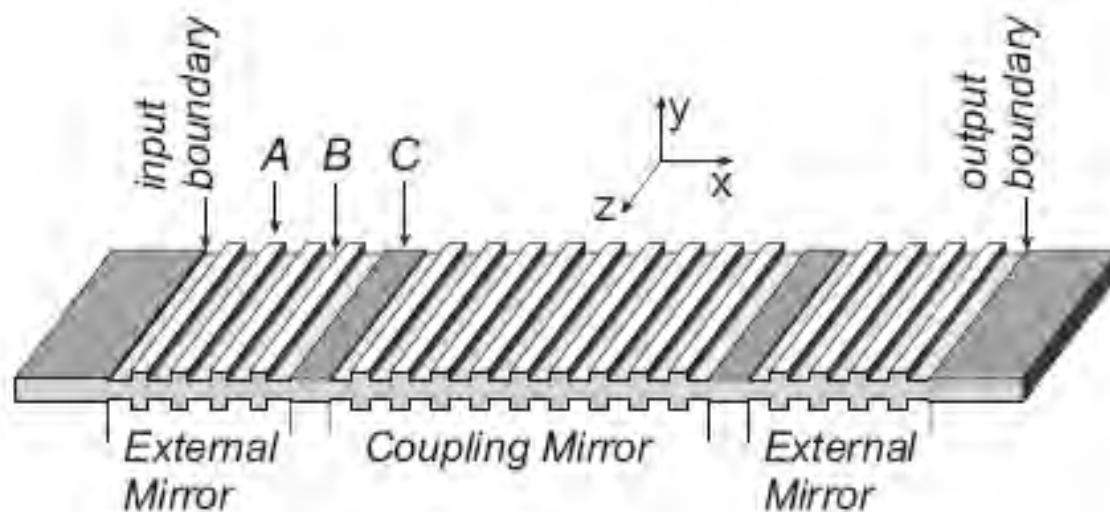
$$k_2 = k_1; \quad \omega_2 = \omega_1 n_1/n_2$$

Morgenthaler, *IEEE Trans. Microw. Theory Tech.* 6, 167-172 (1958)

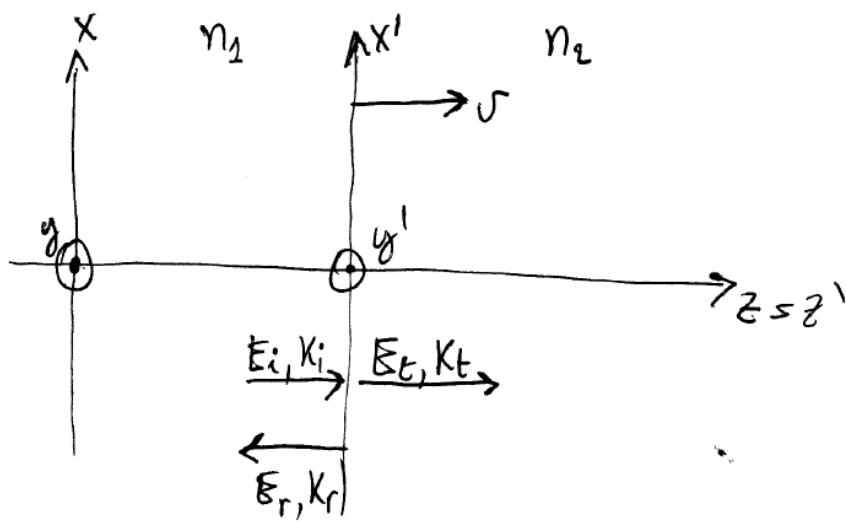
Wilks *et al.*, *Phys. Rev. Lett.* 61, 337-340 (1988)

Segev *et al.*, *Phys. Lett. A* 370, 202-206 (2007)

Biancalana *et al.*, *Phys. Rev. E* 75, 046607 (2007)



Z. Gaburro *et al.*, Optics Express (2006)



$$\omega_i = \gamma [\omega_i + \beta c K_i] = \omega_i' [1 + \beta n_1]$$

$$\omega_r = \omega_i' [1 - \beta n_1]$$

$$\omega_t = \omega_i' [1 + \beta n_2]$$

$$K_i = \frac{\omega}{c} \gamma [n_1 + \beta]$$

$$K_r = -\frac{\omega}{c} \gamma [n_1 - \beta]$$

$$K_t = \frac{\omega}{c} \gamma [n_2 + \beta]$$

$$\boxed{\omega_r = \omega_i \frac{1 - \beta n_1}{1 + \beta n_1}}$$

$$\boxed{\omega_t = \omega_i \frac{1 + \beta n_2}{1 + \beta n_1}}$$

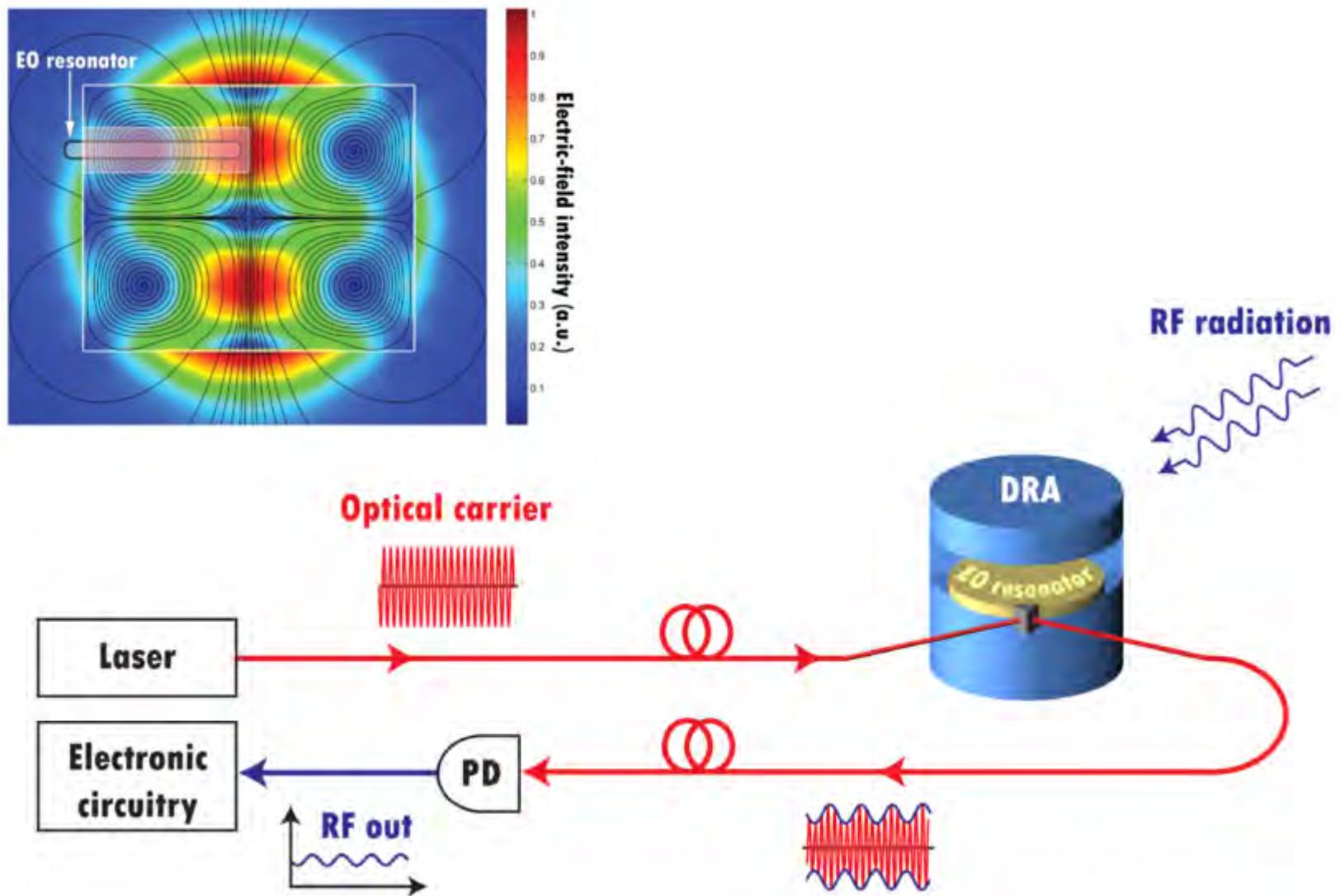
$$\beta = \frac{v}{c}$$

$$\gamma = \frac{1}{\sqrt{1 - \beta^2}}$$

$$\omega_r = \omega_i \frac{1 - \beta n_1}{1 + \beta n_1},$$

$$\omega_t = \omega_i \frac{1 - \beta n_1}{1 - \beta n_2}$$

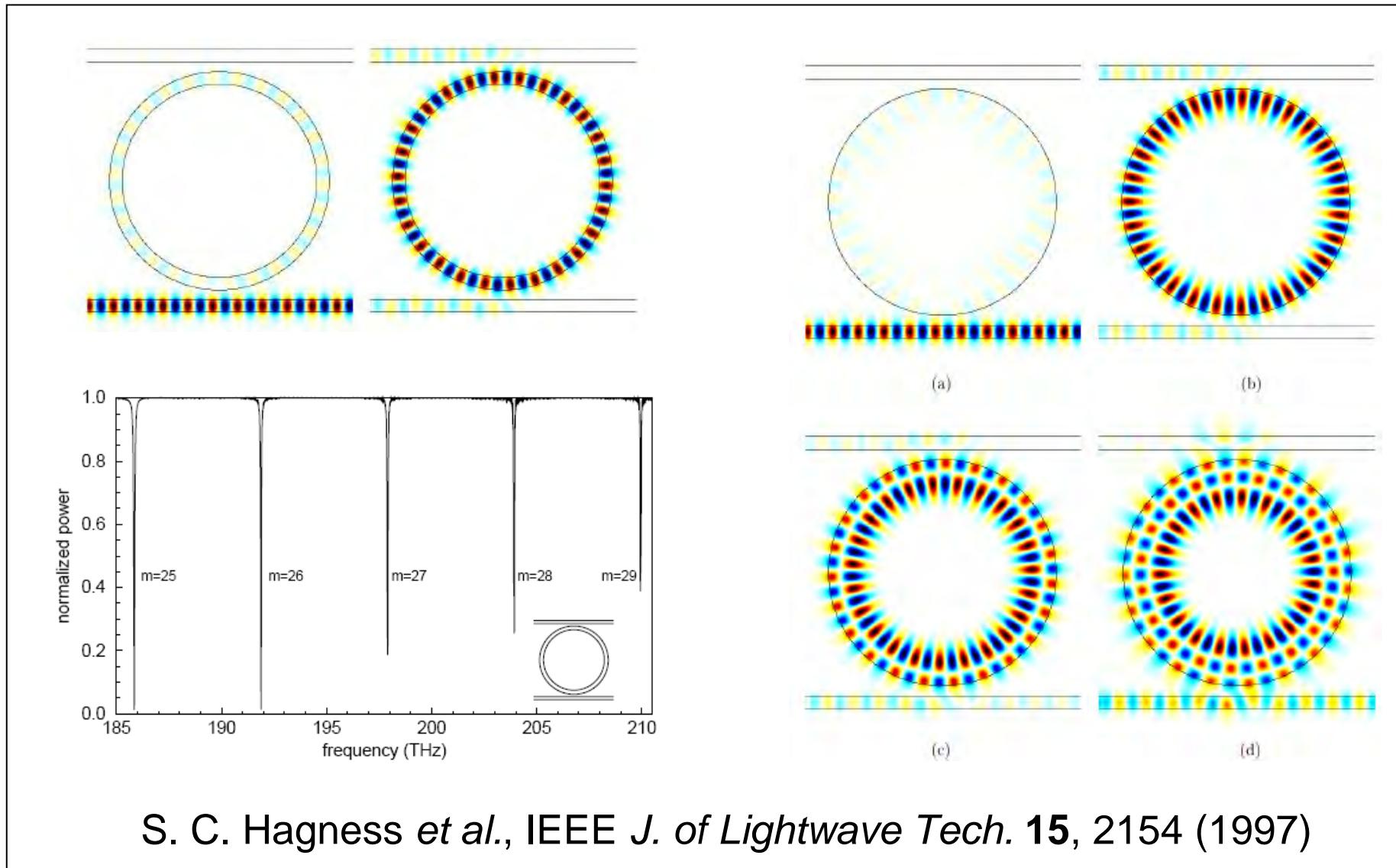
**With still dielectric**

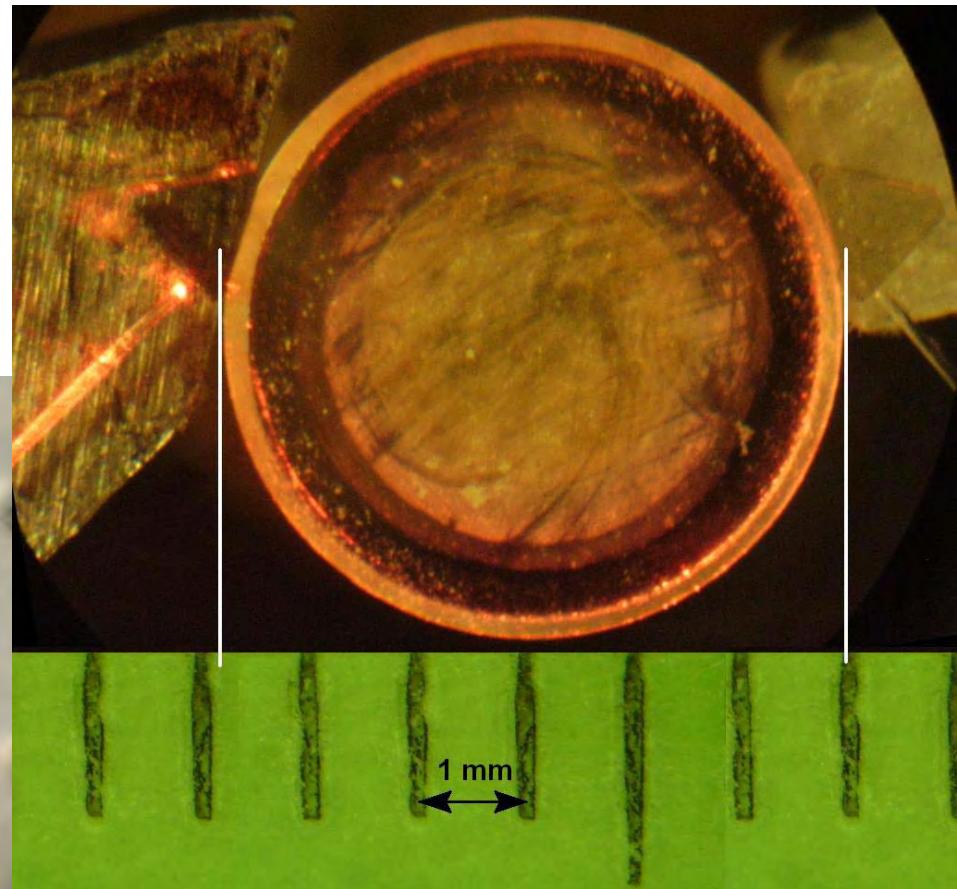
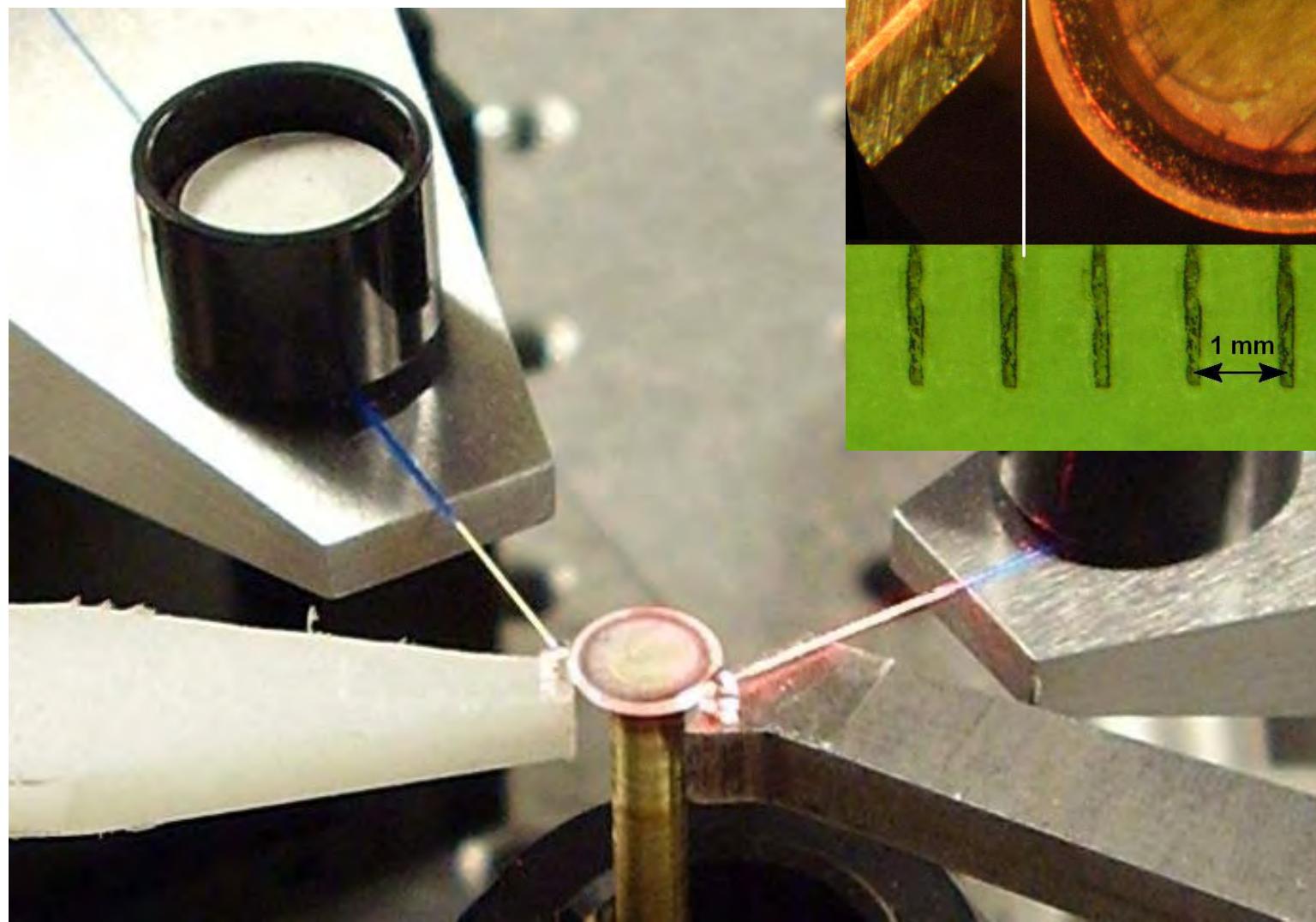


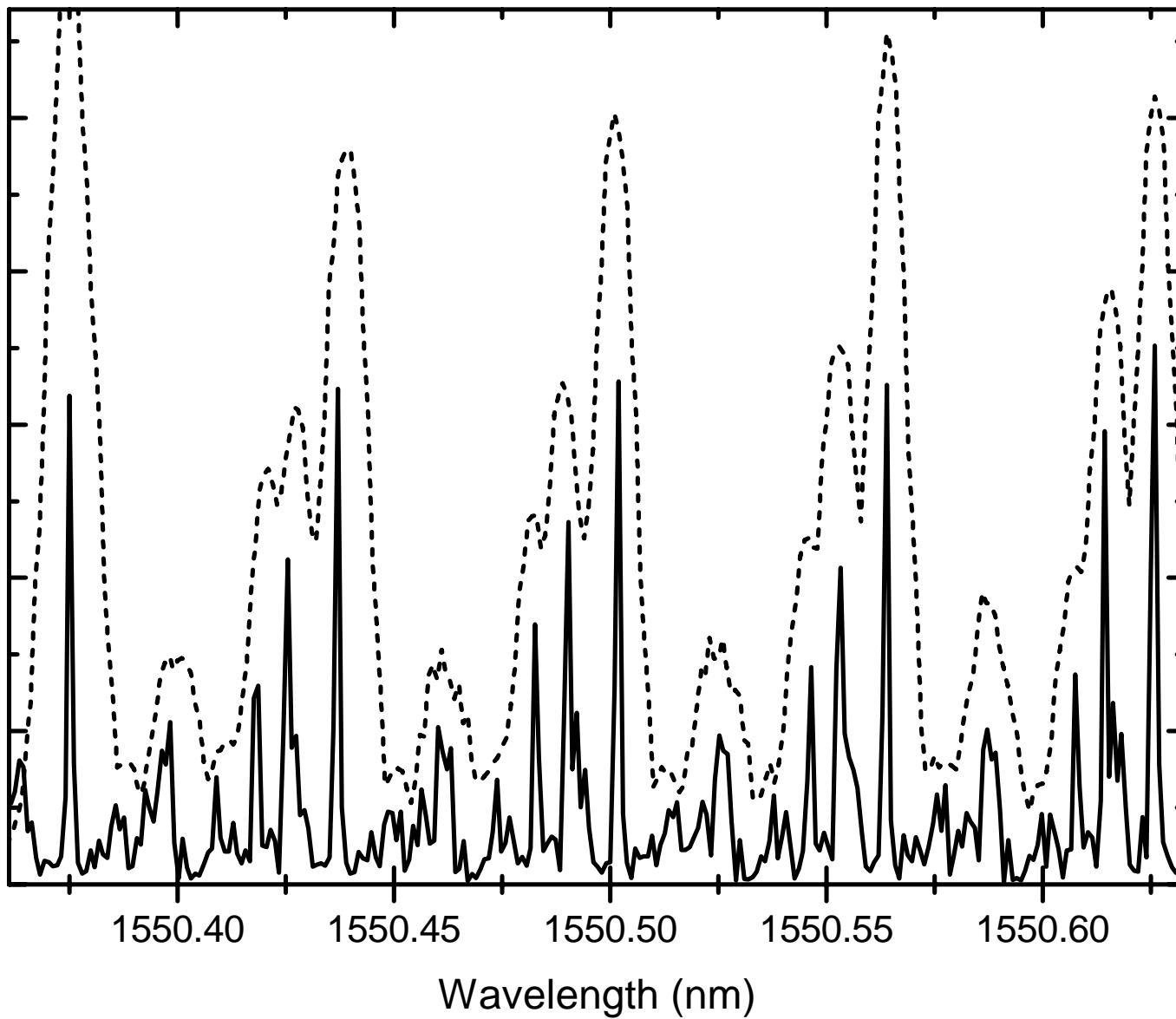
R. C. J. Hsu *et al.*, *Nature Photonics* **1**, 535 (2007).

L. Rayleigh, *Philos. Mag.* **27**, 100 (1914).

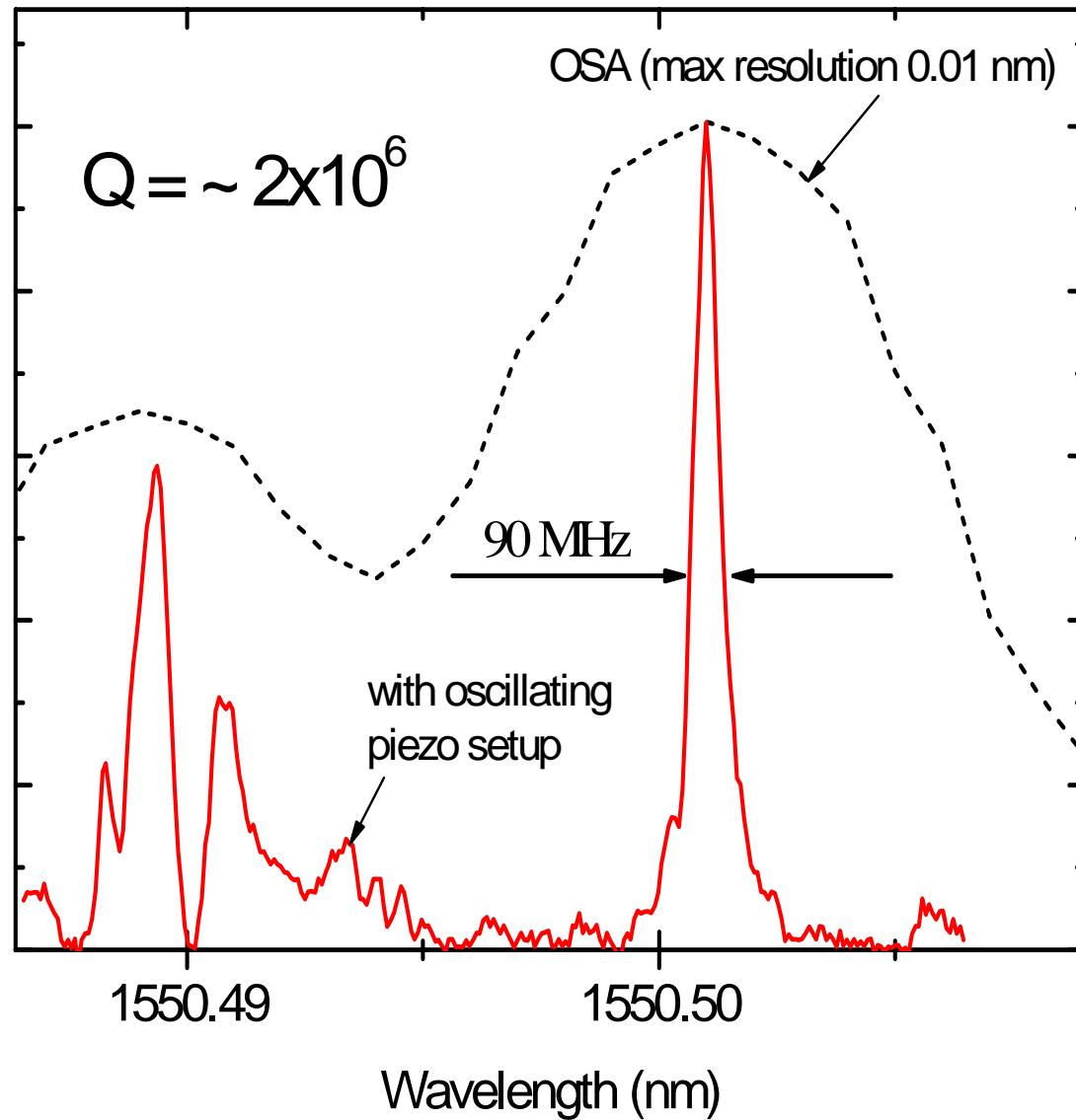
A. B. Matsko *et al.*, *IEEE J. Sel. Top. Quantum Electron.* **12**, 3-14 (2006)





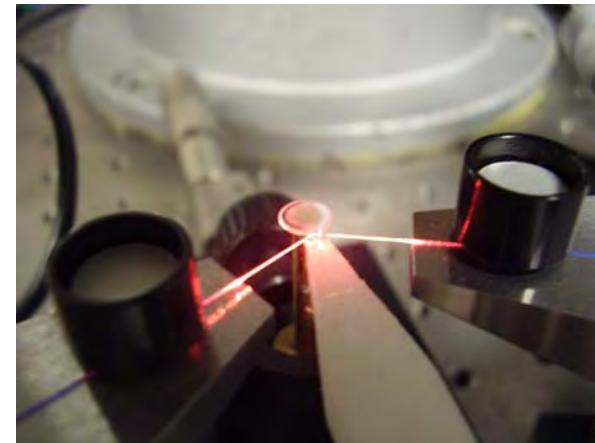
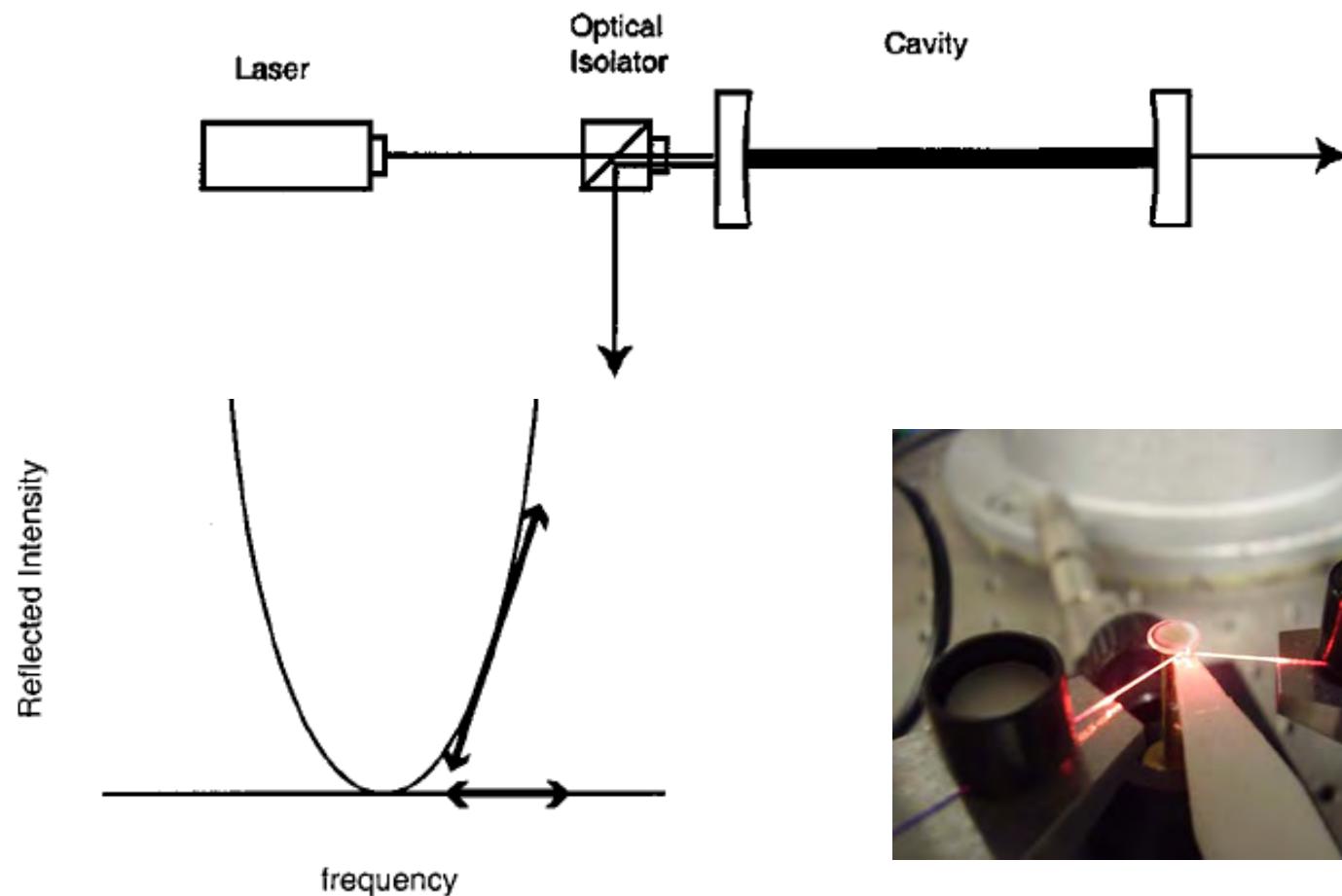


Z. Gaburro, *J. Nanophoton.* **2**, 021853 (2008)

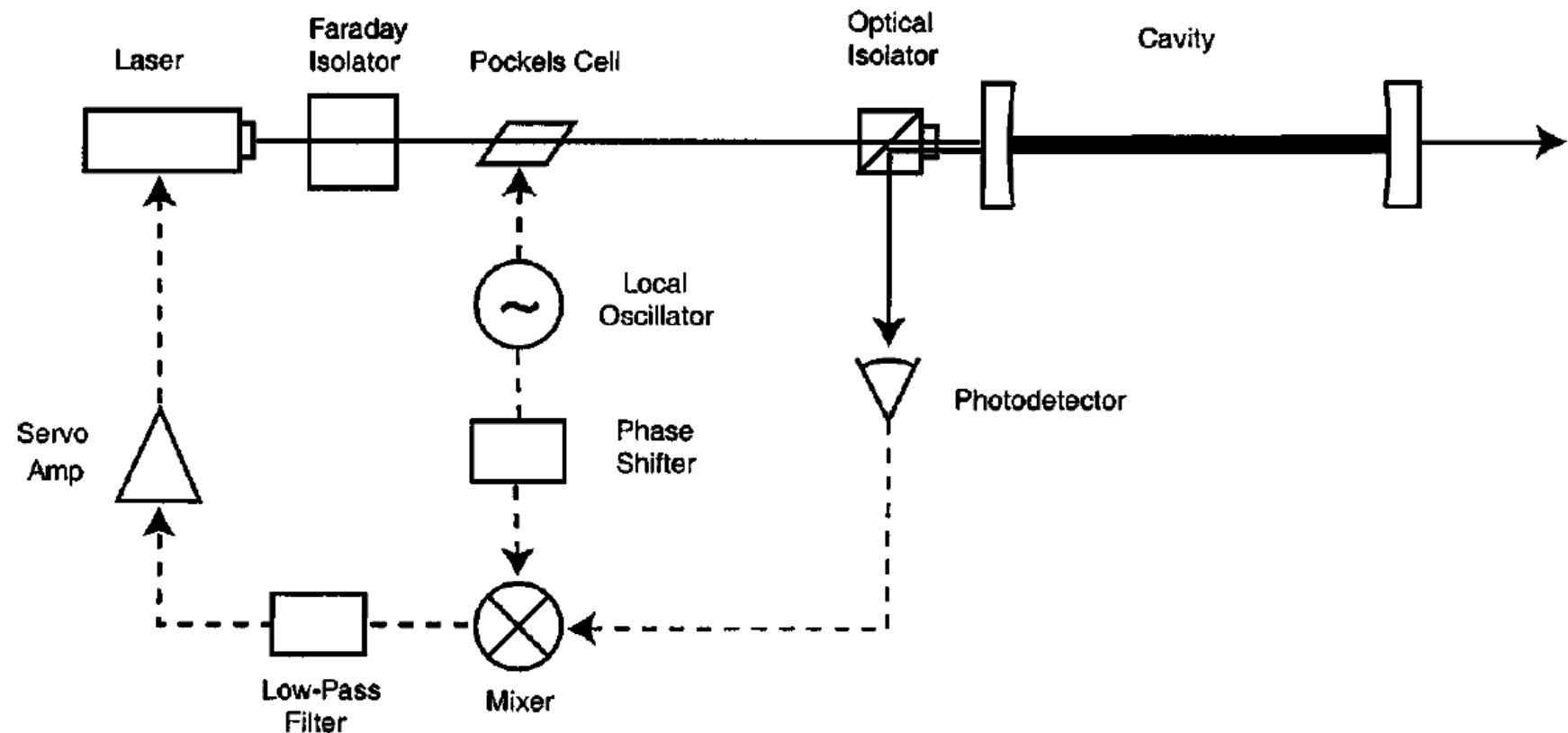


Z. Gaburro, *J. Nanophoton.* **2**, 021853 (2008)

# Pond-Drever-Hall stabilization

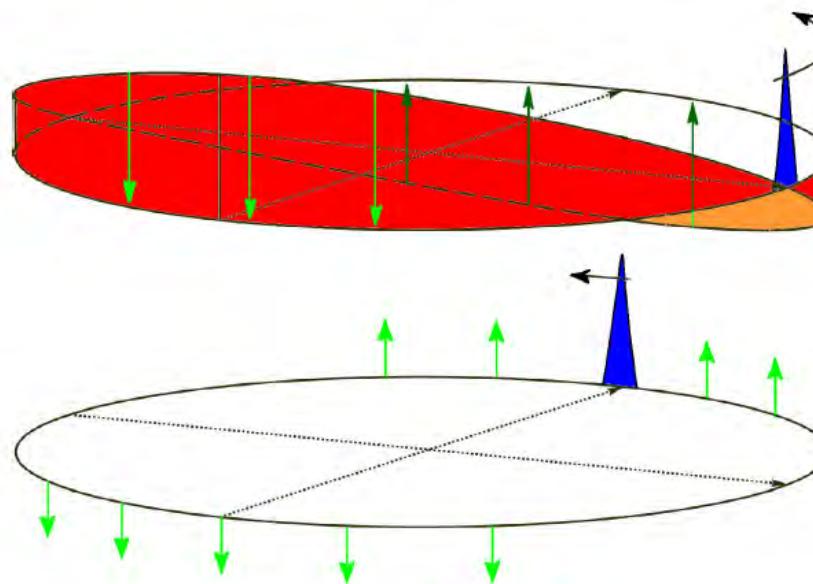
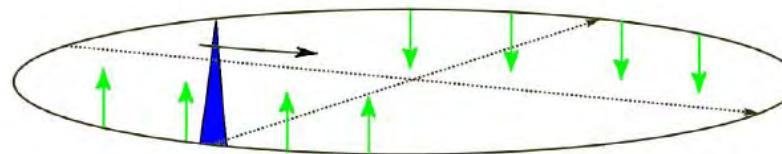
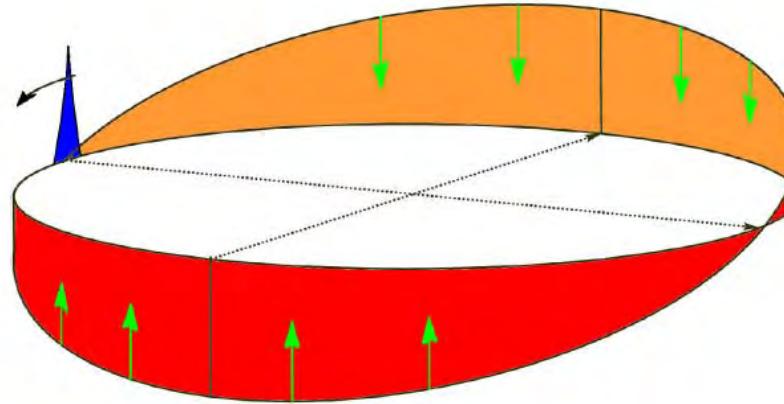


R. Drever *et al.*, Appl. Phys. B: Photophys. Laser Chem. **31**, 97–105 (1983).

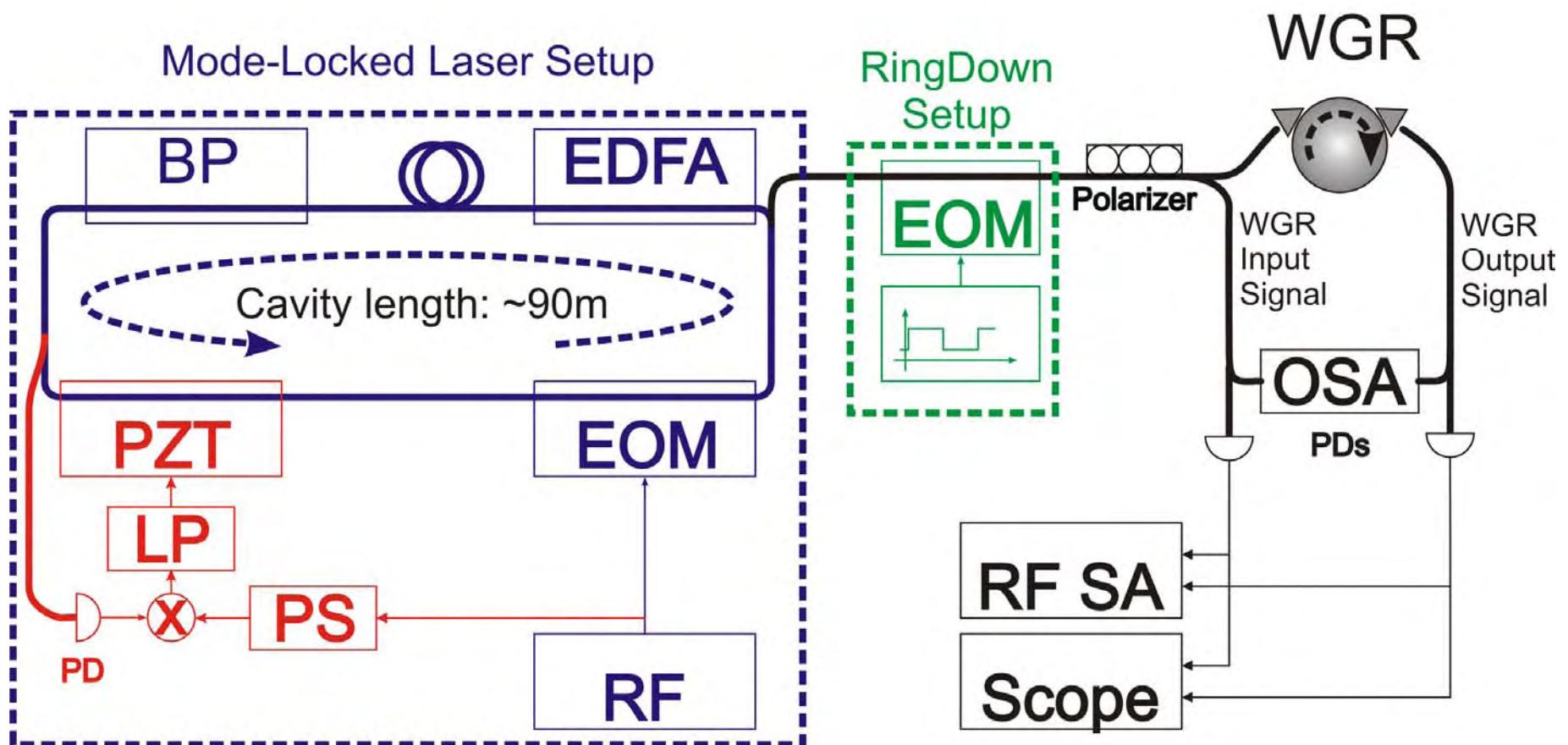


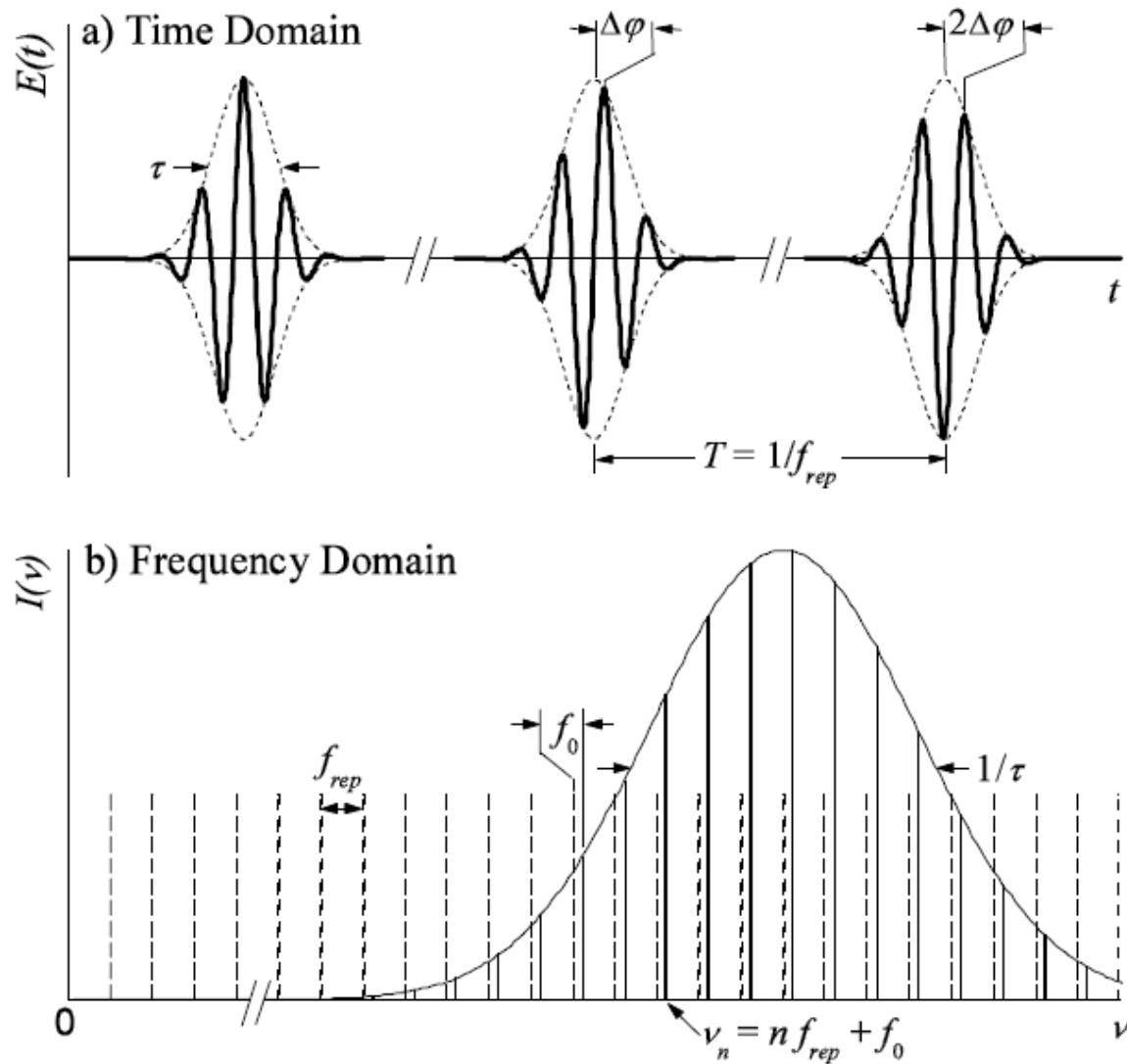
$$E_{\text{inc}} = E_0 e^{i(\omega t + \beta \sin \Omega t)} = E_0 [J_0(\beta) e^{i\omega t} + J_1(\beta) e^{i(\omega + \Omega)t} - J_1(\beta) e^{i(\omega - \Omega)t}]$$

E. Black, *Am. J. Phys.* **69**, 79-87 (2001)

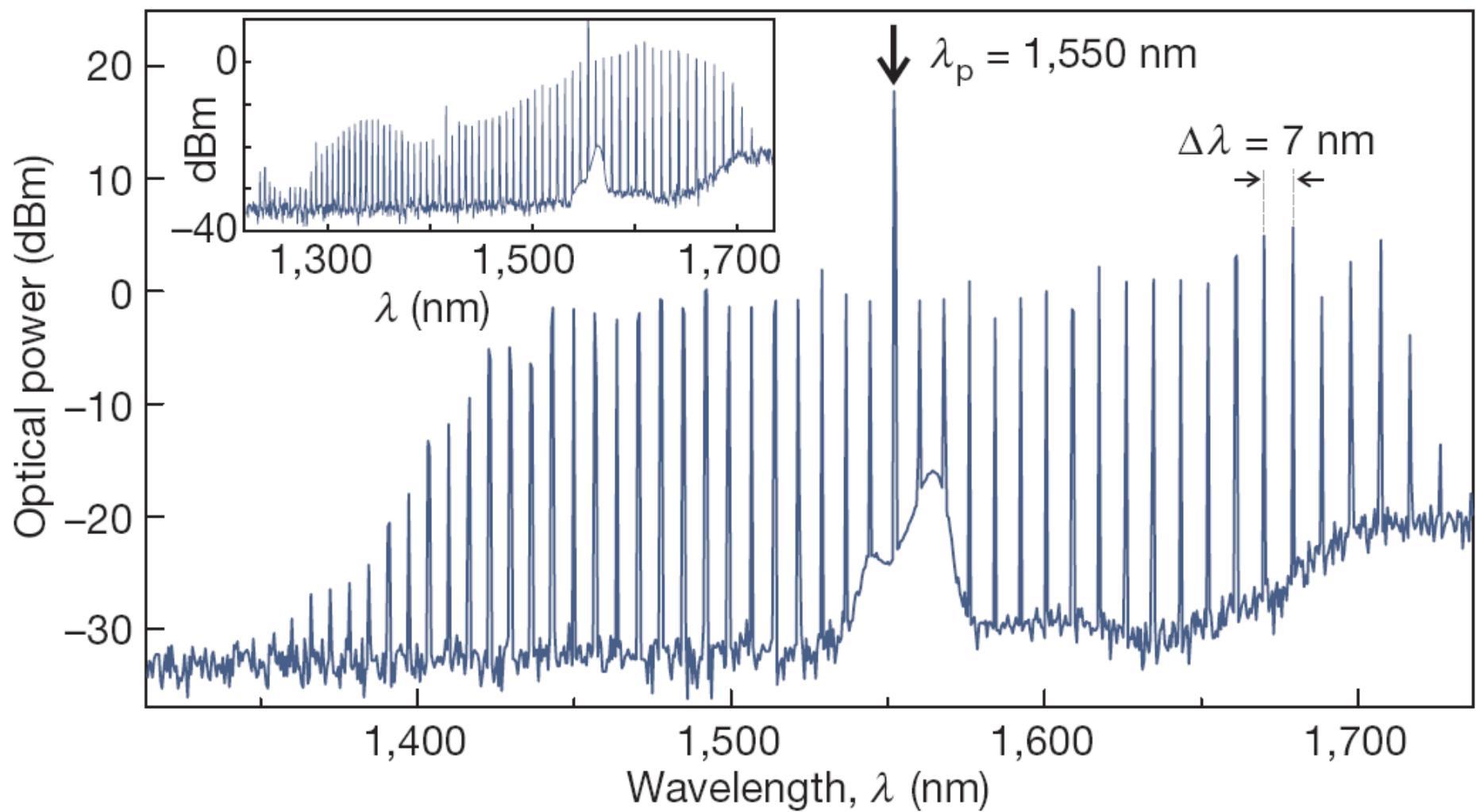


# Setup





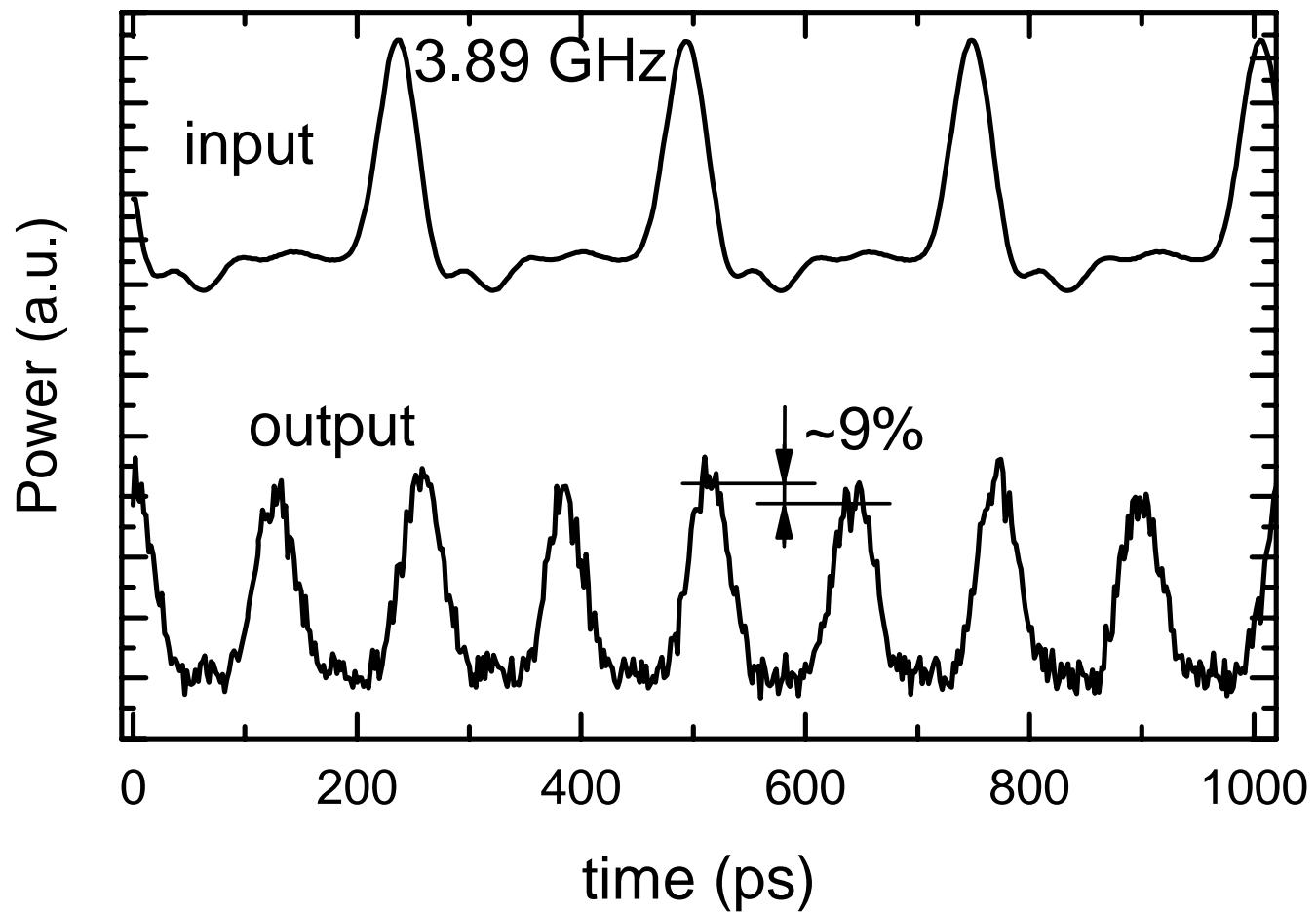
Jun Ye (*JILA, National Institute of Standards and Technology*)  
 Thorpe *et al.*, *Science* **311**, 1595-1599 (2006)



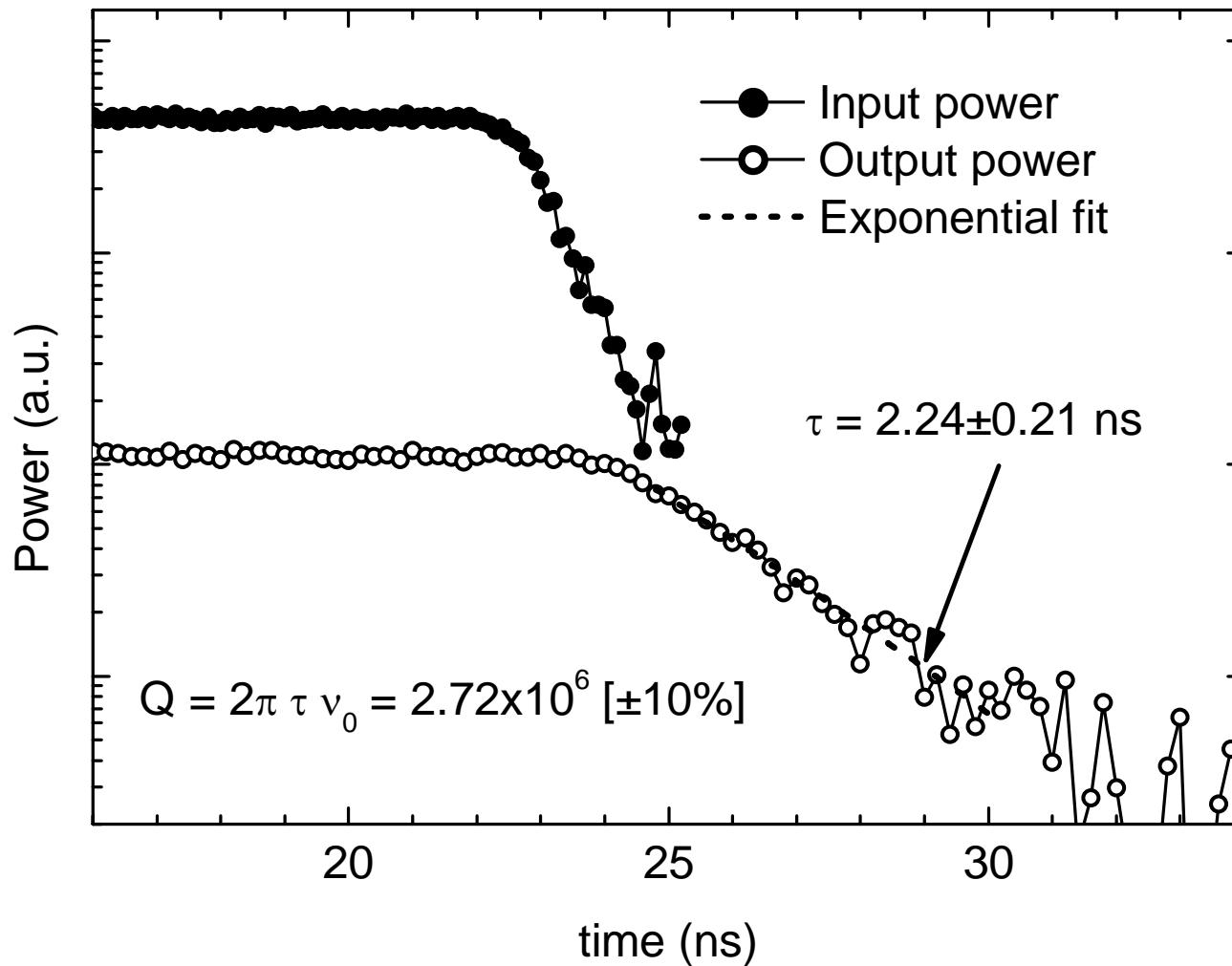
Uniformity of the mode spacing:  $7.3 \times 10^{-18}$

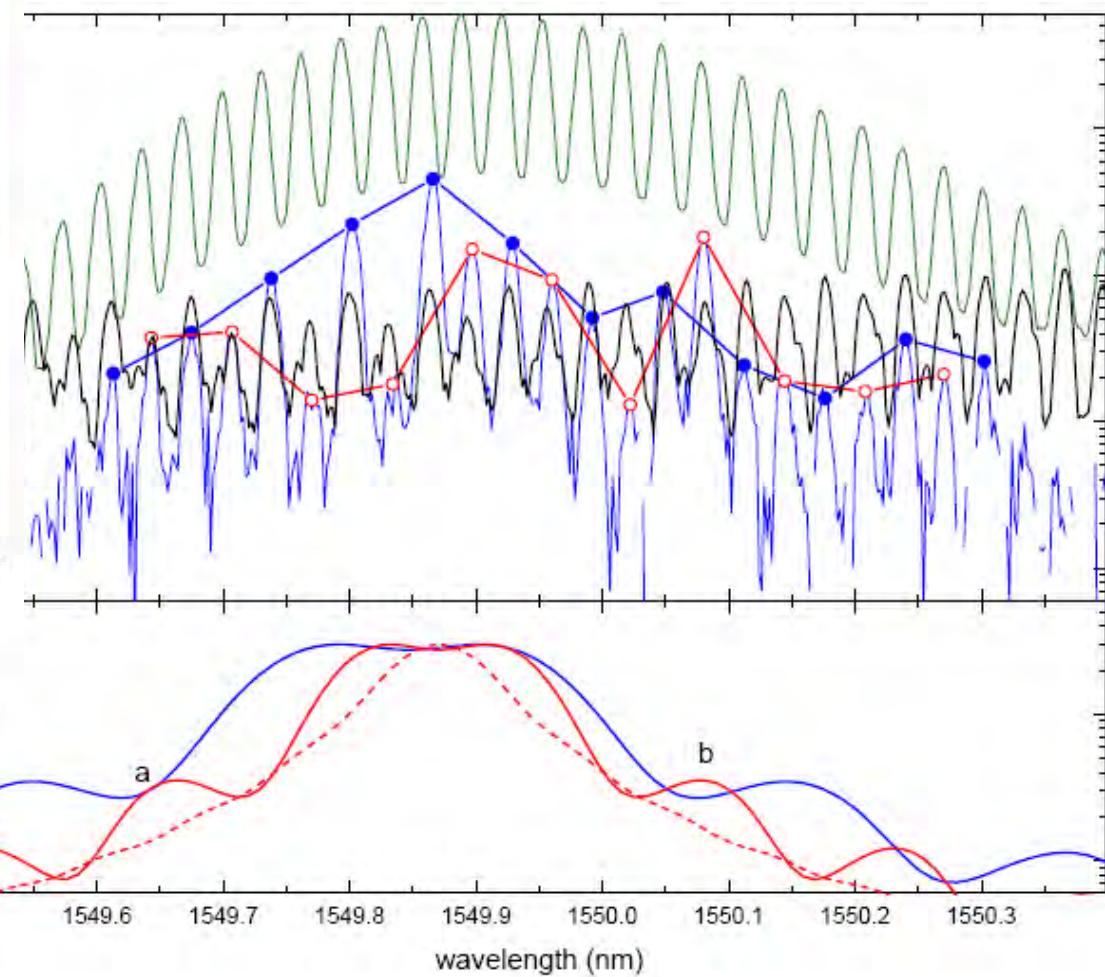
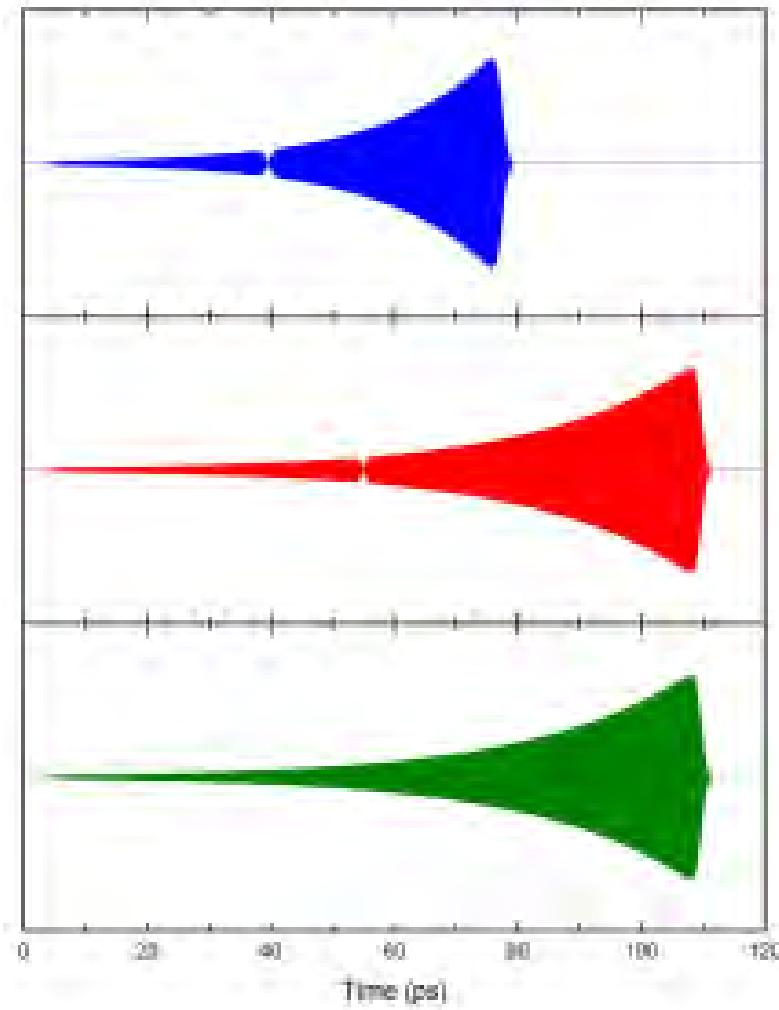
P. Del'Haye *et al.*, *Nature* **450**, 1214-1217 (2007).

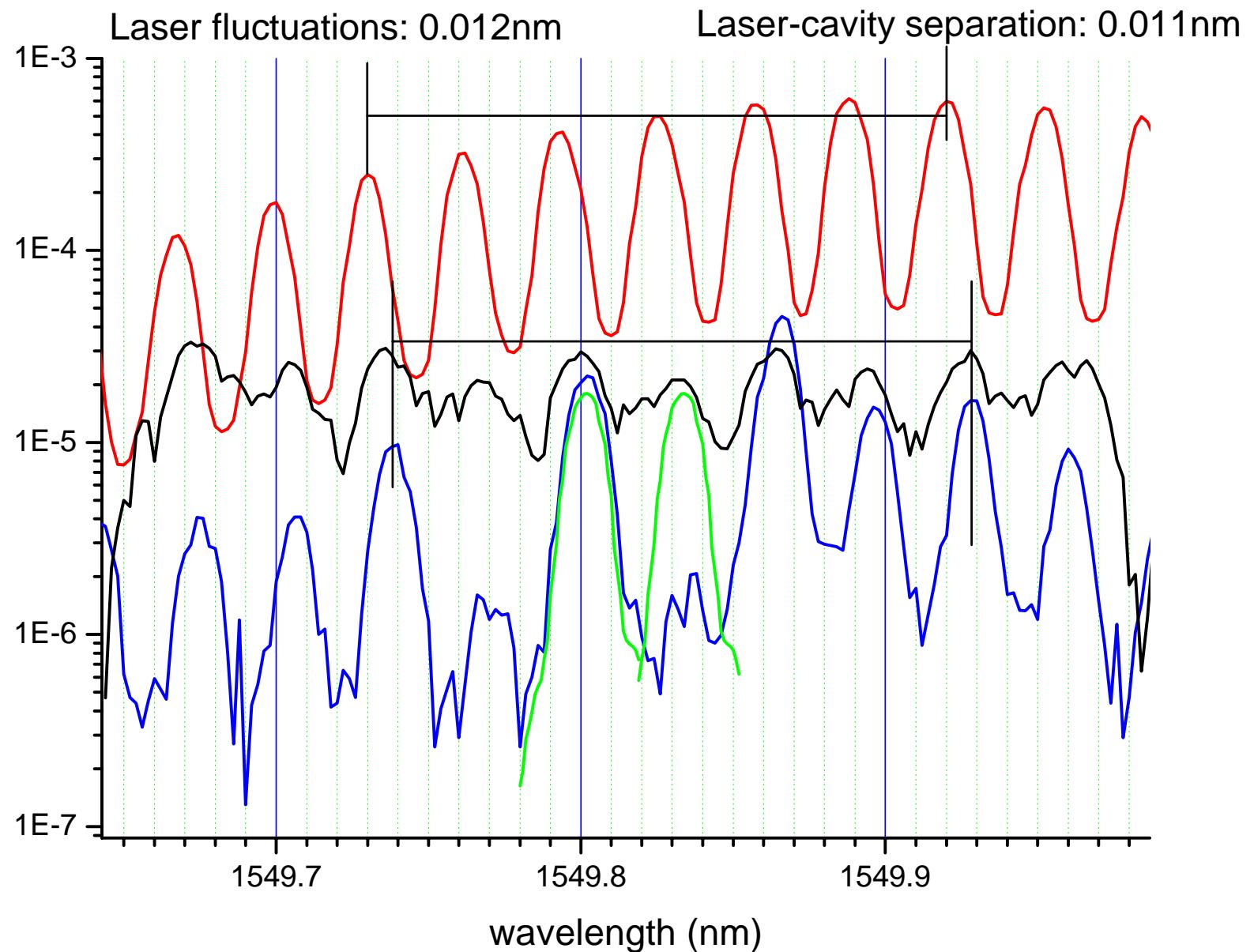
$$Q = \frac{2\pi c}{\lambda \text{ FSR} \ln(1 - F)^{-1}}$$

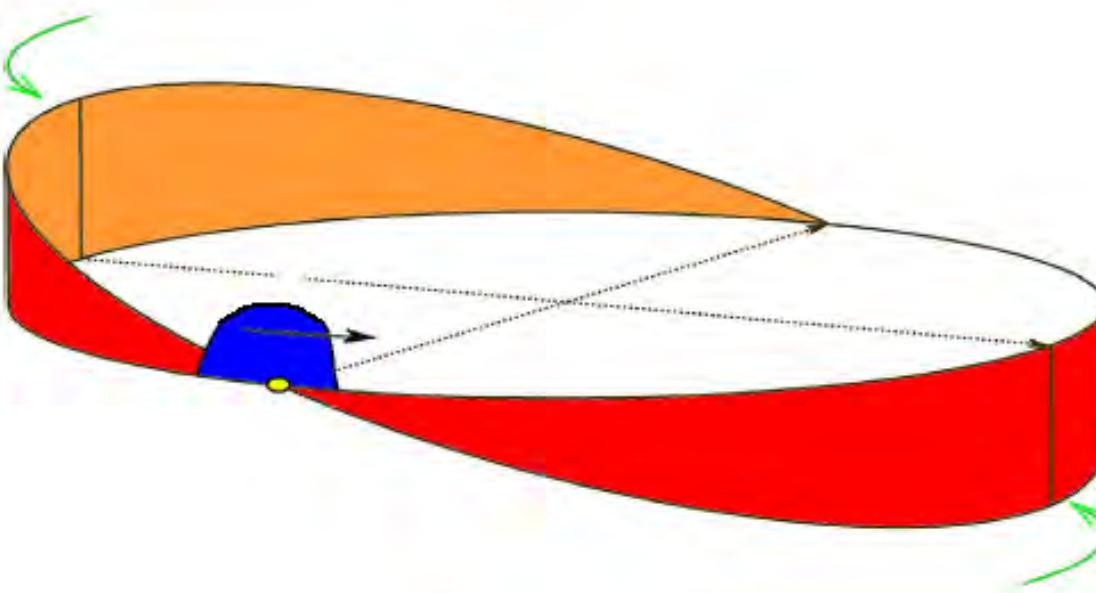
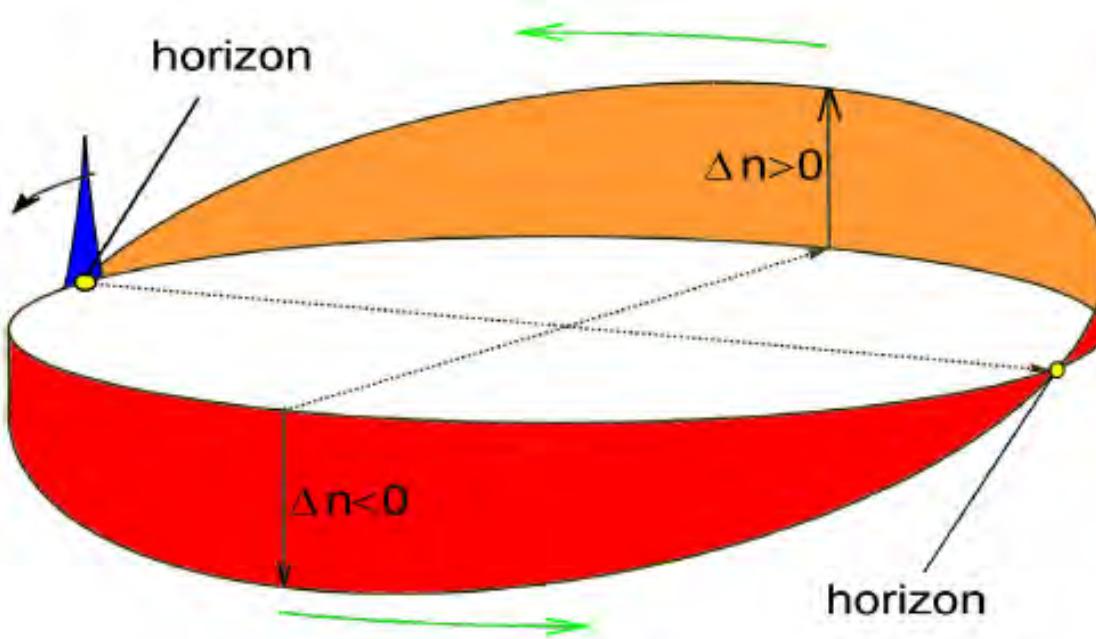


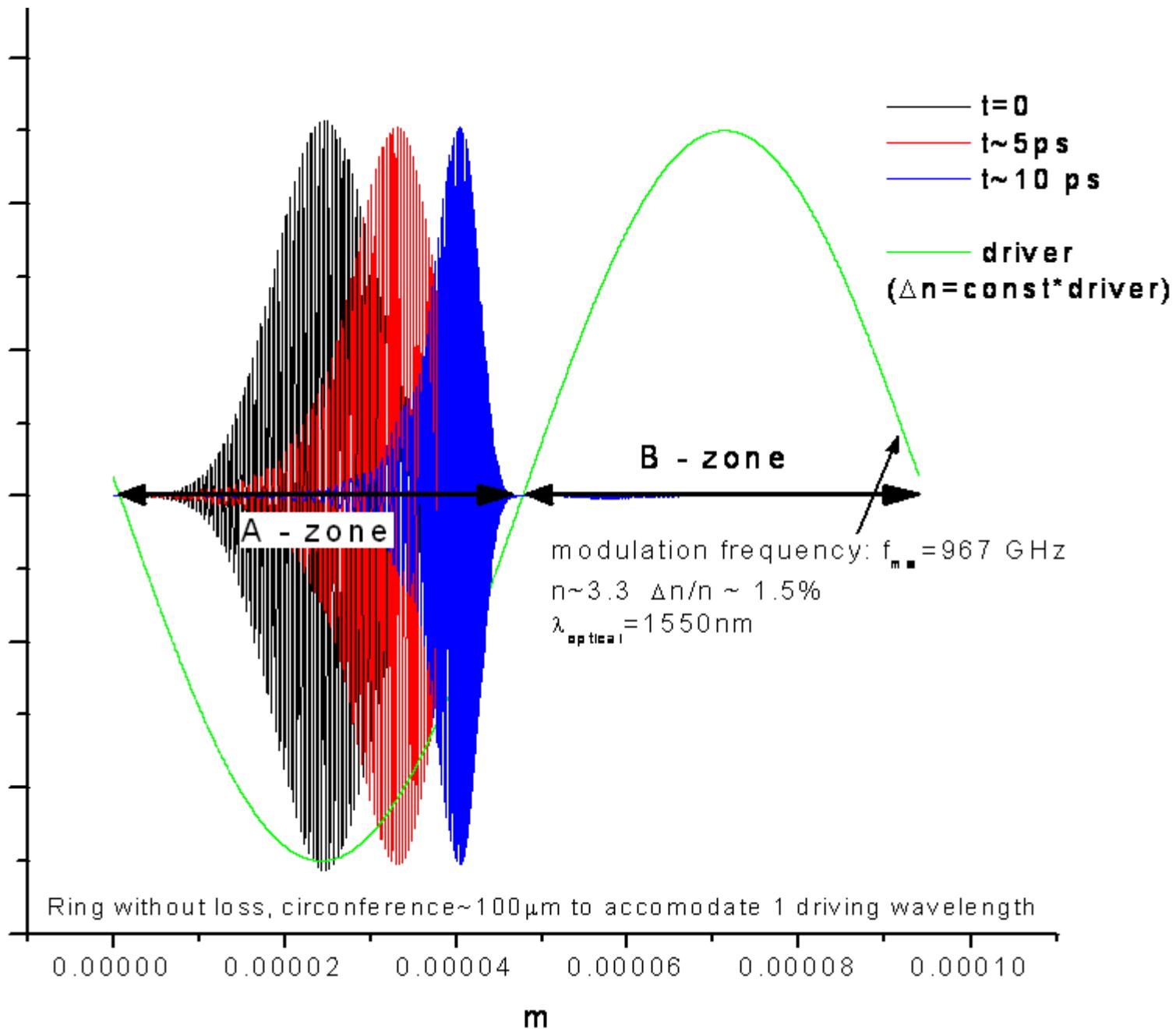
# Ringdown

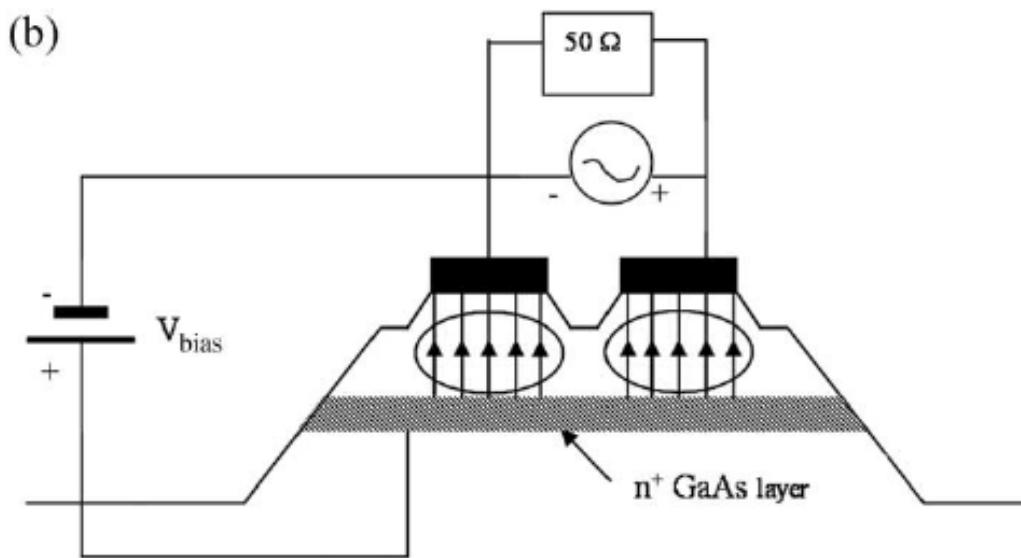
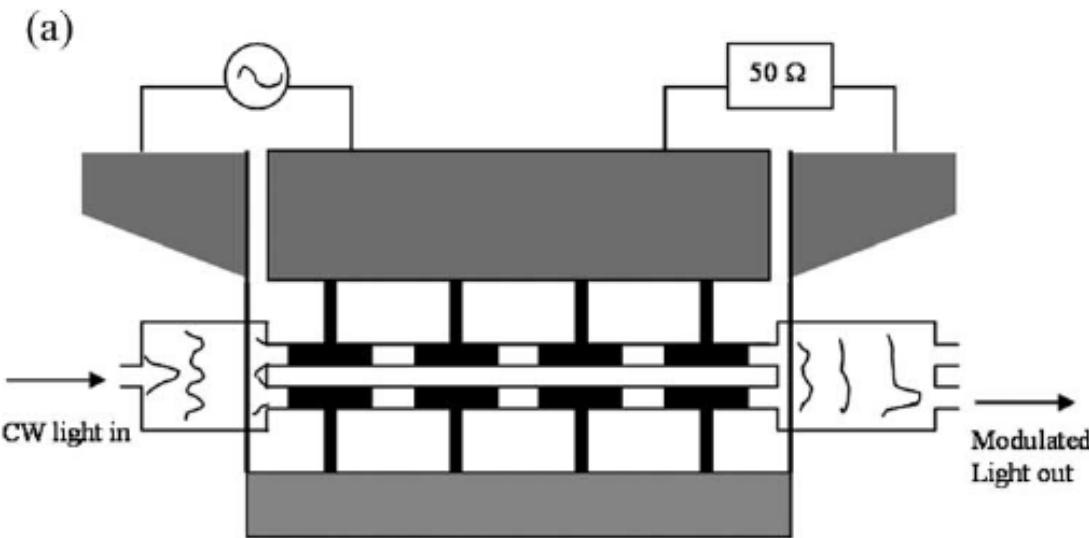










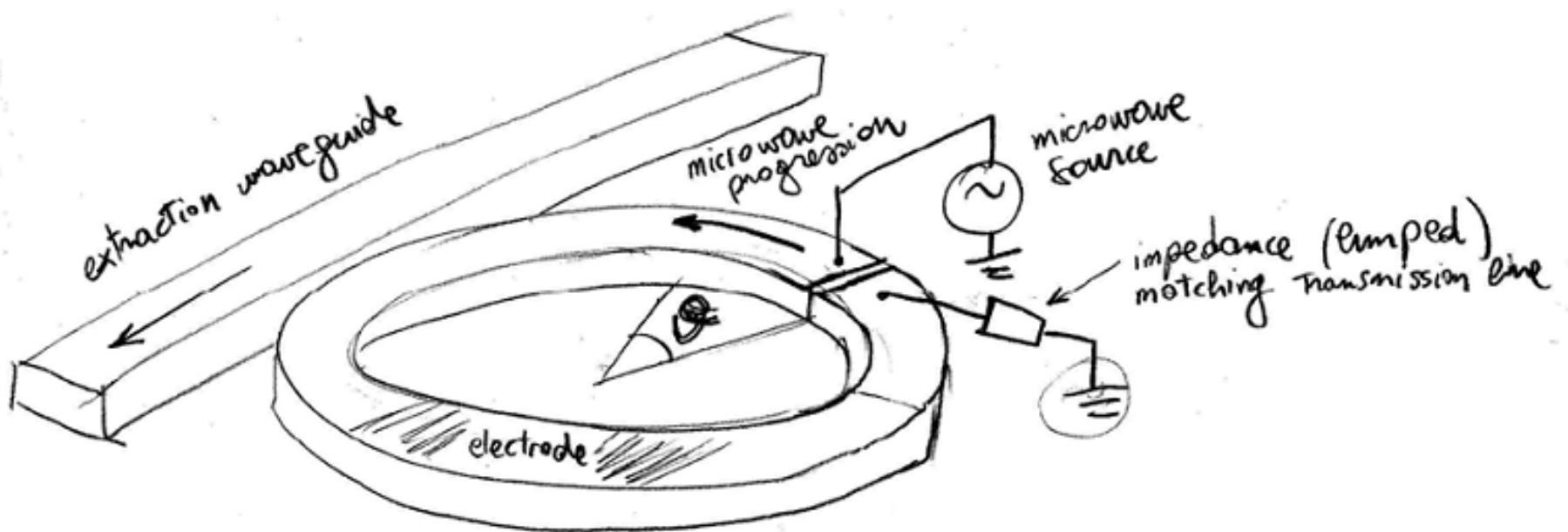


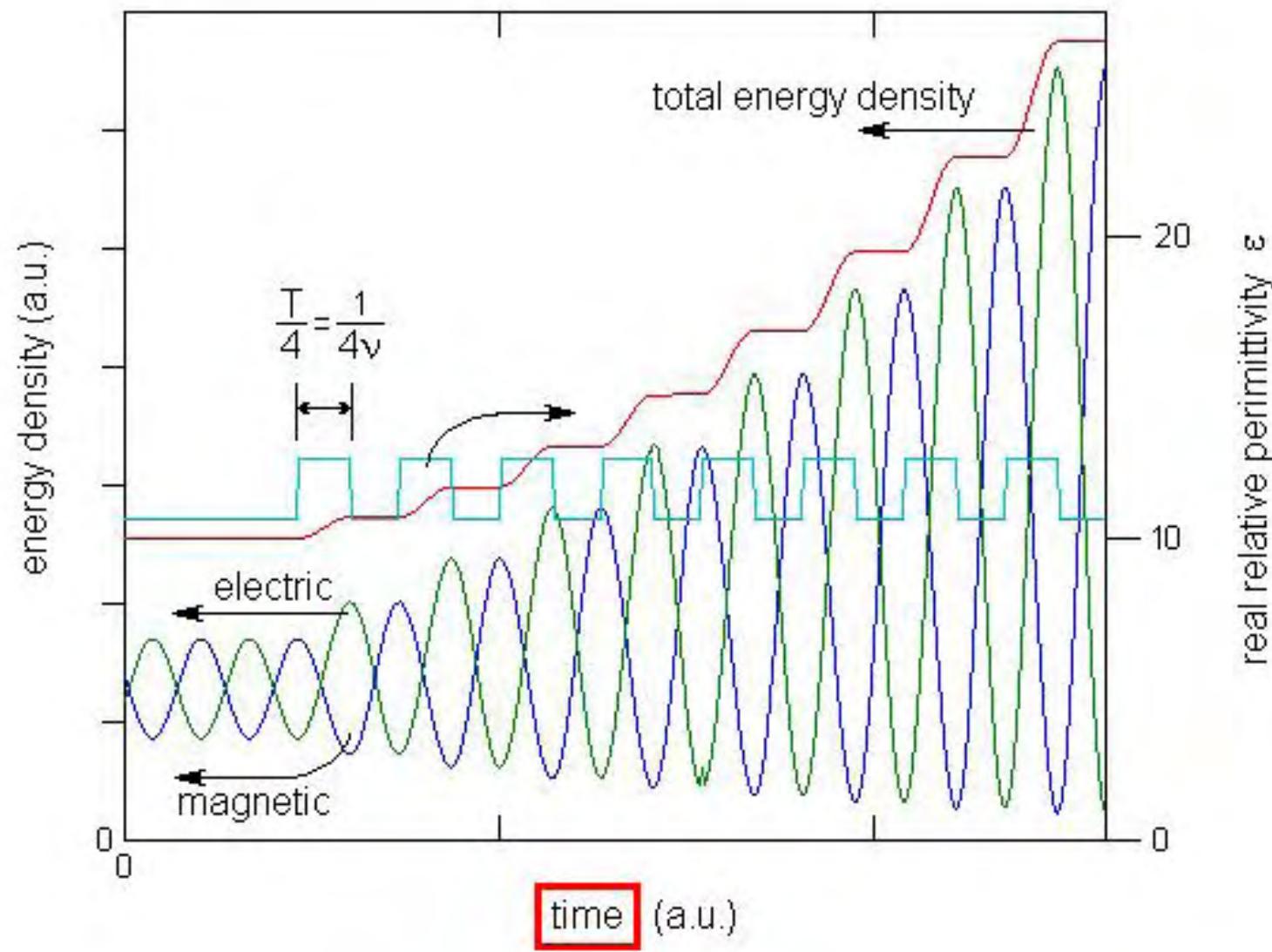
$$v_p = \frac{1}{\sqrt{LC}} = \frac{c_0}{n_m}$$

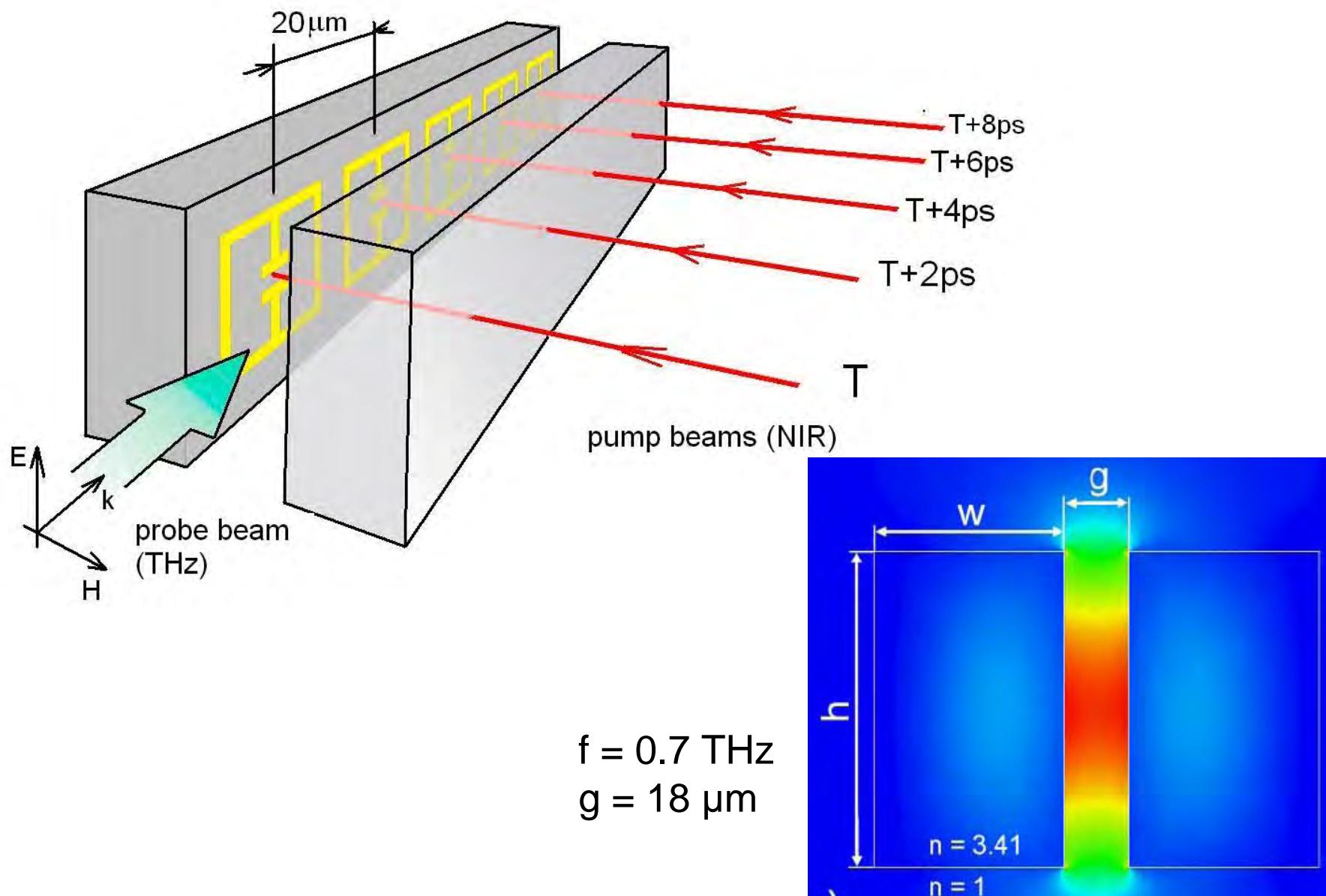
$$C = C_u + C_l$$

$$n_o = 3.5284$$

Cui J., and Berini P., *J. of Lightwave Technol.* **24**, 544 (2006).







M. Nagel et al., *Optics Express* **14**, 9944 (2006).