

Surface States of Rashba Spin-Split Type and Topological Insulators

Bi : Bulk = Semi-metal,
Surface = Spin-split metal (Rashba effect)

$\text{Bi}_{1-x}\text{Sb}_x$, Bi_2Se_3 ↓
: Bulk = Insulator (Topological Insulator)
Surface = Spin-split metal (Topological Metal)

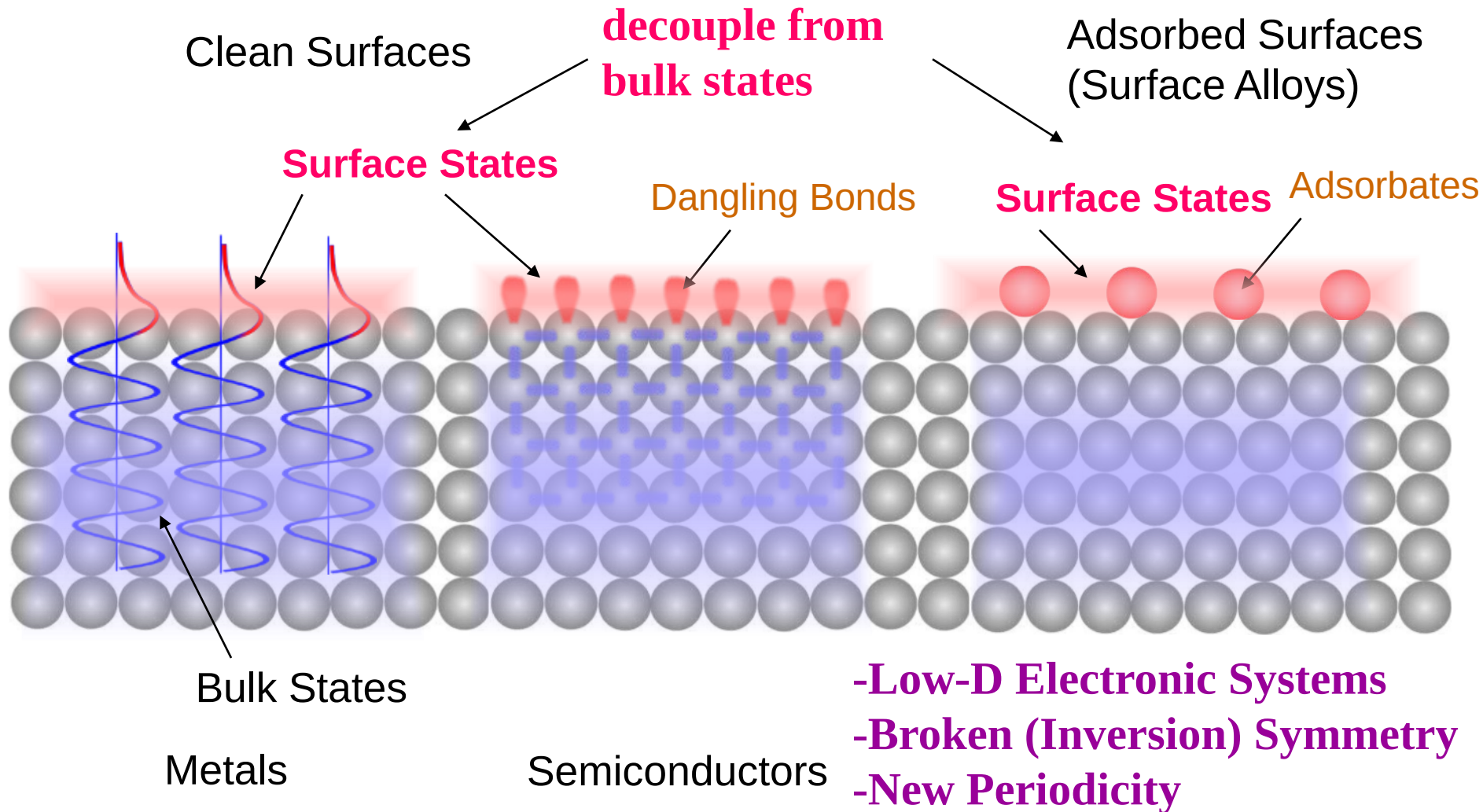
¹ Dept. Phys., Univ. Tokyo ² UVSOR ³ ISSP, Univ. Tokyo

⁴ HSRC ⁵ Julich, Germany ⁶ San Sebastian, Spain

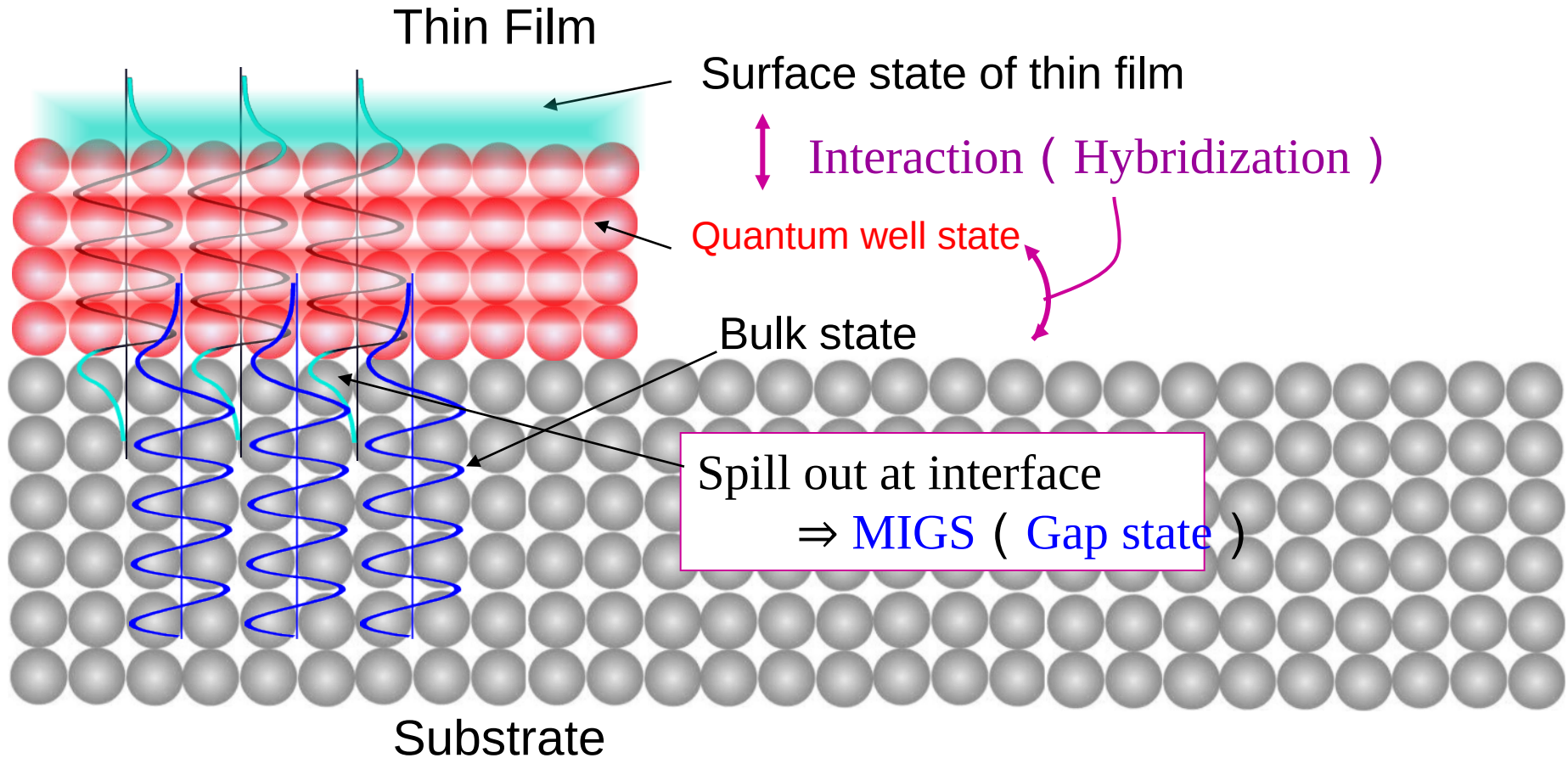
T. Hirahara,¹ Y. Sakamoto,¹ M. Yamada¹, Y. Saisyu,¹ H. Miyazaki,²
S. Kimura,² T. Okuda,^{3,4} G. Bihlmayer,⁵ E. V. Chulkov⁶, S. Hasegawa¹



Surface States — Shockley & Tamm States —



Thin Film and Interface



Ex: Interaction between QWS and surface state

QWS's are spin-split

← Spin-split surface state due to Rashba-effect

K. He, et al., PRL
101, 107604 (2008)

Various Surface States

1. Shockley states (extended)

Tamm states (localized)

Chemical bonding, Potential
(Previous slide)

2. Image states

Image charge

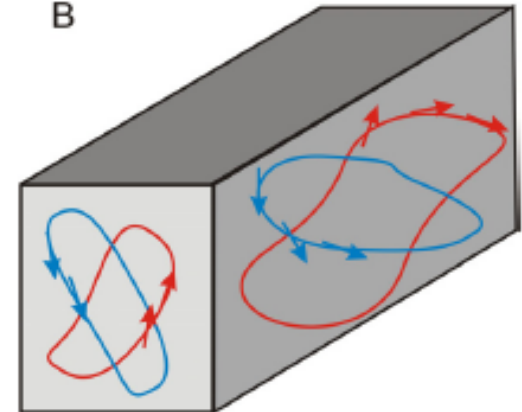
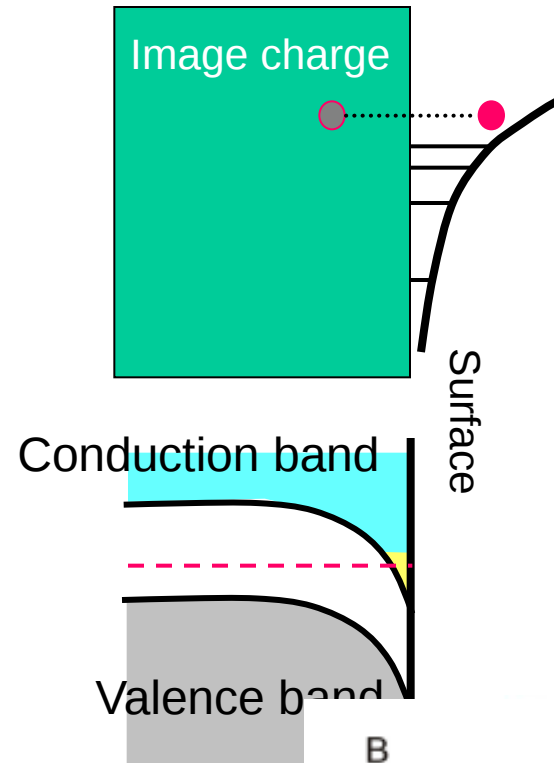
3. Surface space-charge layer

Bending of bulk bands

4. Topological surface states

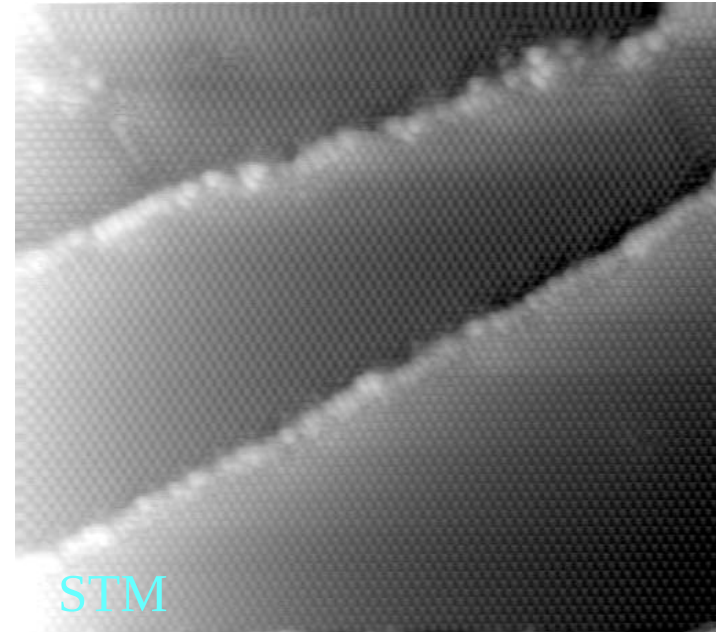
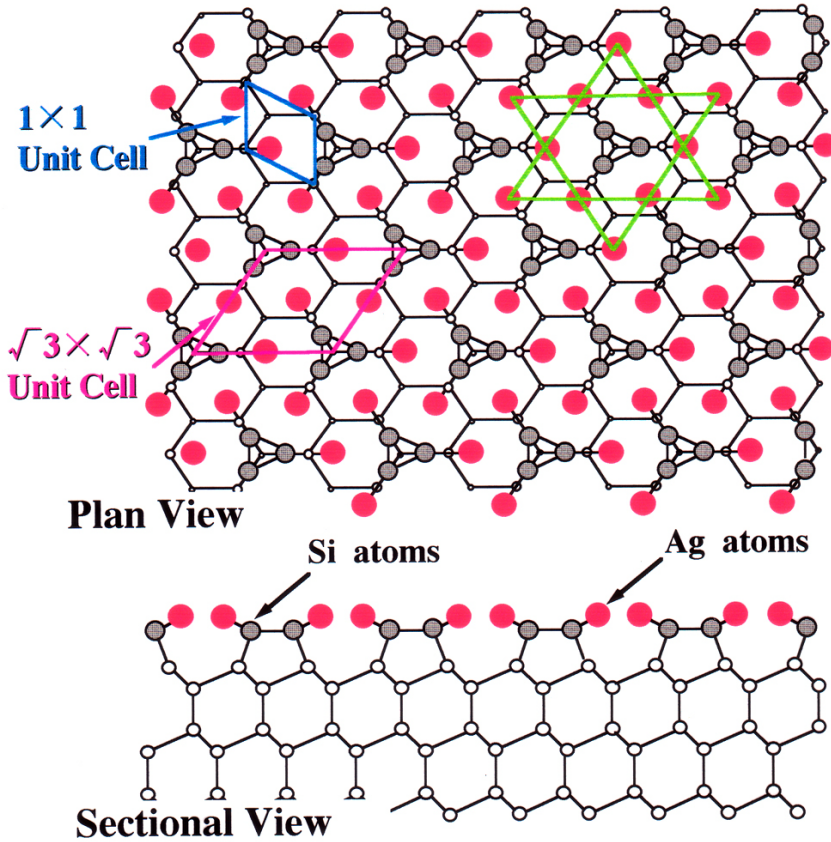
Spin-orbit coupling ← Edge states of Q(S)H phase

HgTe (QW), $\text{Bi}_{1-x}\text{Sb}_x$, Bi_2Te_3 , Bi_2Se_3 ,



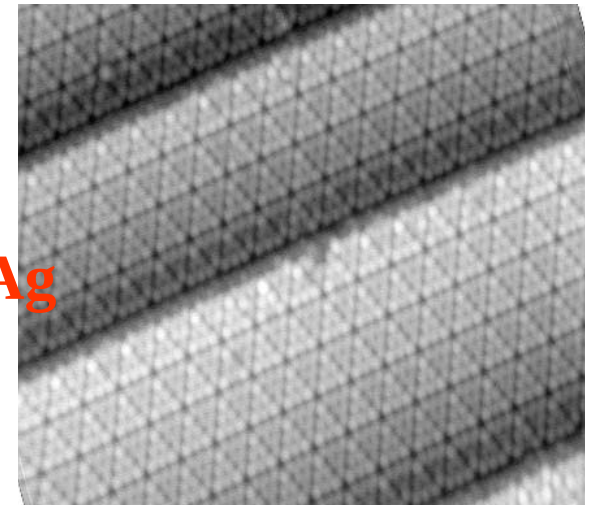
MonAtomic Layer of Ag: Si (111)- $\sqrt{3}\times\sqrt{3}$ -Ag Surface

2D Metal



**Deposit
Monolayer of Ag**

**Clean
Si(111)- 7×7**

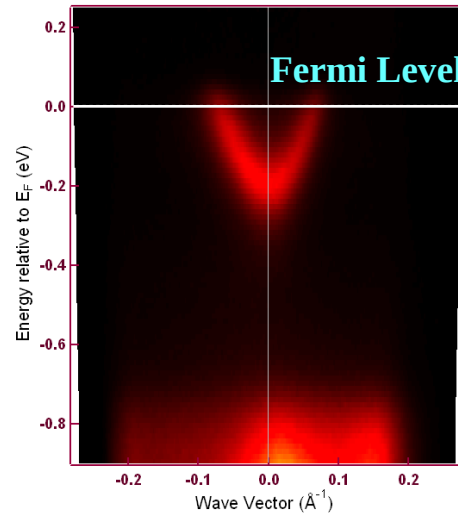
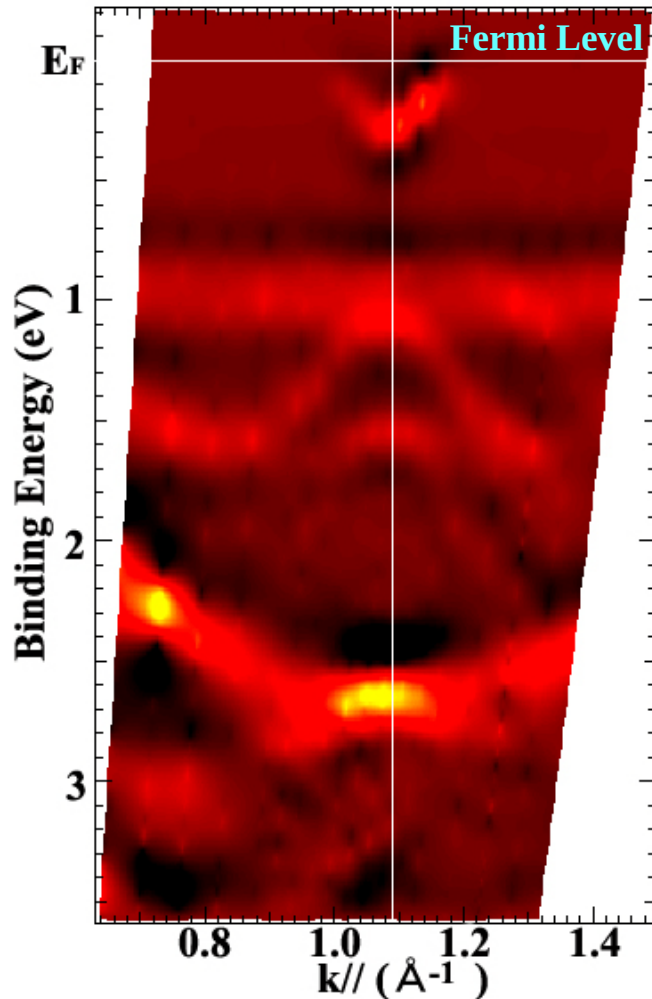


Surface-state bands of Monolayer Ag : Si(111)- $\sqrt{3}\times\sqrt{3}$ -Ag

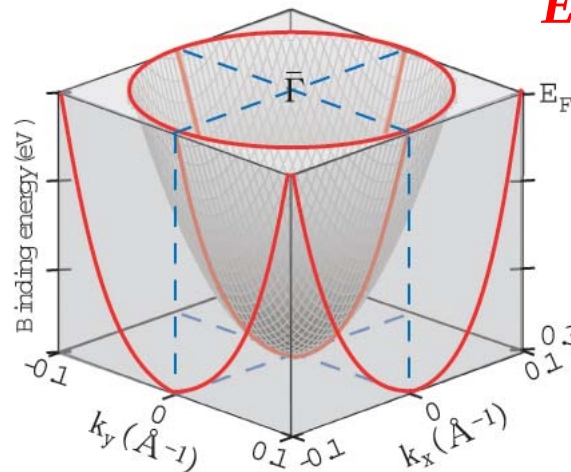
ARPES

S. Hasegawa, *et al.*, Prog. Surf. Sci. **60** (1999) 89.
T. Hirahara, *et al.*, e-J. Surf. Sci. Nanotech. **2** (2004) 141.
T. Hirahara, *et al.*, Surf. Sci. **563** (2004) 191.

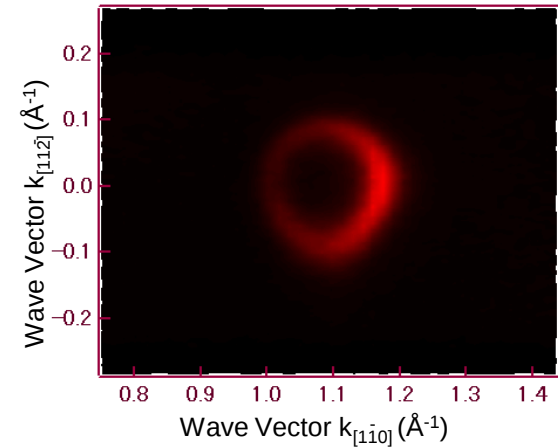
Band Dispersion



$$m^* = 0.13m_e$$



Fermi Surface Mapping



Parabolic Dispersion

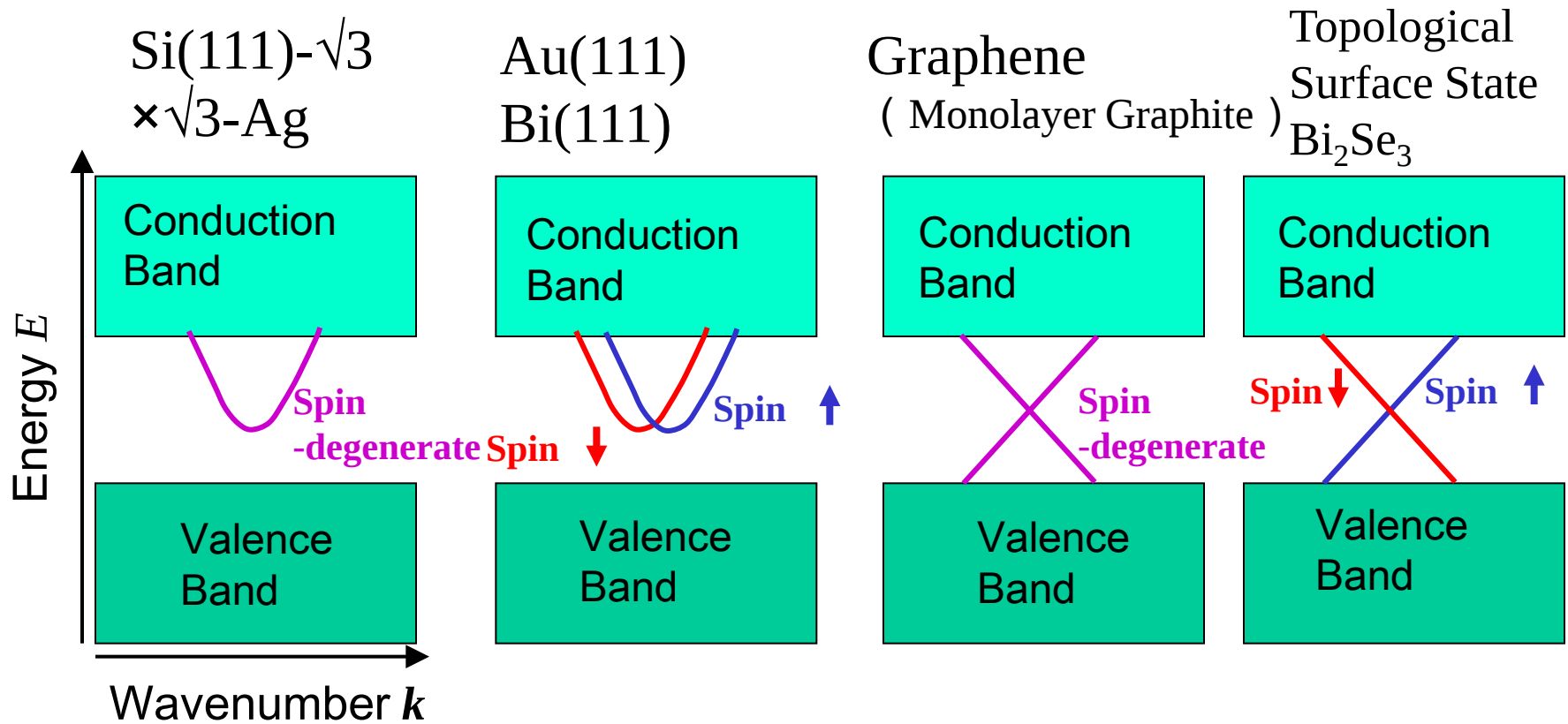
$$E = \frac{\hbar^2 k^2}{2m^*} \longrightarrow \text{Free-electron}$$

Metallic

Fermi Circle

Isotropic, Metallic,
Free-electron-like
Surface state

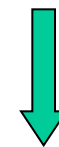
Various Surface States



$$E = \frac{p^2}{2m^*} = \frac{\hbar^2 k^2}{2m^*}$$

Free-Electron-like

$$E = \sqrt{(mc^2)^2 + (pc)^2}$$



$$m = 0$$

$$E = \pm pc = \pm \hbar ck$$

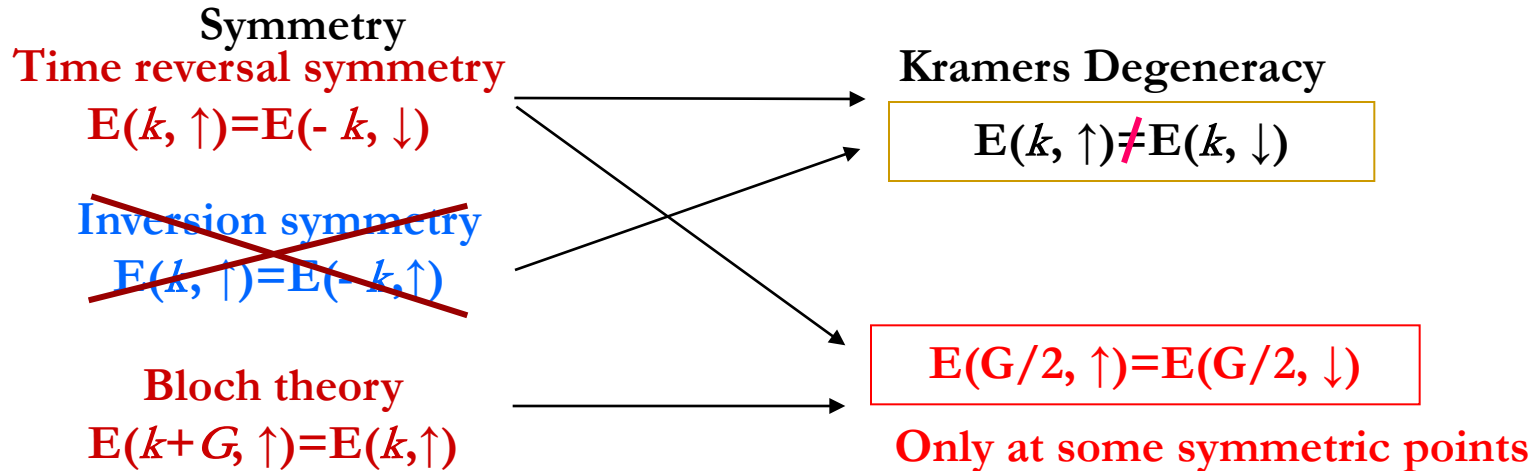
Massless Dirac Fermion

Rashba Effect in Surface States

E. I. Rashba,
Sov. Phys. Solid State **2**, 1109(1960)

$$H = \frac{1}{2m} p^2 + V(x) + \frac{1}{4mc^2} \boldsymbol{\sigma} \cdot (\text{grad} V(x) \times \mathbf{p})$$

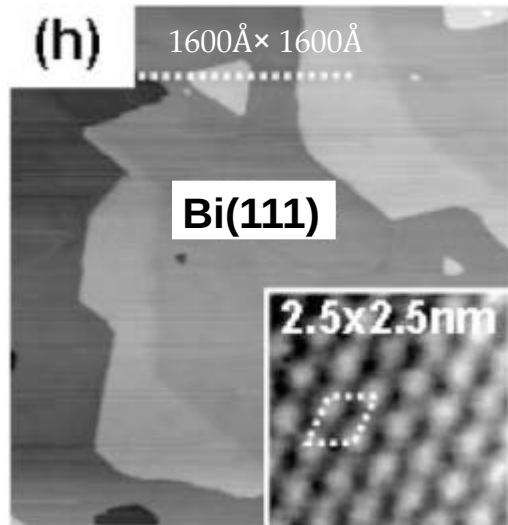
Spin-orbit coupling Hamiltonian



Atomically Flat Ultrathin Bi Film on Si(111)-7×7

T. Nagao *et al.*, PRL **93** 105501(2004)

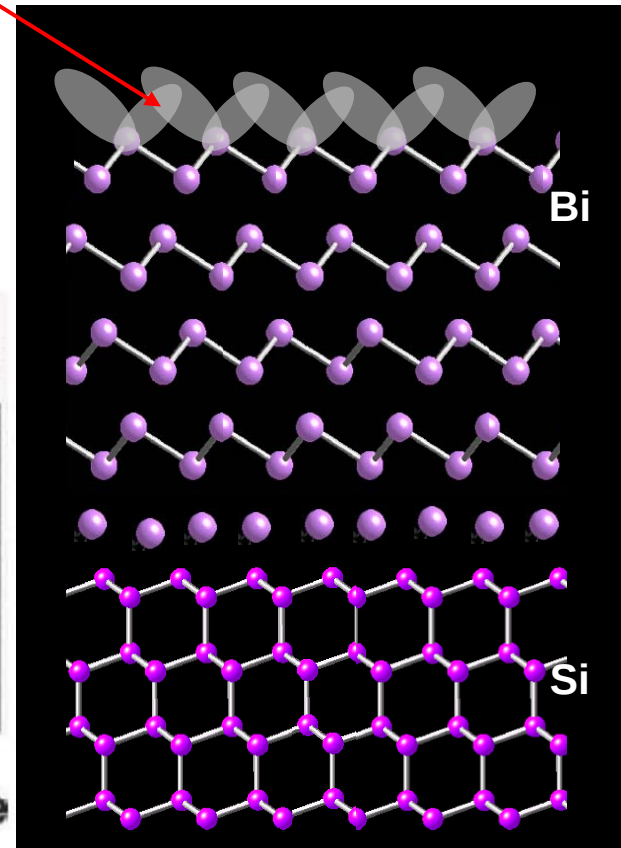
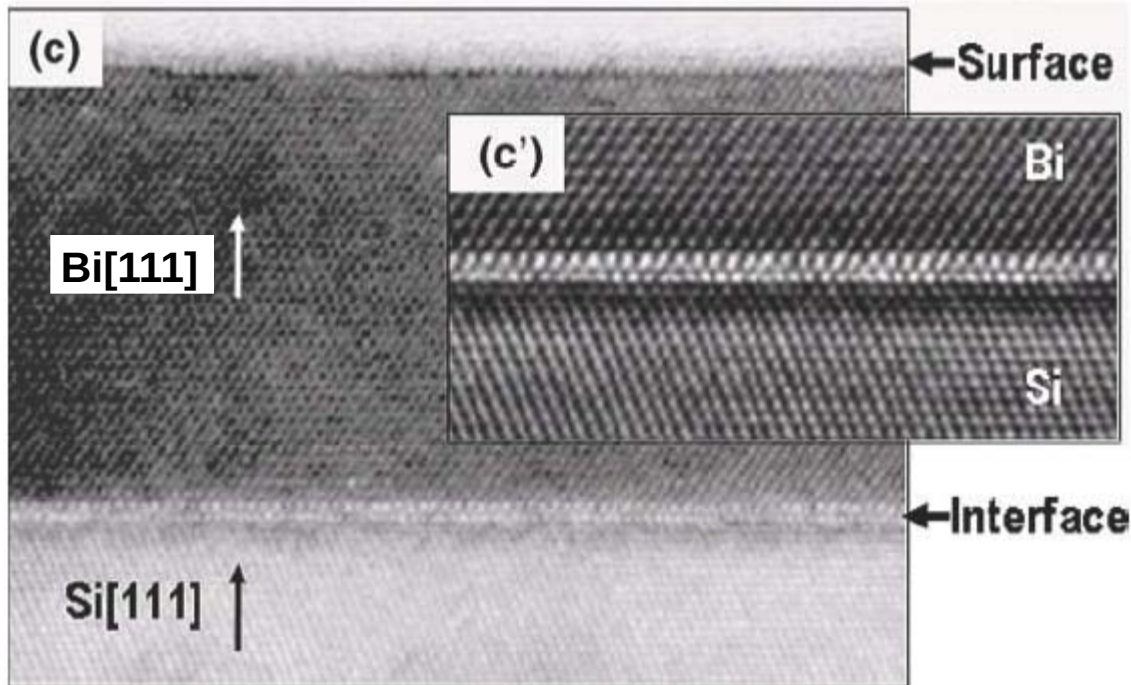
T. Nagao *et al.*,
Surf. Sci. **590**, L247-252 (2005).



STM

Surface States

XTEM



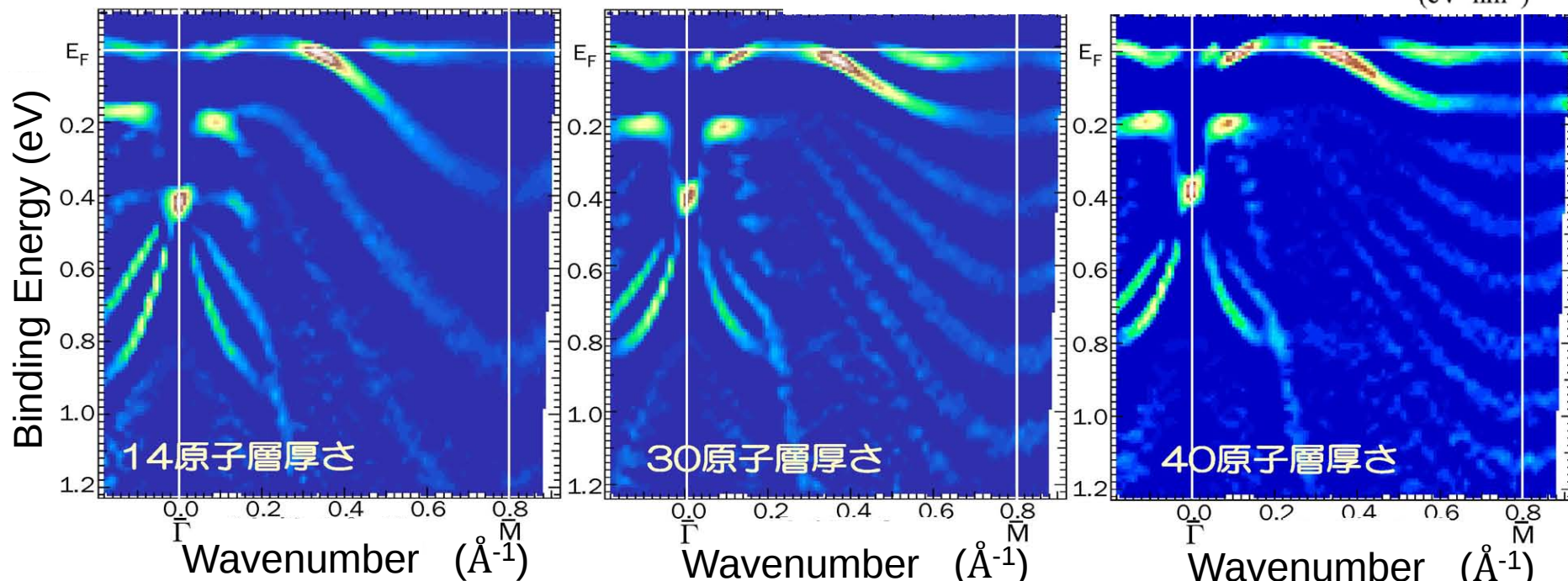
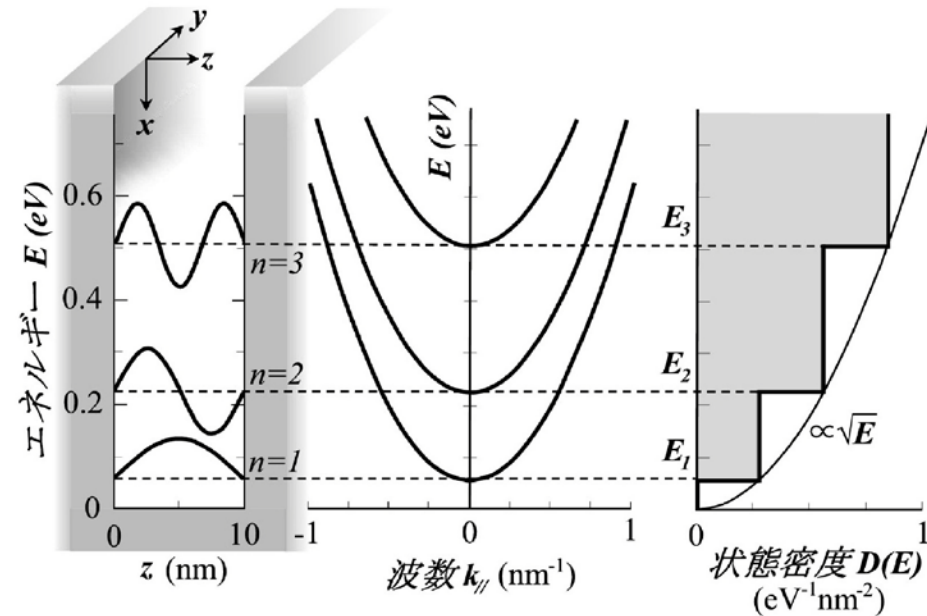
ARPES : Electronic States of Bi Quantum Well

T. Hirahara, et al., PRB 75, 035422 ('07)

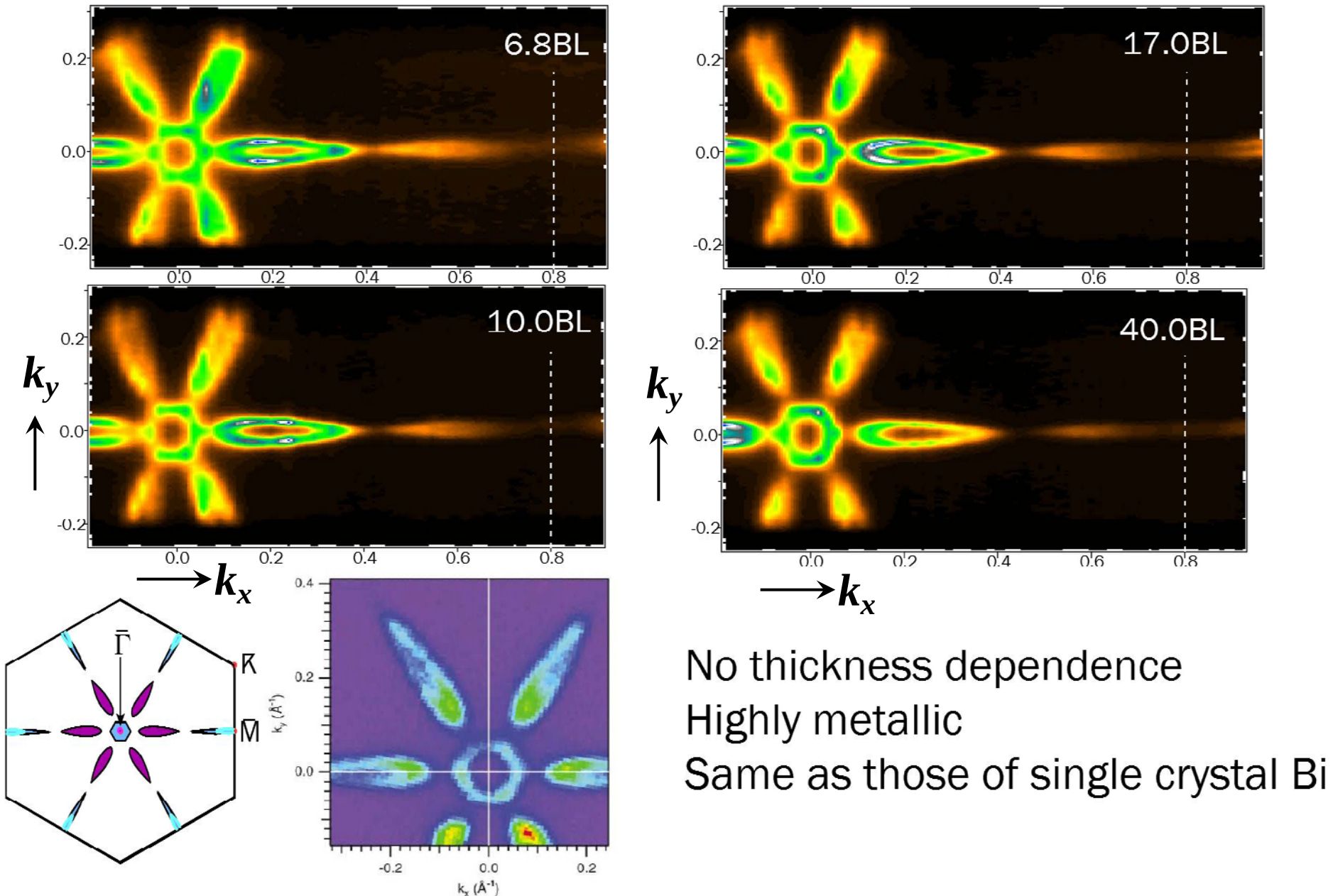
Quantum-Well States
Surface States :



Electrical Cond. Of Bi Film
= Surface-State Conduction



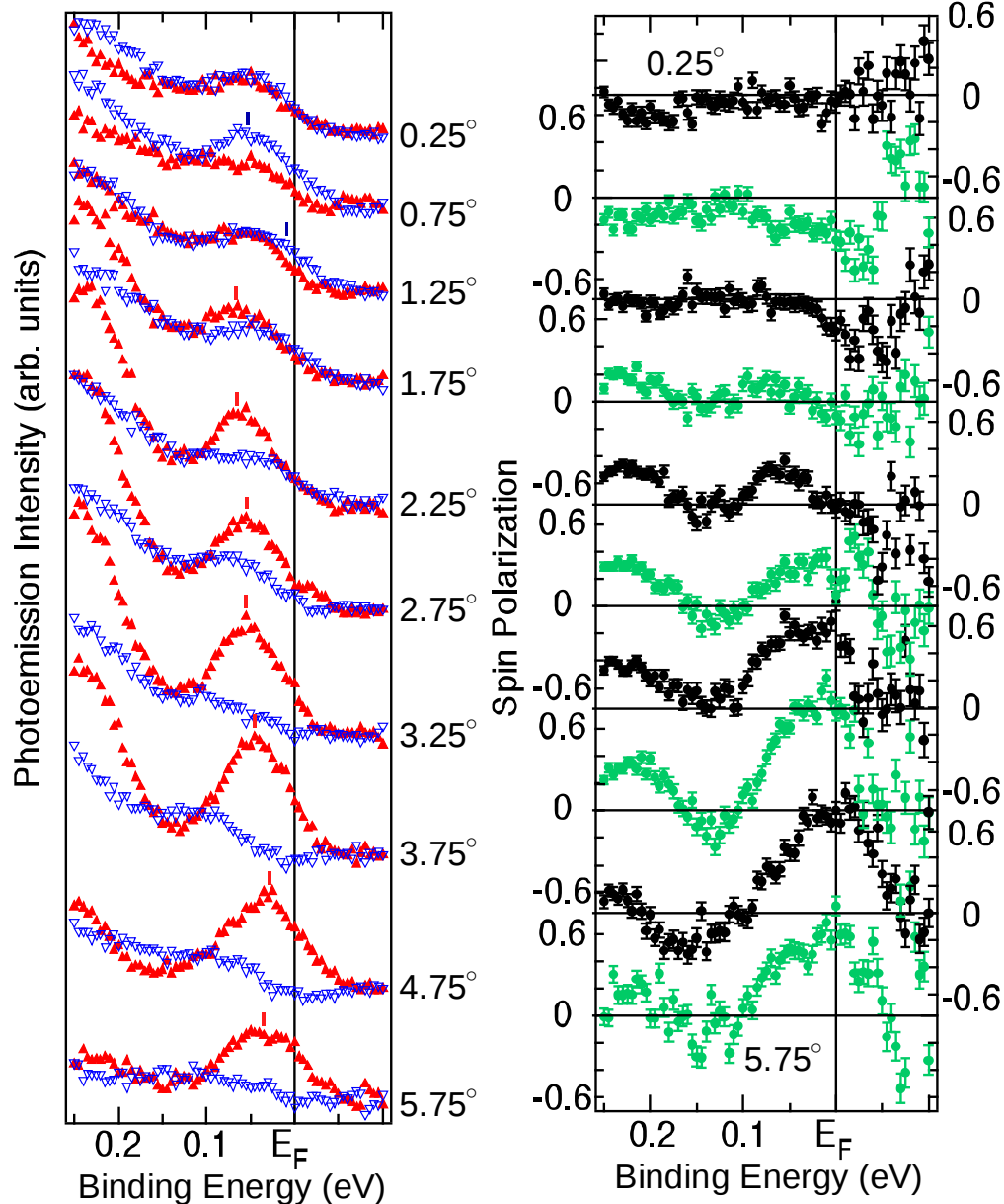
Fermi Surfaces of Bi(001) films



Single Crystal of Bi: C. R. Ast *et al.*, PRL **87** 177602(2001)

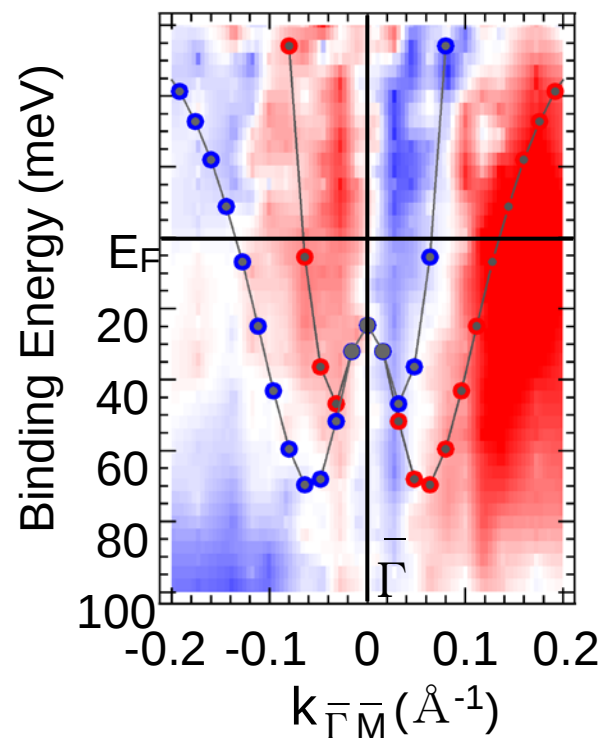
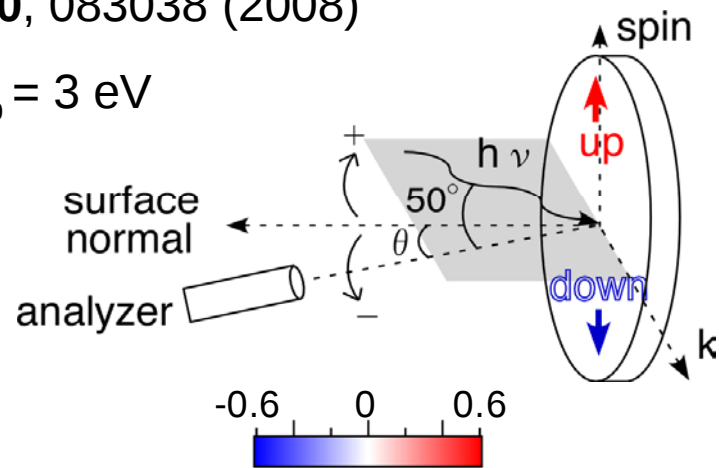
Spin-resolved ARPES

7 BL



T. Hirahara, et al., New J. Phys.
10, 083038 (2008)

$E_p = 3$ eV

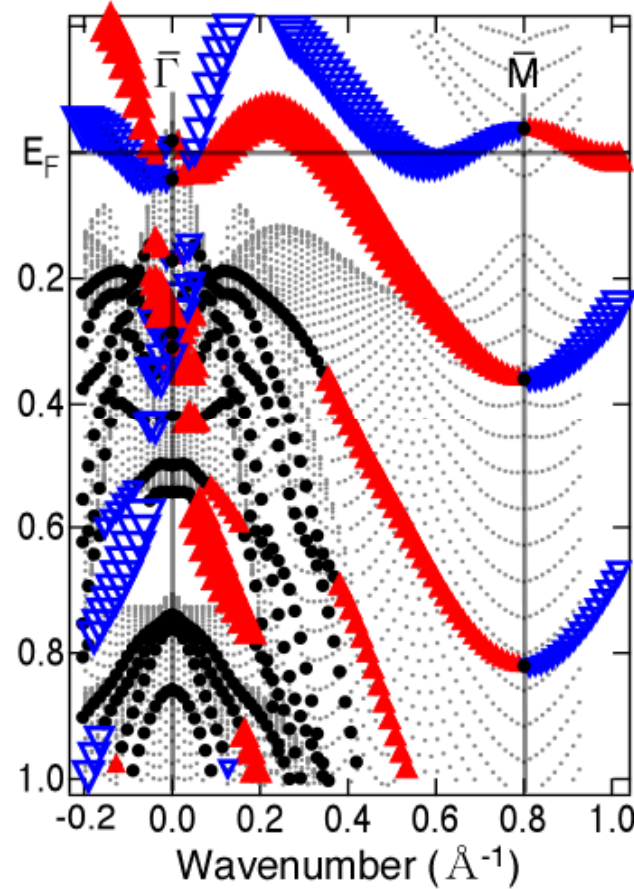
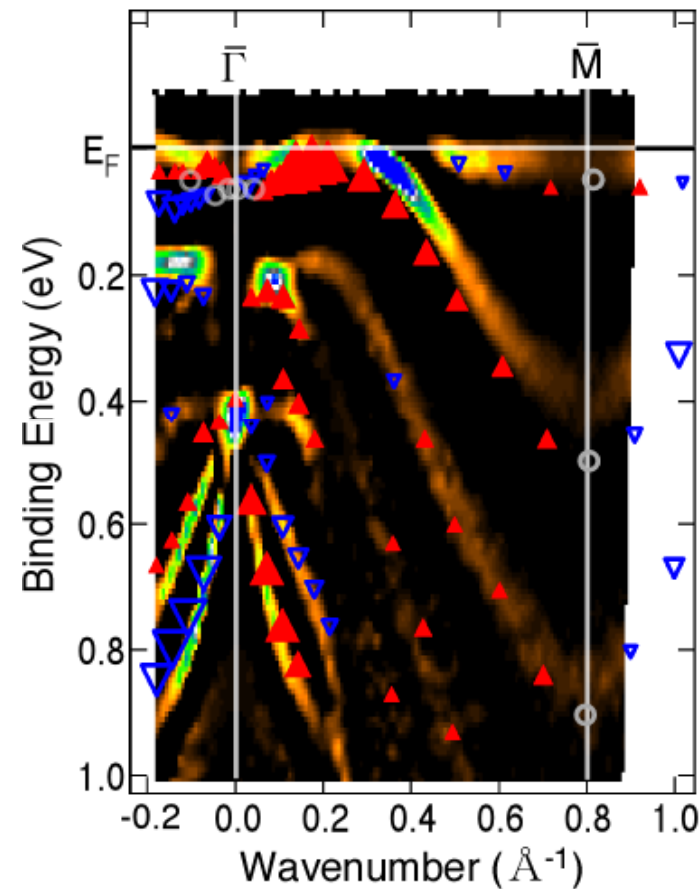


Consistent with the Rashba model

Spin-resolved band mapping

7 BL experiment

7 BL calculation (free-standing Bi slabs)



Size of the markers

||

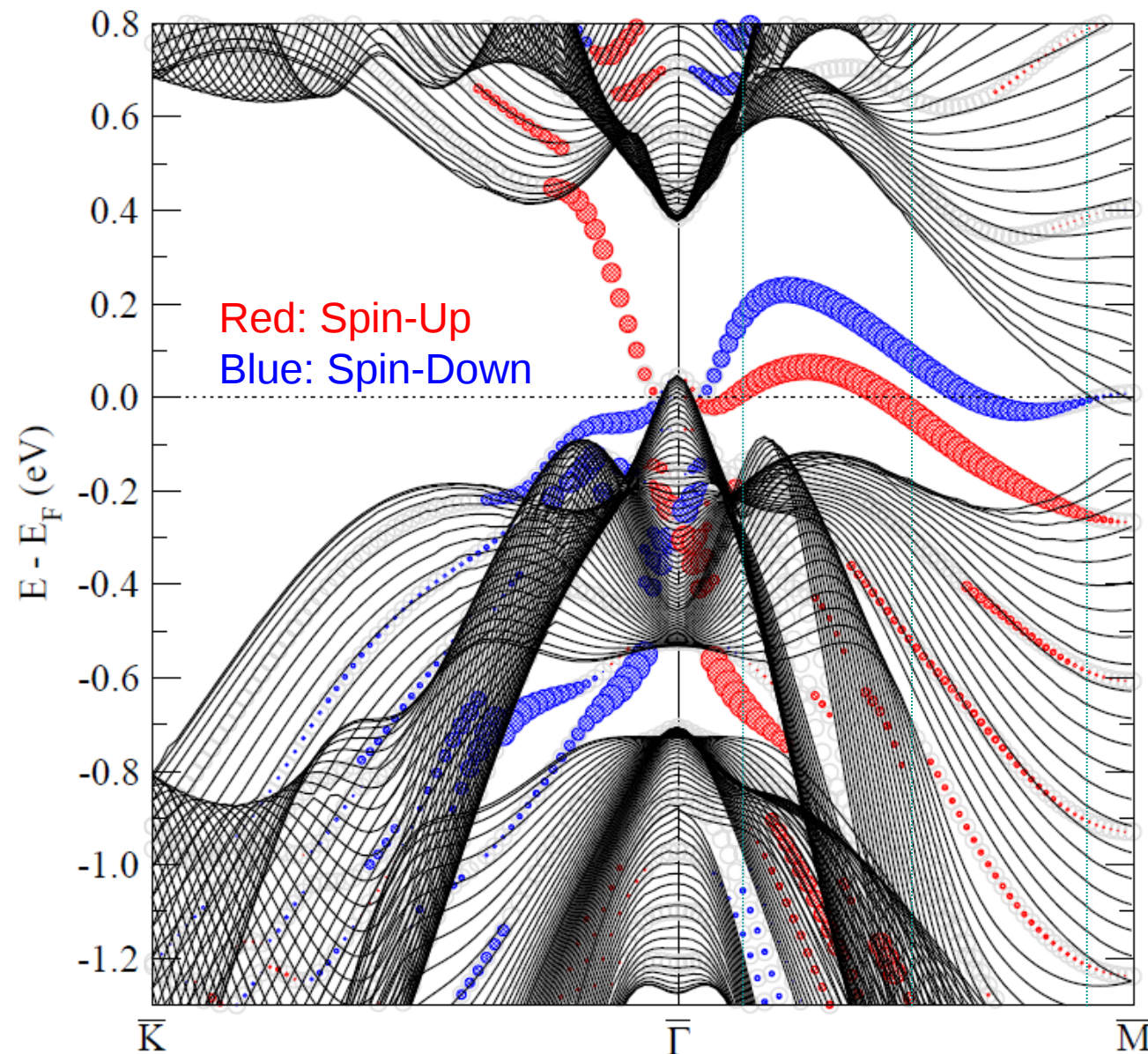
Magnitude of the
spin polarization

Asymmetric spin
structure with
respect to $\bar{\Gamma}$ and $\bar{M}$

Qualitative consistency between experiment and calculation concerning the k-dependence of the spin polarization

Dispersion of a symmetric 10BL Bi slab

Bihlmayer
(Jülich, Germany)



vacuum

Bi

vacuum

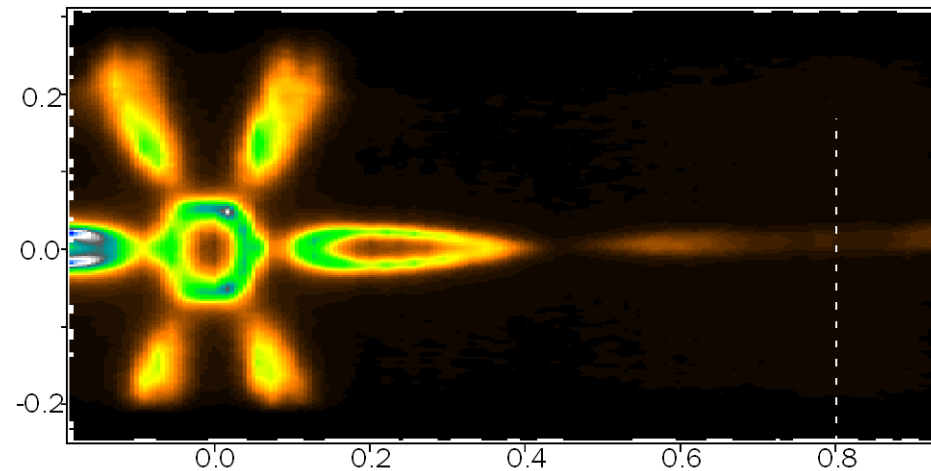
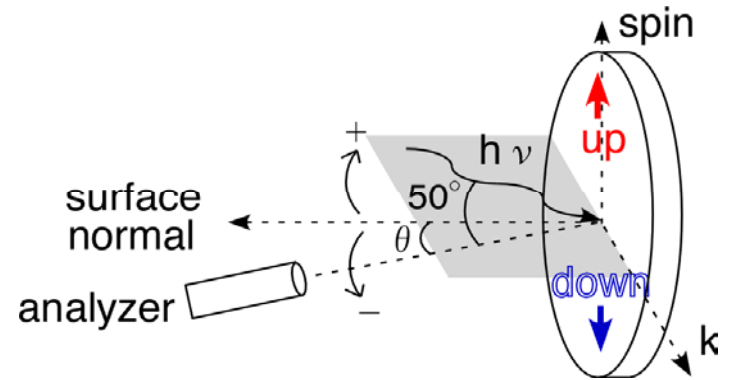
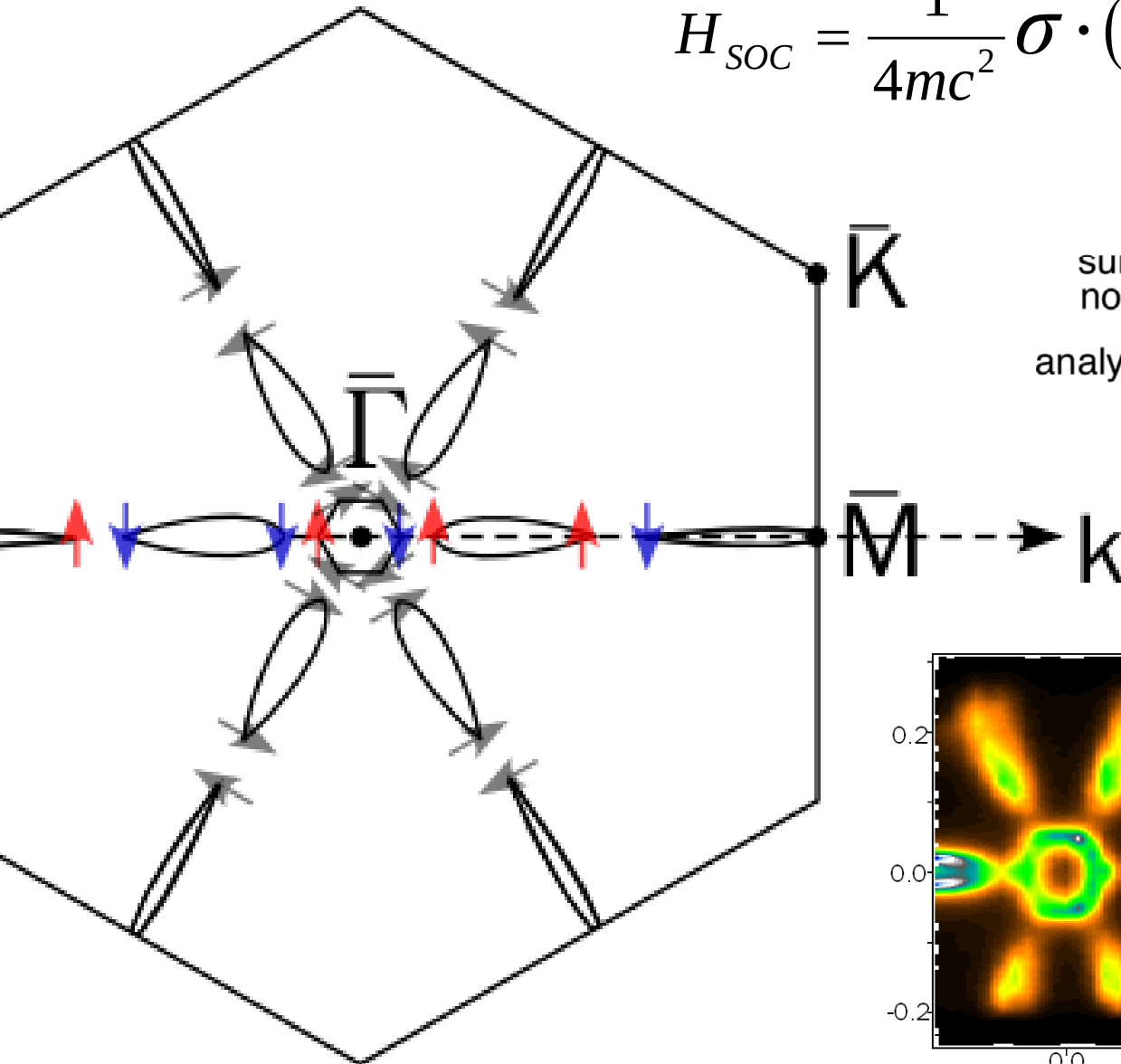
First-principles calculation
for free-standing Bi slabs
including SOC

Pure Bi

- Semi-metal in Bulk
- Conduction band and valence band are connected by the spin-split surface states

Spin-Texture Structure in Fermi Surface

$$H_{soc} = \frac{1}{4mc^2} \boldsymbol{\sigma} \cdot (\text{grad}V(x) \times p)$$



Various Surface States

1. Shockley states (extended)

Tamm states (localized)

Chemical bonding, Potential
(Previous slide)

2. Image states

Image charge

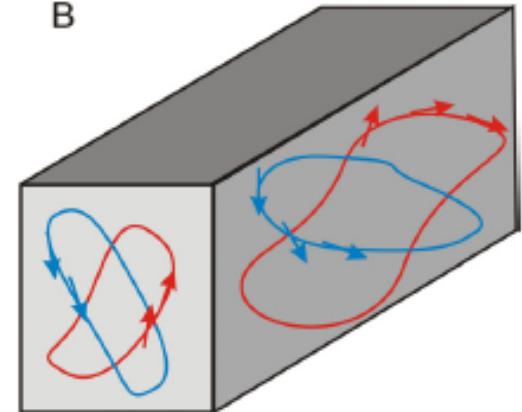
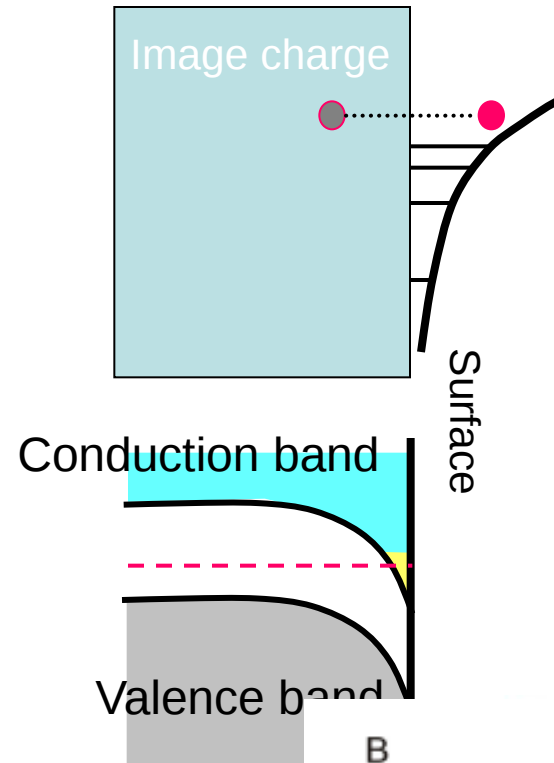
3. Surface space-charge layer

Bending of bulk bands

4. Topological surface states

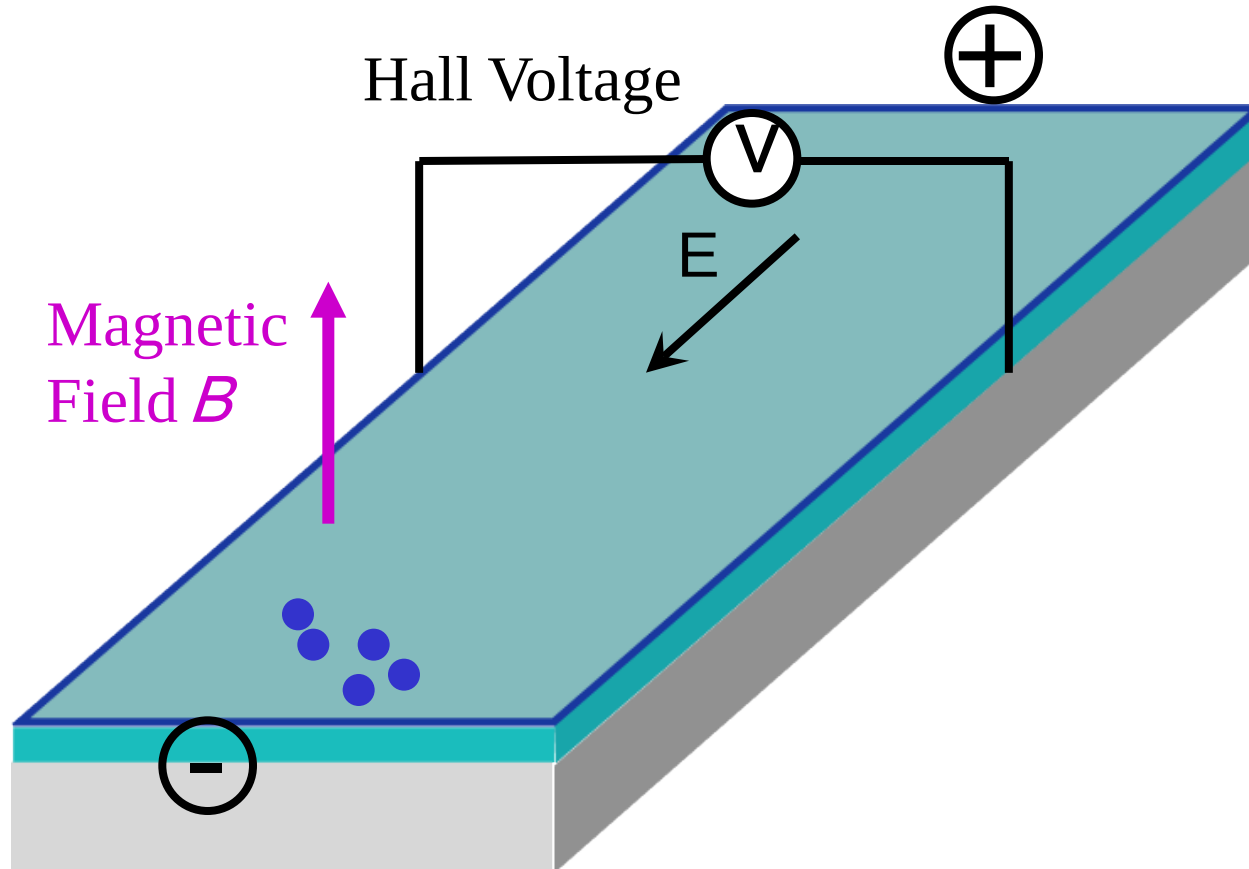
Spin-orbit coupling ← Edge states of Q(S)H phase

HgTe (QW), $\text{Bi}_{1-x}\text{Sb}_x$, Bi_2Te_3 , Bi_2Se_3 ,



Hall Effect

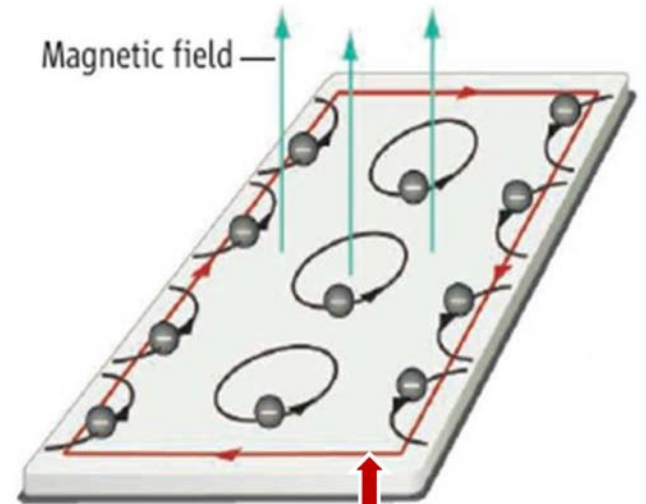
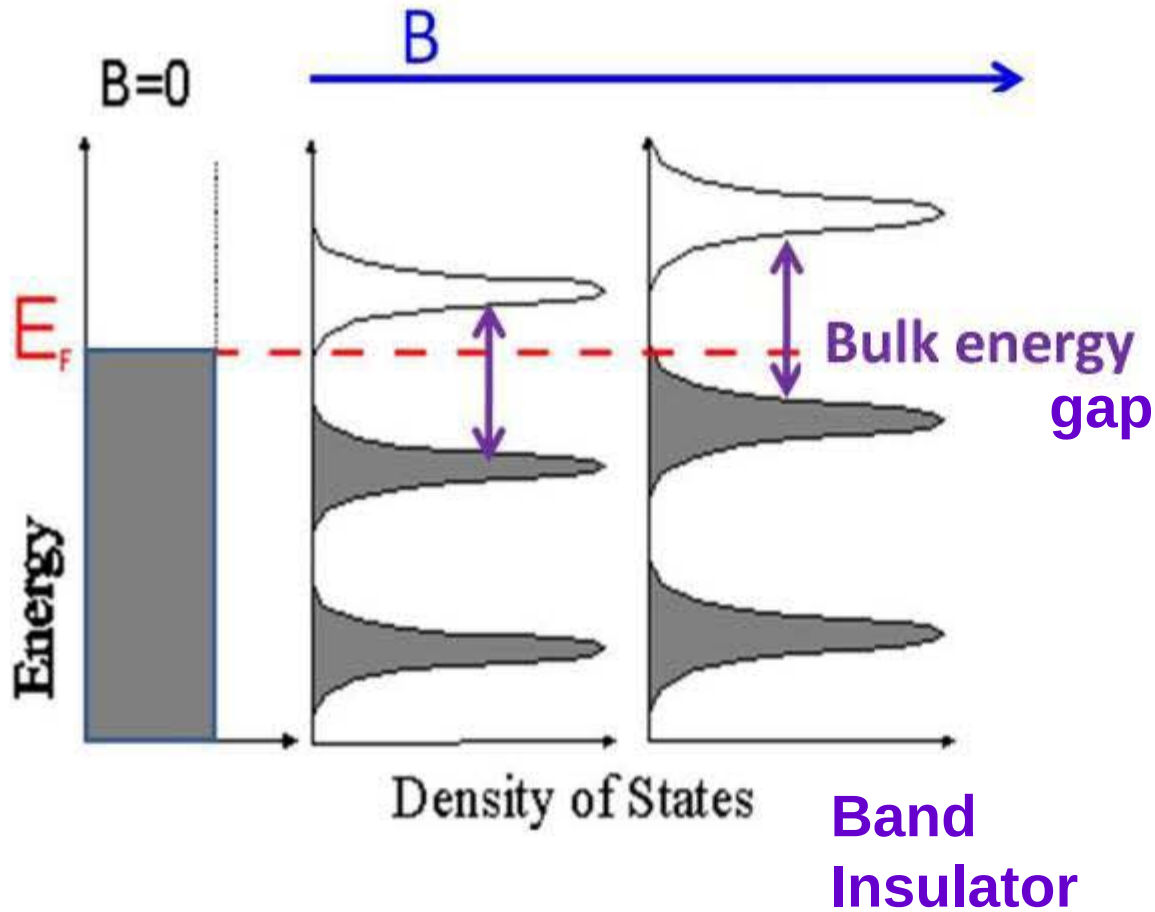
Edwin H. Hall (1879)



Hall Effect at high magnetic fields

Electrons + strong magnetic field

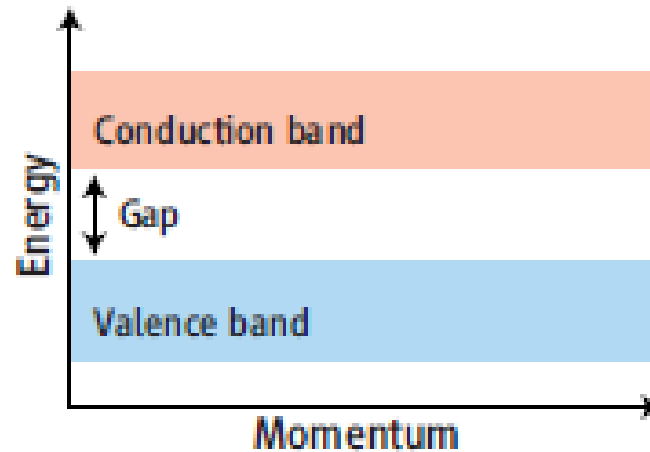
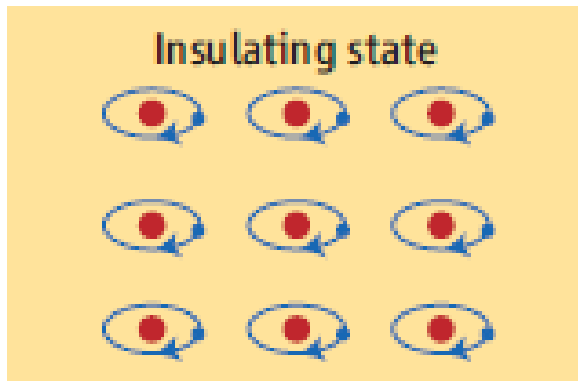
→ Discrete Energy Levels
Landau Levels



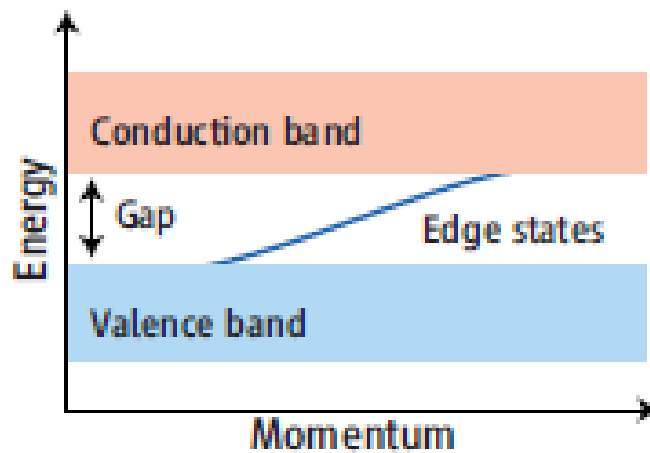
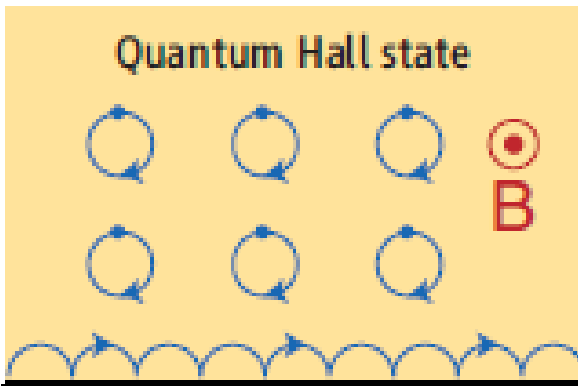
Conduction through
the boundary

→ Metallic edge state

Usual Band Insulator



Quantum Hall State



Spin Hall Effect

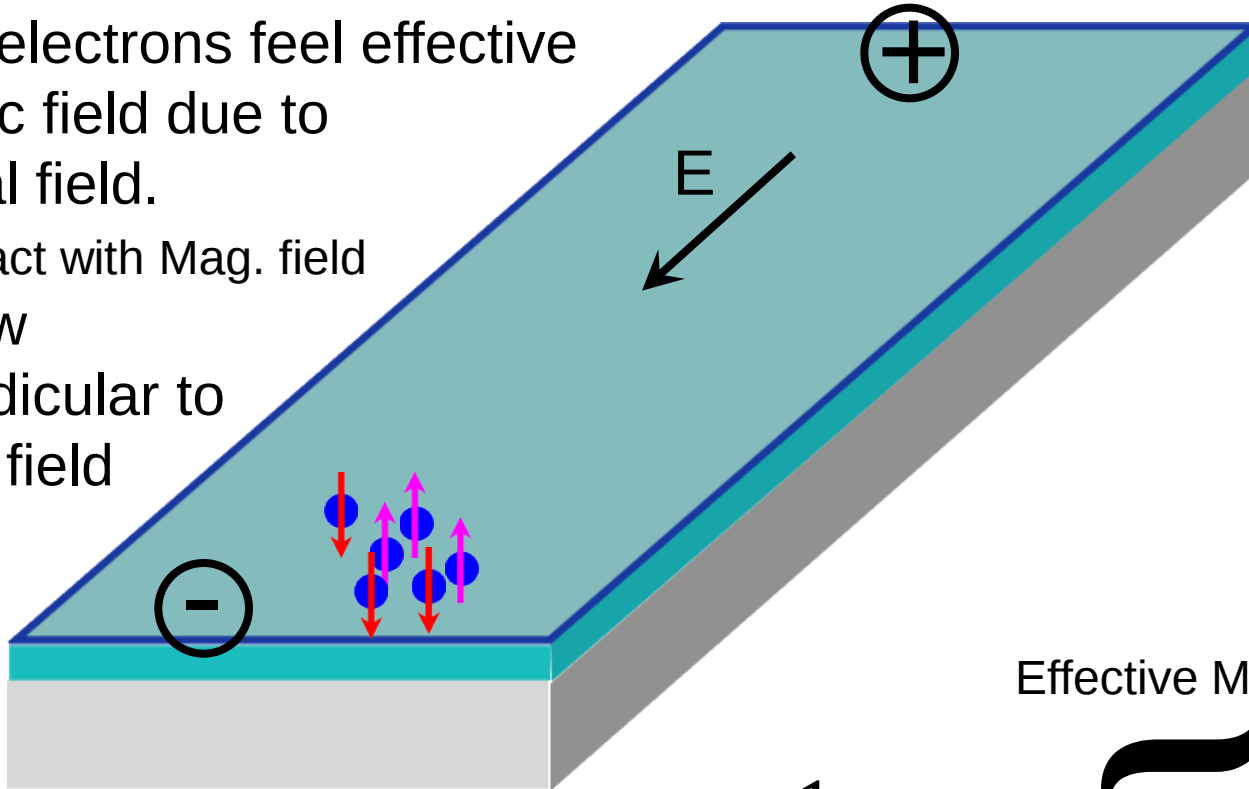
Without external magnetic field
Non-magnetic materials

Spin-Orbit Interaction

⇒ Moving electrons feel effective magnetic field due to electrical field.

⇒ Spin interact with Mag. field

⇒ Spin flow perpendicular to electric field

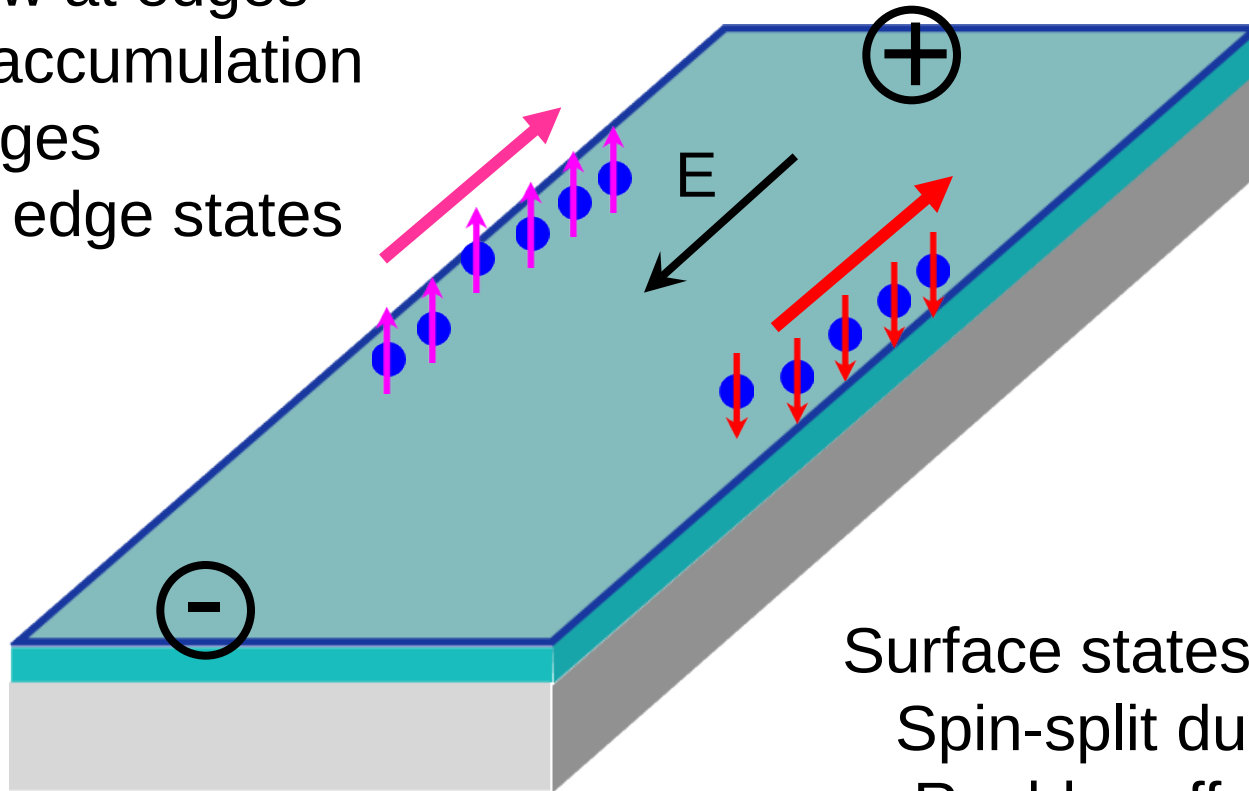


Effective Magnetic Field

$$H_{soc} = \frac{1}{4mc^2} \boldsymbol{\sigma} \cdot \overbrace{\text{grad} V(x)}^{\text{Effective Magnetic Field}} \times \mathbf{p}$$

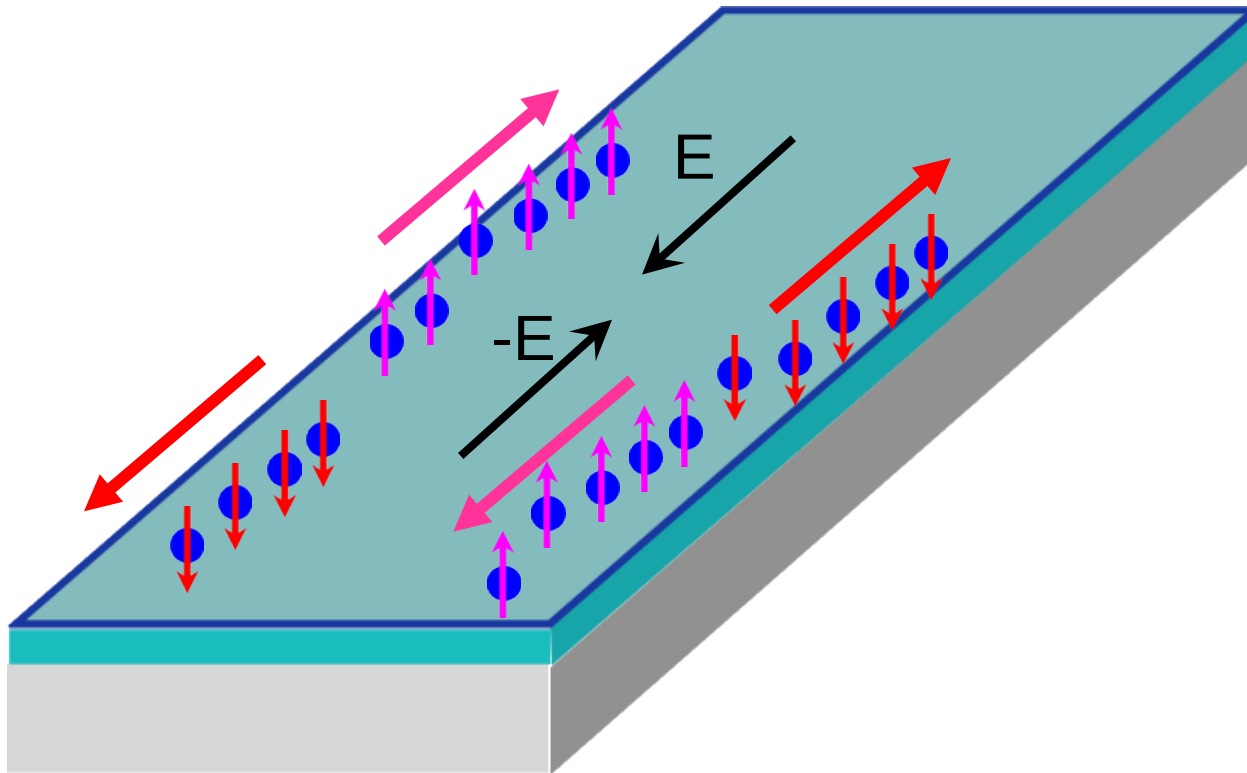
Spin Hall Effect

Spin flow at edges
⇒ Spin accumulation
at edges
⇒ chiral edge states



Surface states :
Spin-split due to
Rashba effect or
Topological insulators

Spin Current flowing at Edges

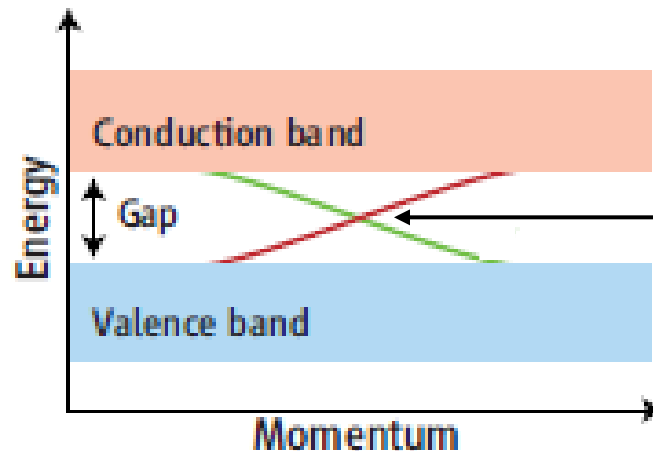
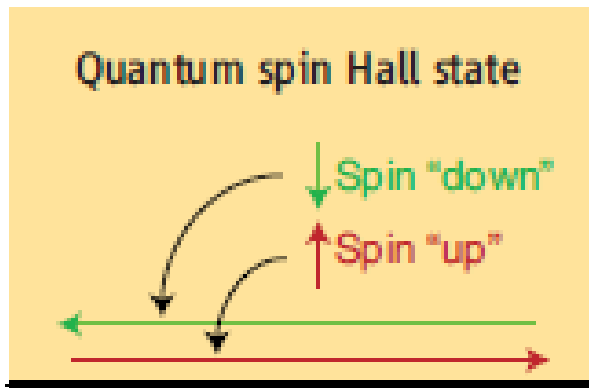


Quantum (Spin) Hall State Without Magnetic Field!

Spin-Orbit Interaction

→ **Electric field = Effective magnetic field**
for moving electrons

{ **Bulk; insulator**
Surface; Spin-split metal (Kramers degeneracy is lifted)
Spin flow

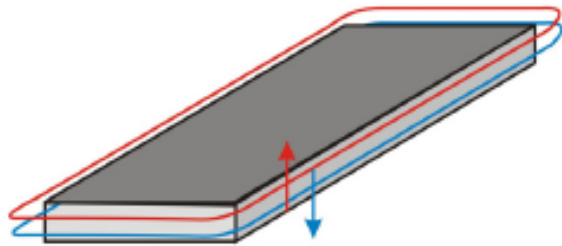


(Chiral) Dirac Fermion

Bulk; insulator
Surface; (Topologically protected)

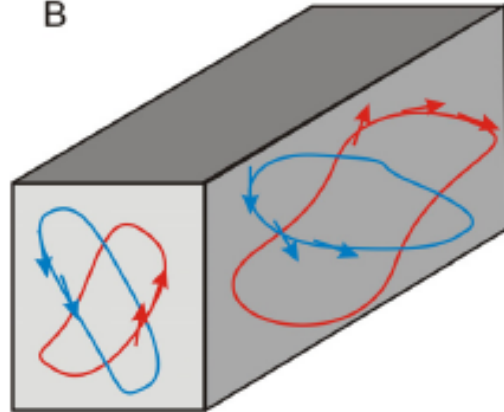
Quantum spin Hall phases and topological insulators

A



2D QSH phase

B



3D topological insulators

- bulk = gapped

- **Gapless edge states**

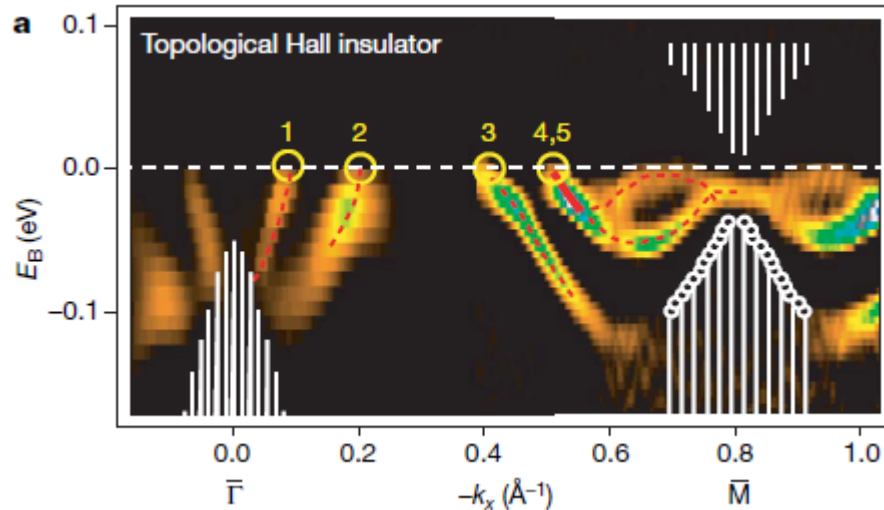
Spin-orbit coupling

- Carry spin current
- Robust against weak non-magnetic impurities or interaction

(**topological metal**)

(S)ARPES

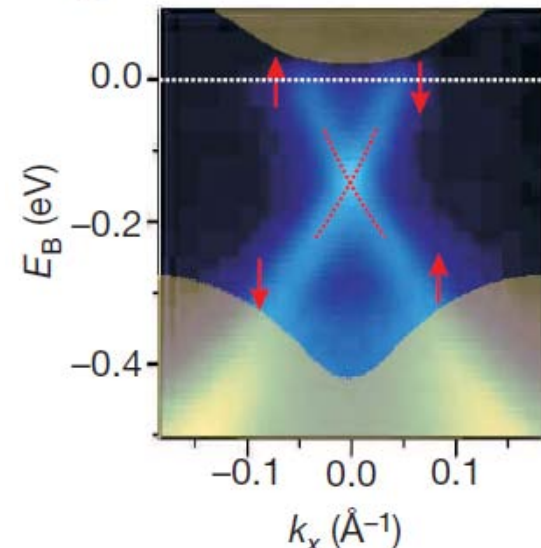
$\text{Bi}_{1-x}\text{Sb}_x$ ($0.07 < x < 0.22$)



D. Hsieh *et al.*, Nature **454**, 970 (2008)

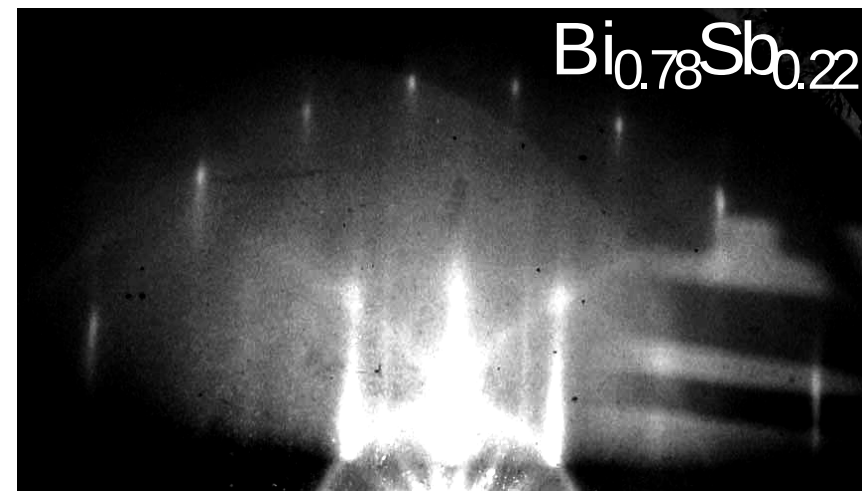
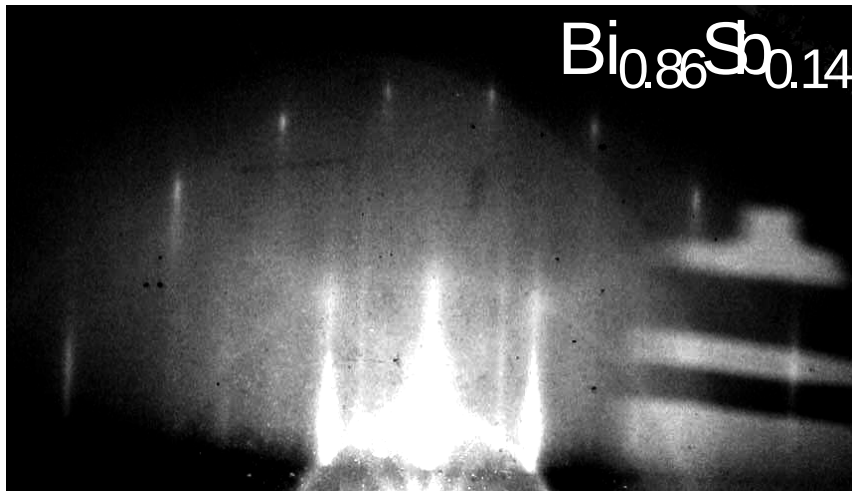
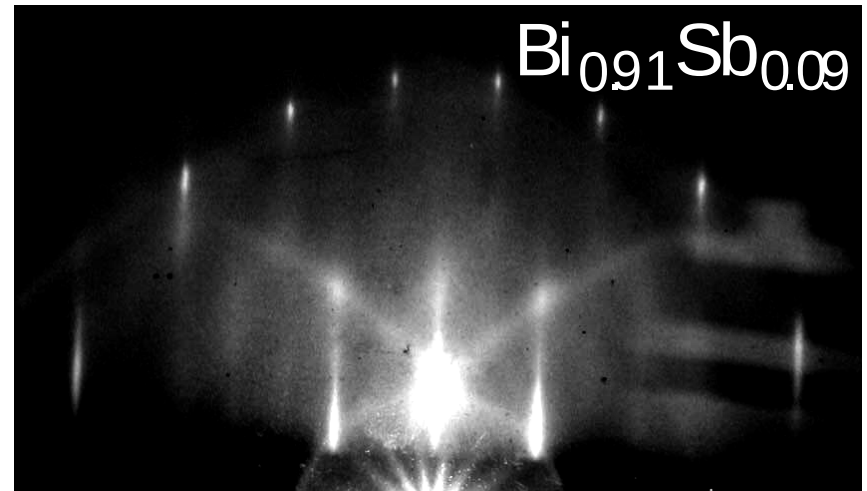
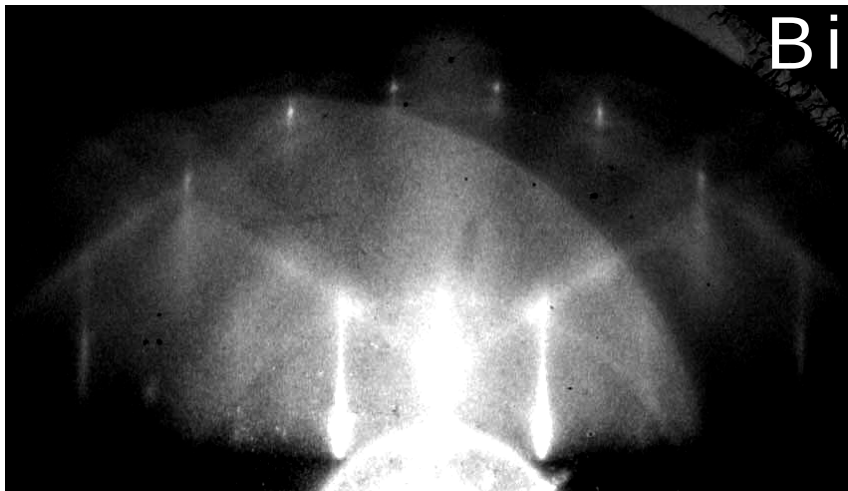
c

Bi_2Se_3



D. Hsieh *et al.*, Nature **470**, 1101 (2009)

Co-deposition of Bi & Sb on Si(111)-7x7 at RT: RHEED observation

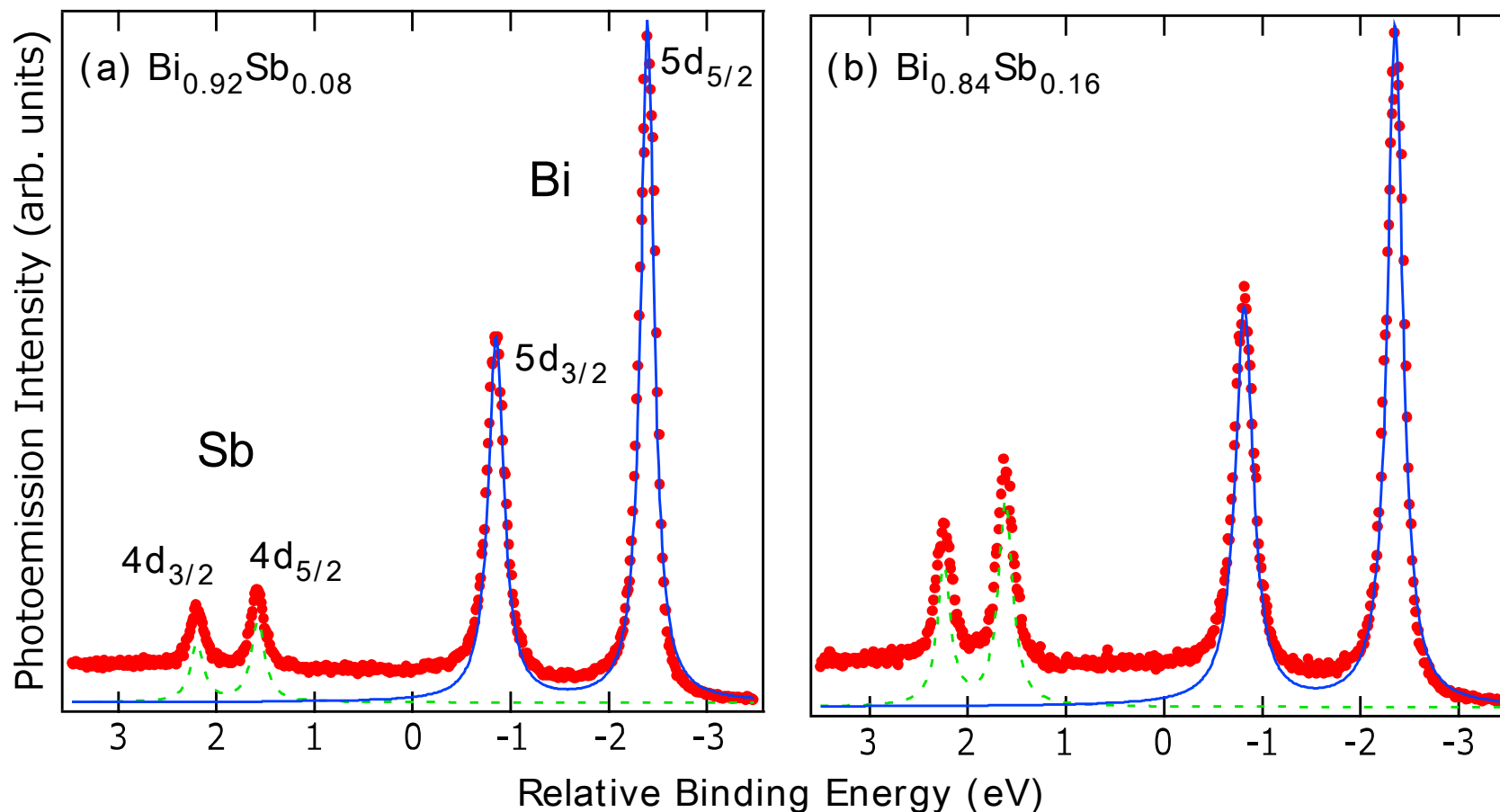


30 Å (7 BL) ultrathin film

- Sharp spots of 1x1 periodicity(001)
- Kikuchi pattern

Stoichiometry estimation by CLS

$h\nu = 80 \text{ eV}$



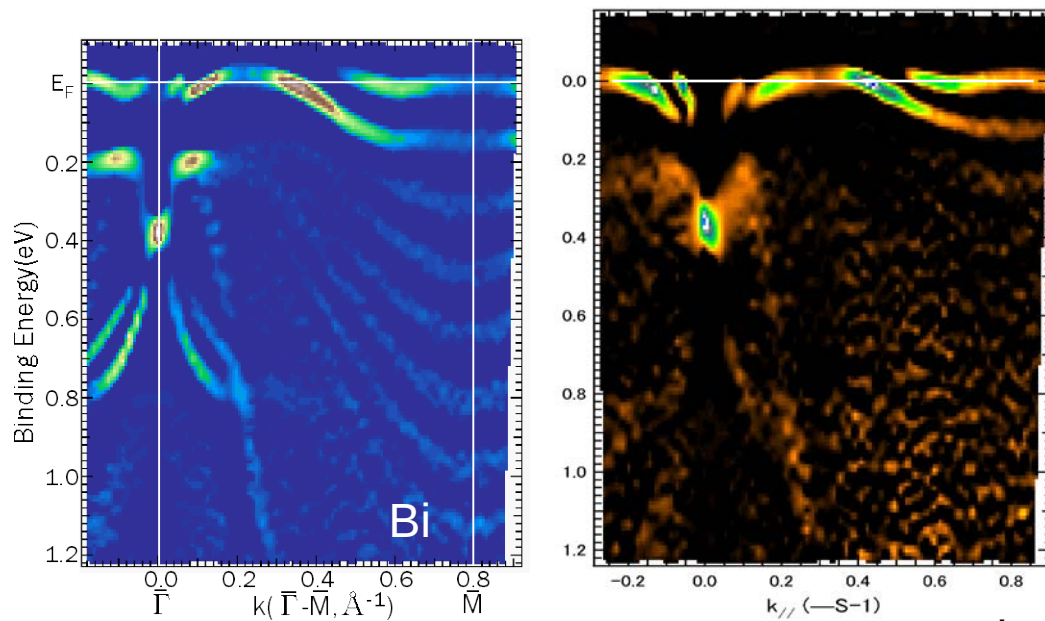
$$\frac{\rho_{\text{Bi}}}{\rho_{\text{Sb}}} = \frac{I_{\text{Bi}}}{I_{\text{Sb}}} \cdot \frac{S_{\text{Sb}}}{S_{\text{Bi}}} \sim 11.4 \text{ (Sbが8.8\%)}$$

11.07 15.88

$$\frac{\rho_{\text{Bi}}}{\rho_{\text{Sb}}} \sim 5.4 \text{ (Sbが18.5\%)}$$

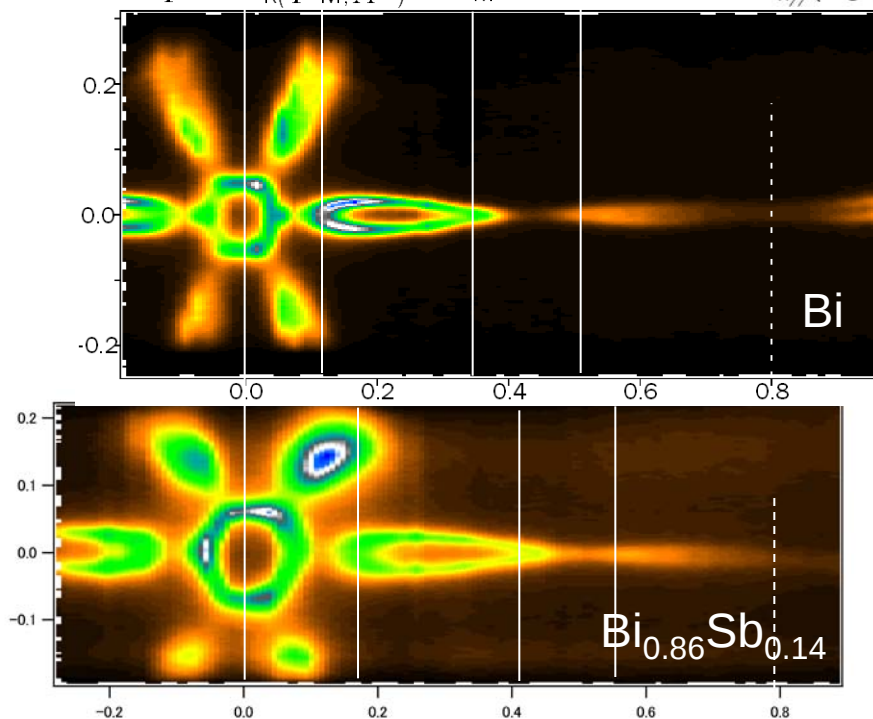
Good match!

Comparison



The surface states at E_F are almost the same between Bi and Bi_{0.86}Sb_{0.14}.

Bi_{0.86}Sb_{0.14}

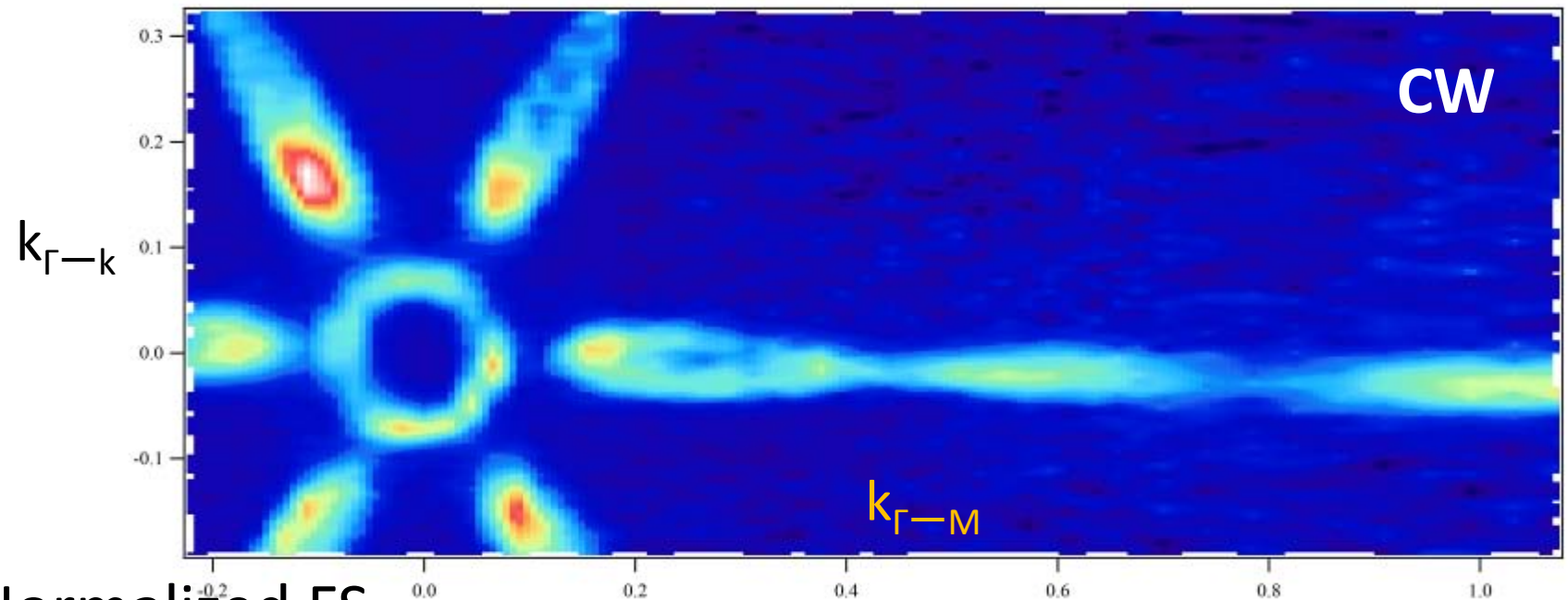
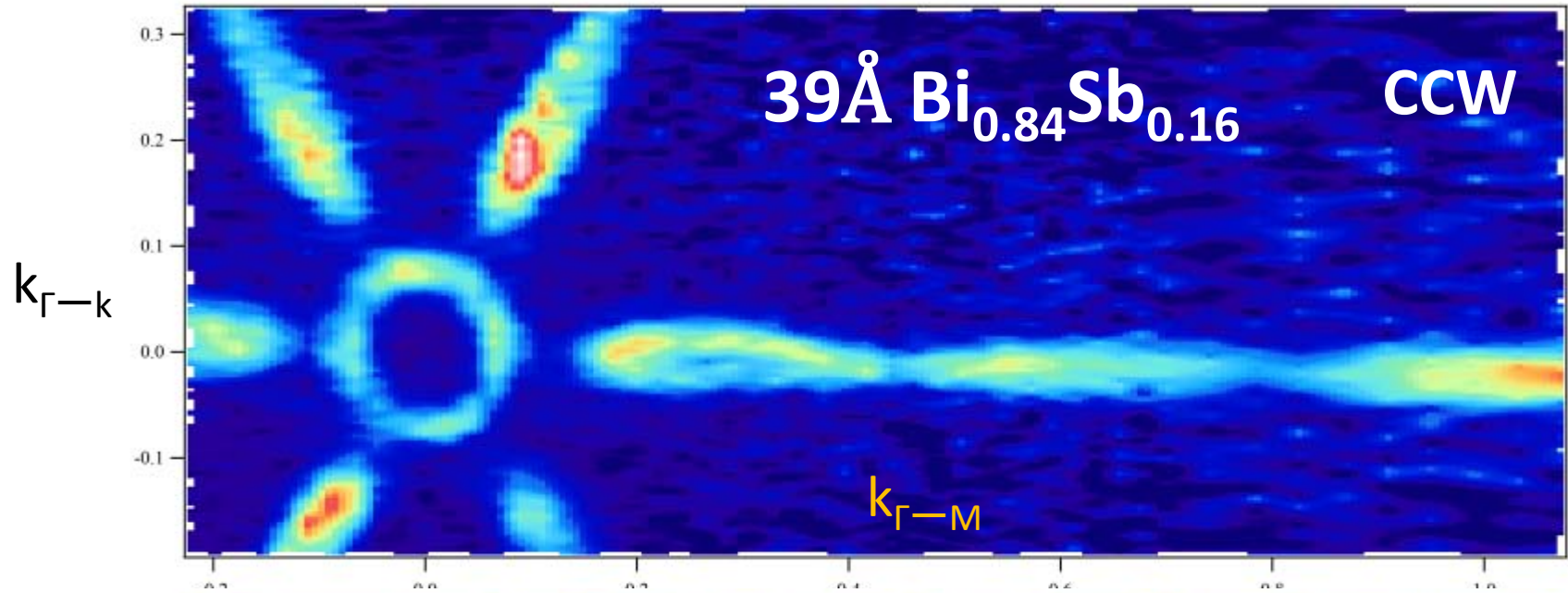


Bi_{0.86}Sb_{0.14} and Bi

Band dispersion
Fermi Surface

} Almost same

Helicity dependence - dichroism effect -



Normalized FS

Resistivity

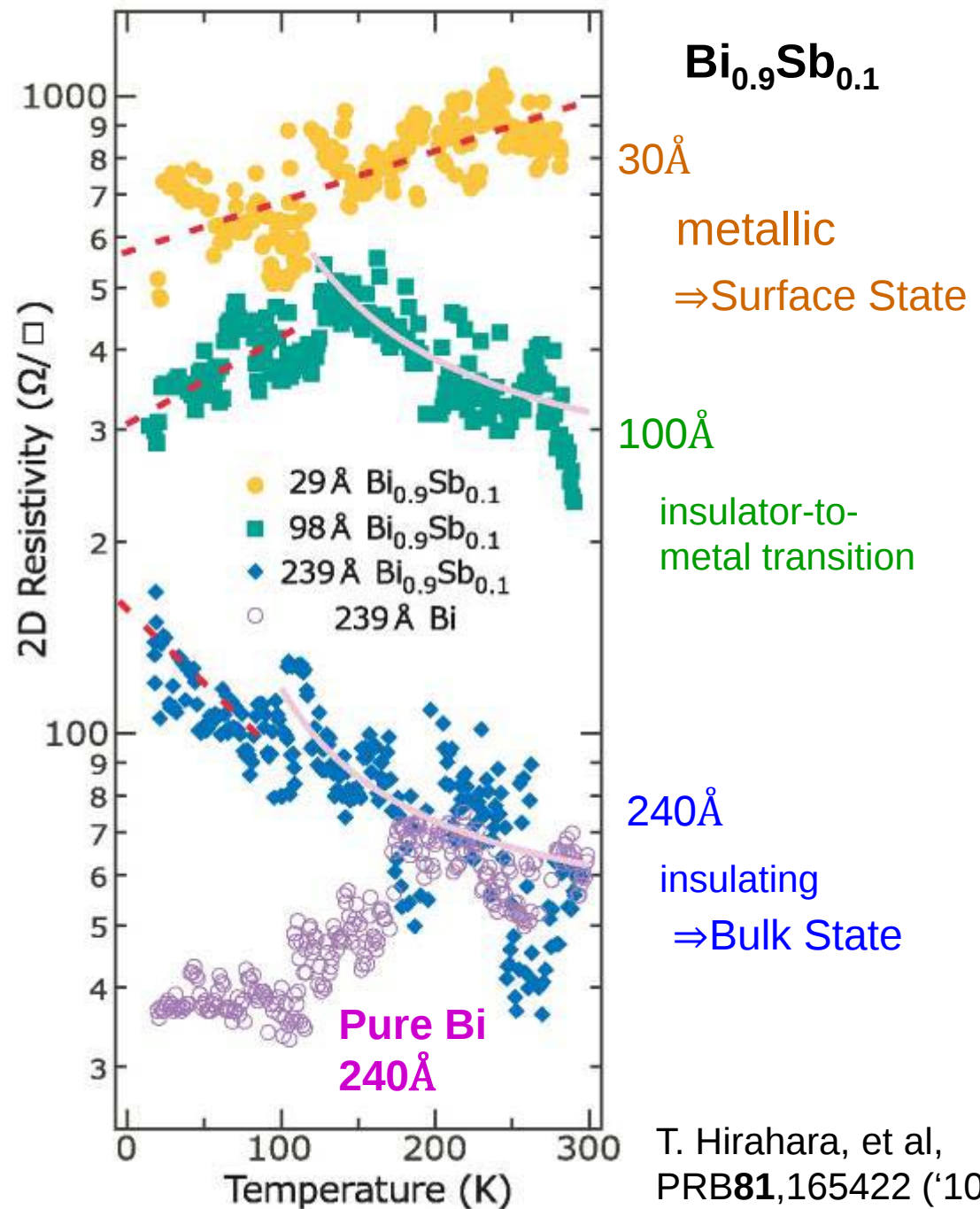
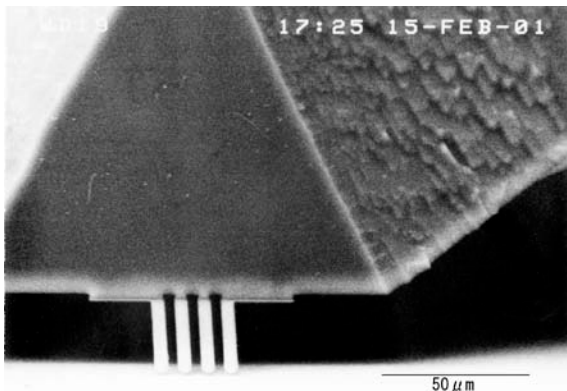
$\text{Bi}_{0.9}\text{Sb}_{0.1}$

The surface is metallic,
while bulk is insulating.

Bi

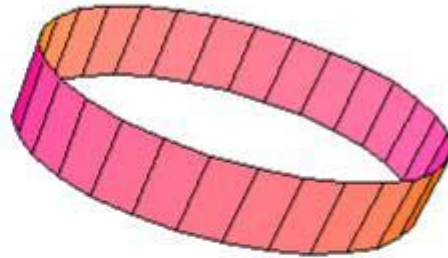
The surface is metallic,
while bulk is (semi)metal.

In situ Micro-Four-Point Probe
Measurement in UHV



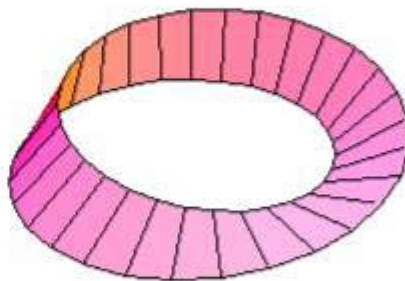
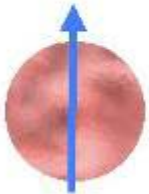
2 π -rotation of spin

Spin=1



$$\psi \xrightarrow{2\pi\text{-rotation}} \psi$$

Spin=1/2

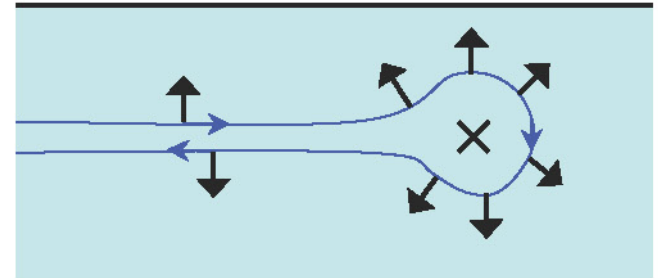


$$\psi \xrightarrow{2\pi\text{-rotation}} -\psi$$

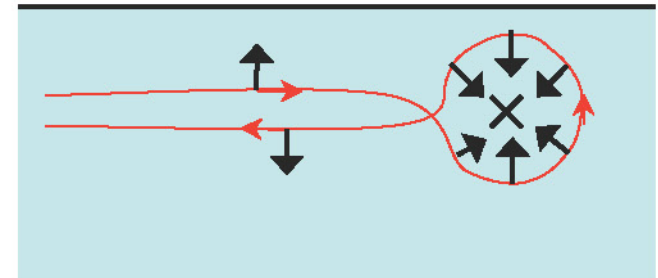
Spinor

Time-Reversal Symmetry

$$E(k, \uparrow) = E(-k, \downarrow)$$



$$\Psi_{\text{initial}} \xrightarrow{\pi\text{-rotation}} \Psi_{\text{scattered1}}$$



$$\Psi_{\text{initial}} \xrightarrow{-\pi\text{-rotation}} \Psi_{\text{scatter2}}$$

$$\Psi_{\text{scatter2}} = -\Psi_{\text{scatter1}}$$

$$\Psi_{\text{scatter1}} + \Psi_{\text{scatter2}} = 0$$

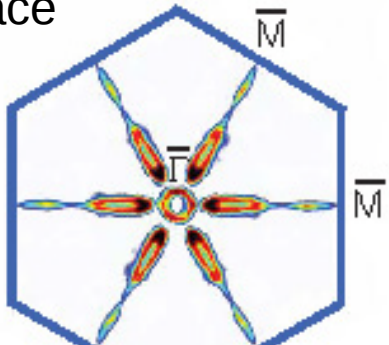
Destructive interference $\Rightarrow$ **No backscattering**

Topological surface states protected from back scattering by chiral spin texture

Yazdani Group, Nature **460**, 1106 (2009)

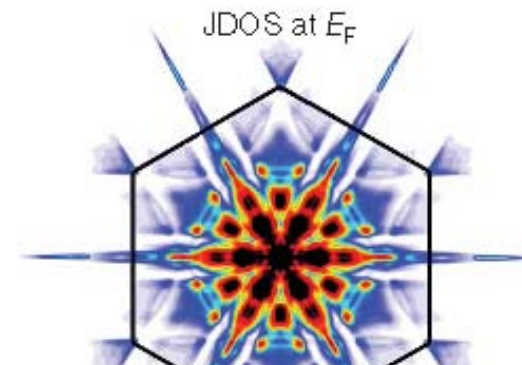
Fermi Surface mapped by ARPES

$I(k)$



calculate

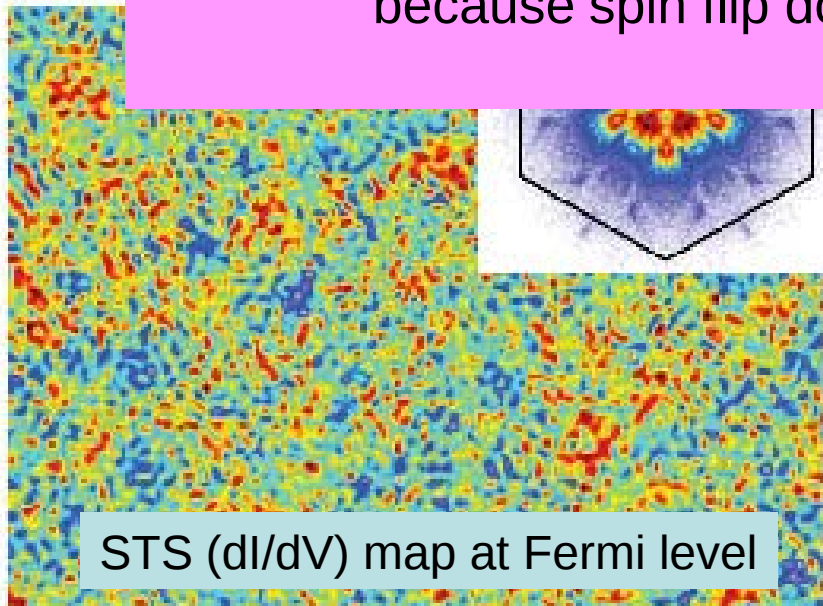
$JDOS(q)$



Back scattering of surface-state electrons are suppressed because spin flip does not occur at scattering.

ent

b



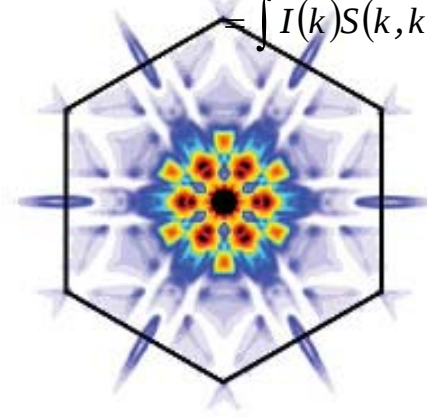
FT pattern

Good match

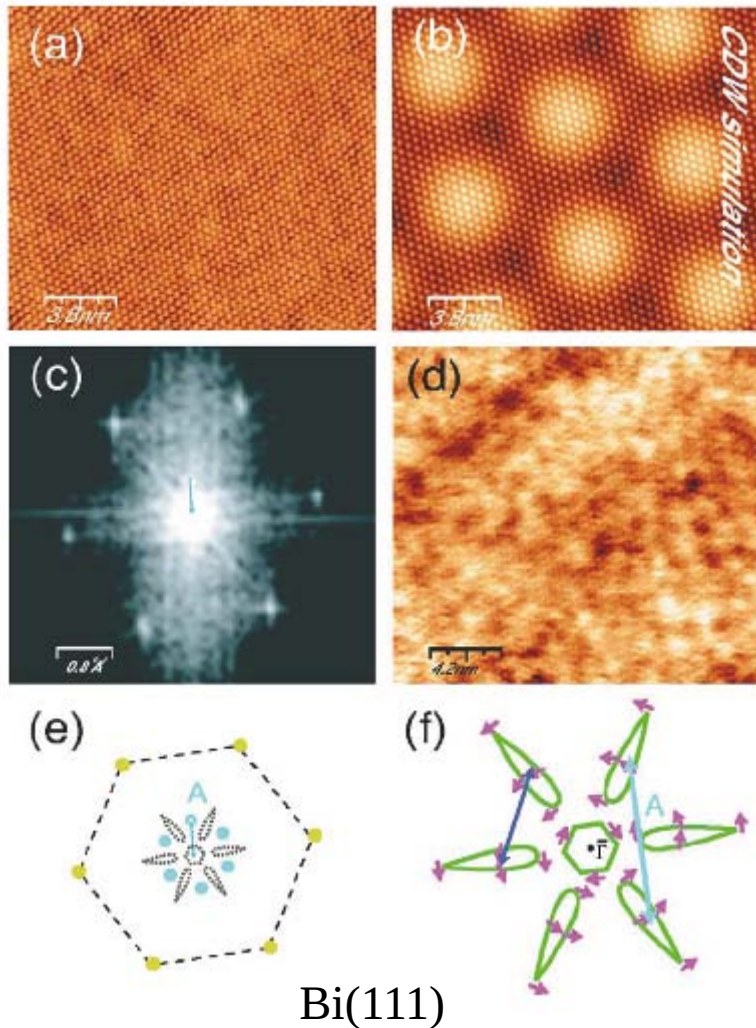
c

$SJDOS(q)$

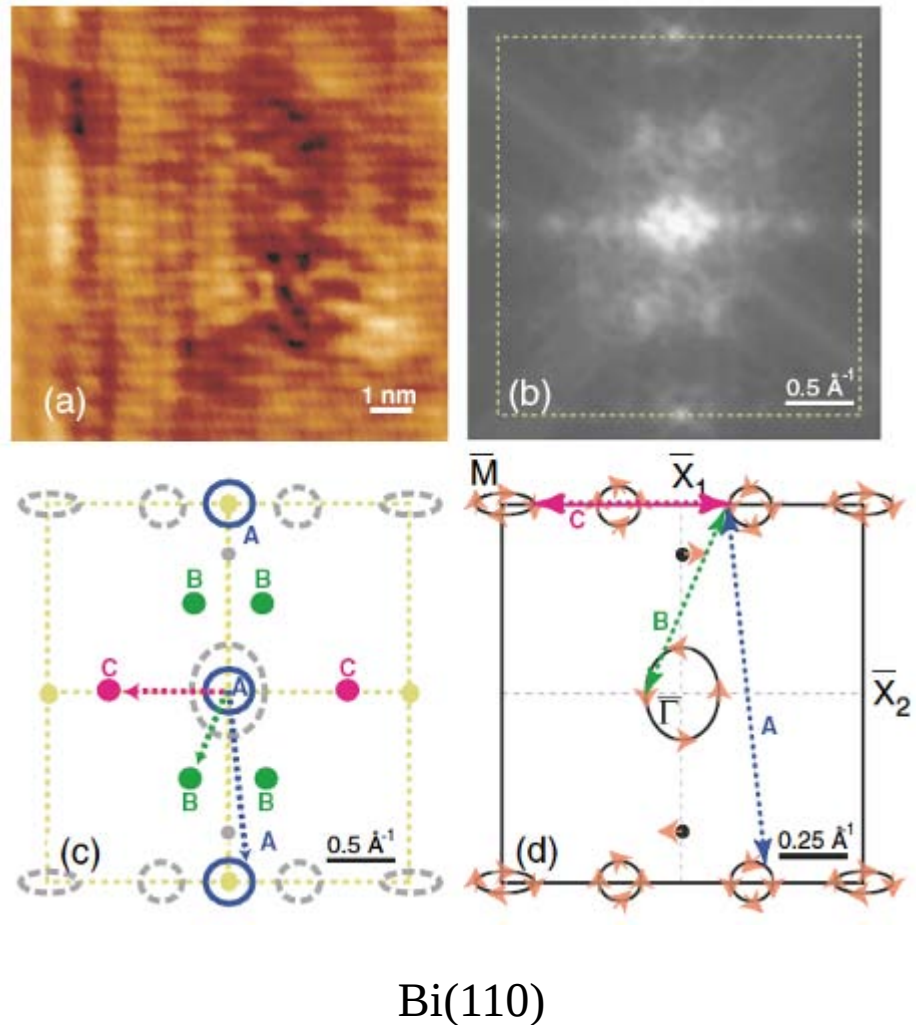
$$= \int I(k) S(k, k+q) I(k+q) d^2k$$



Role of spin in quasiparticle interference on Bi Surface



T. K. Kim *et al.*, PRB **72**, 085440(2005).

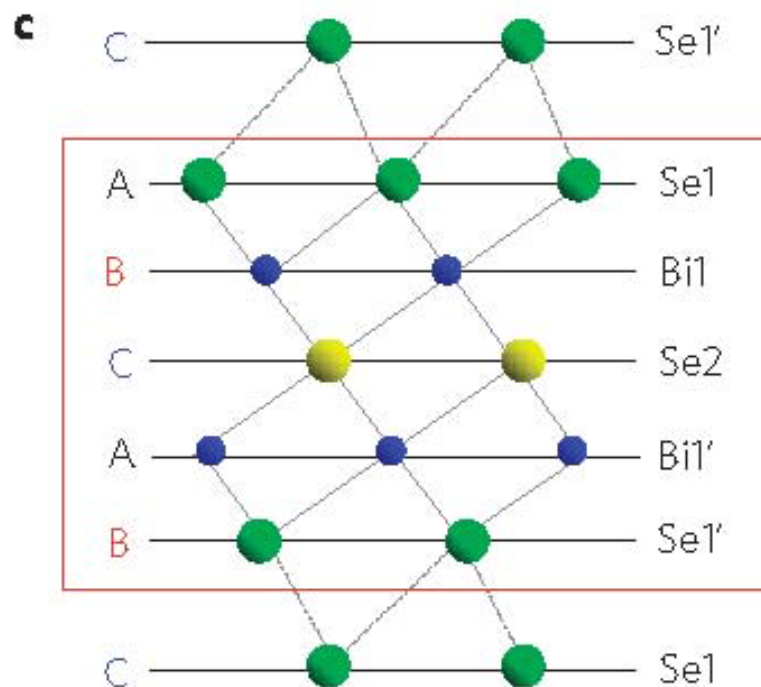
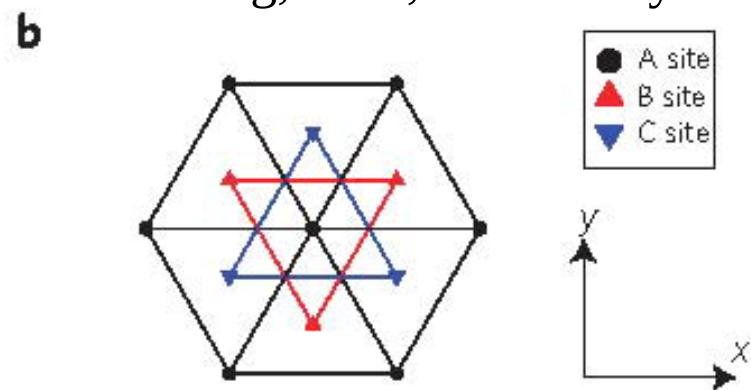
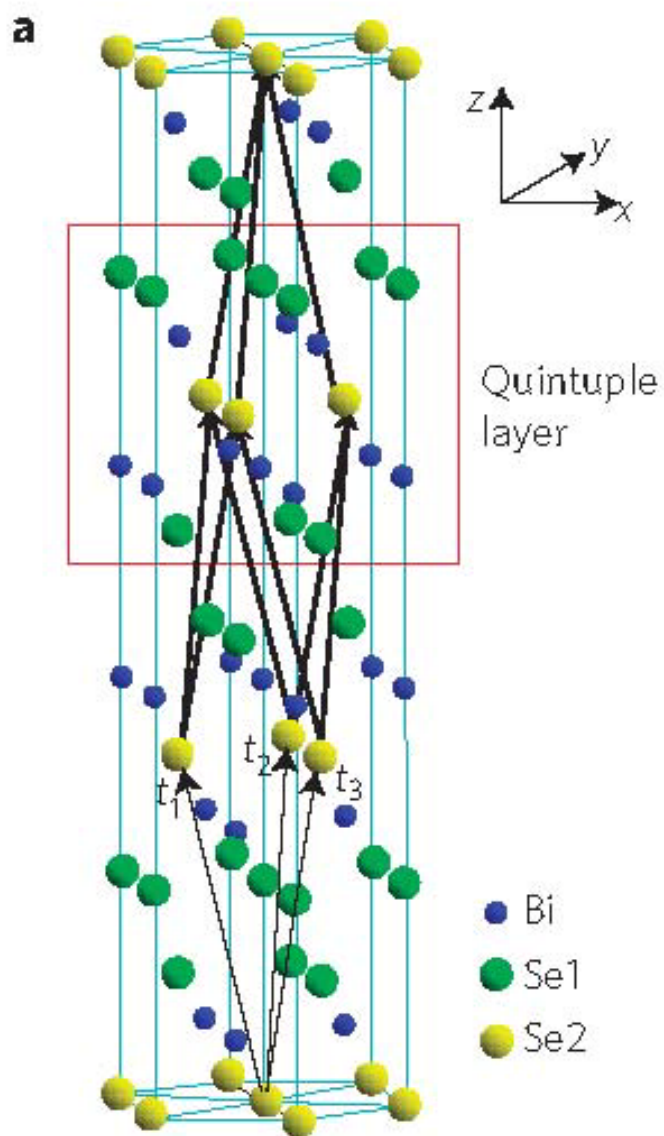


J. I. Pascual *et al.*, PRL **93**, 196802(2004).

Spin-conserving scattering process

Crystal Structure of Bi_2Se_3

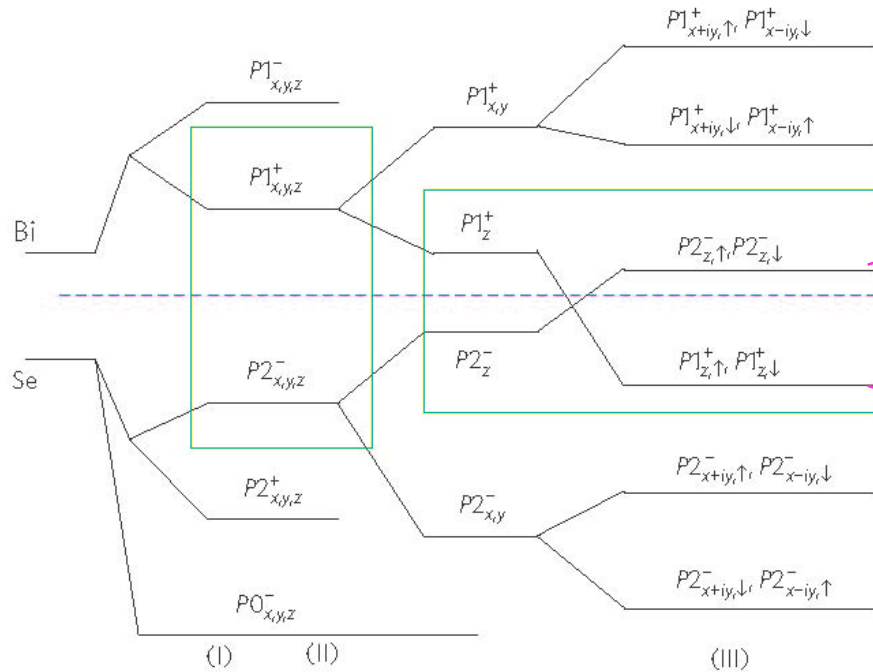
H. Zhang, et al., Nature Physics (May 2009)



Electronic Structure of Bi_2Se_3 (Theory)

H. Zhang, et al., Nature Physics (May 2009)

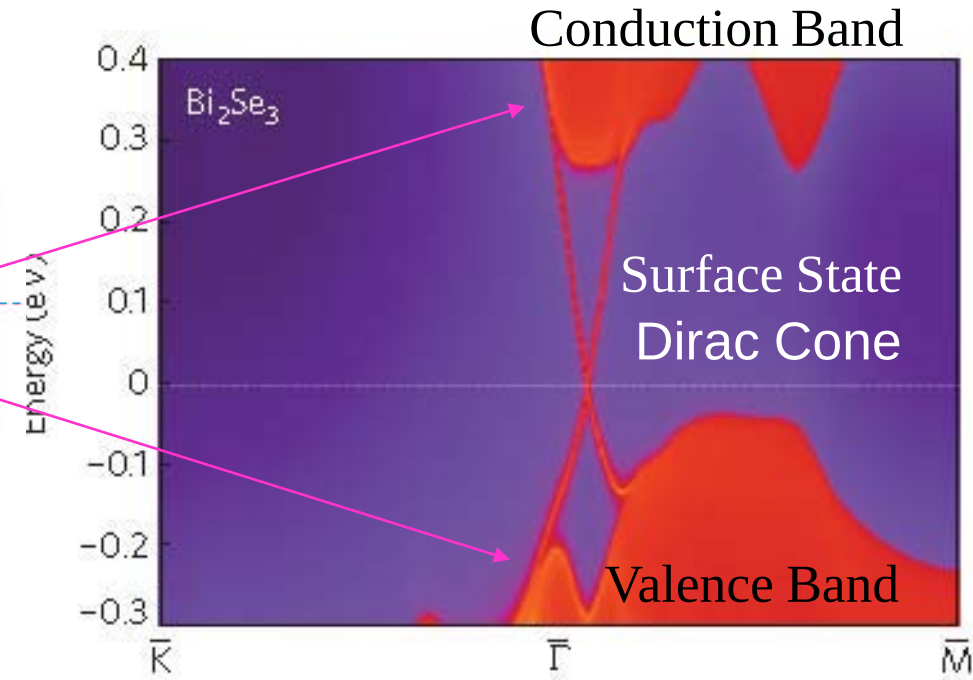
a



Isolated
Atoms
(Atomic
Orbital)

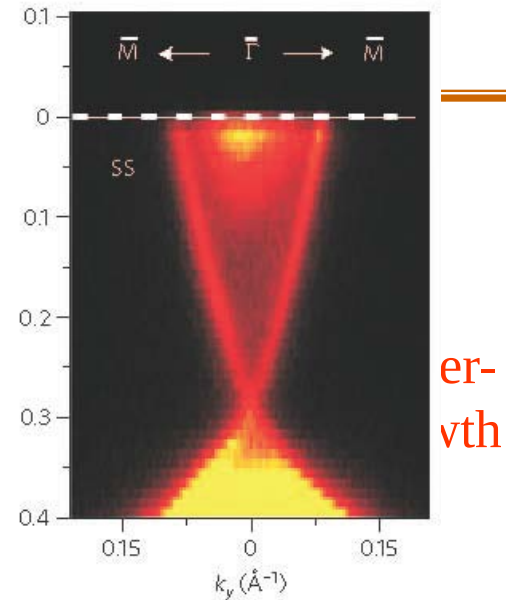
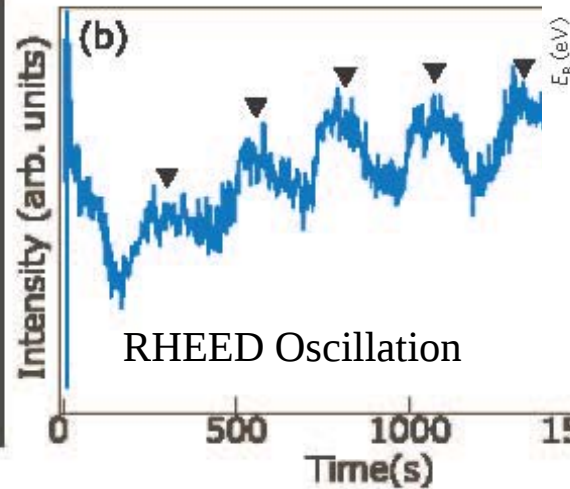
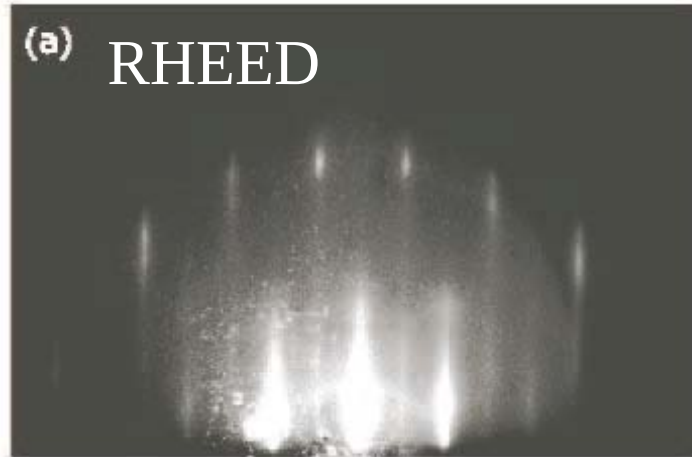
Atomic Bondings
Split due to
Crystal Field

Spin-Orbit
Intercation

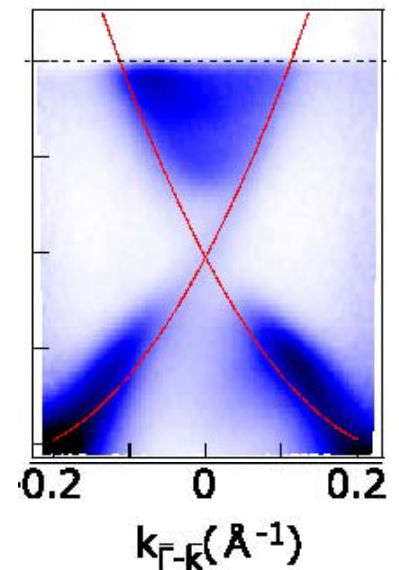
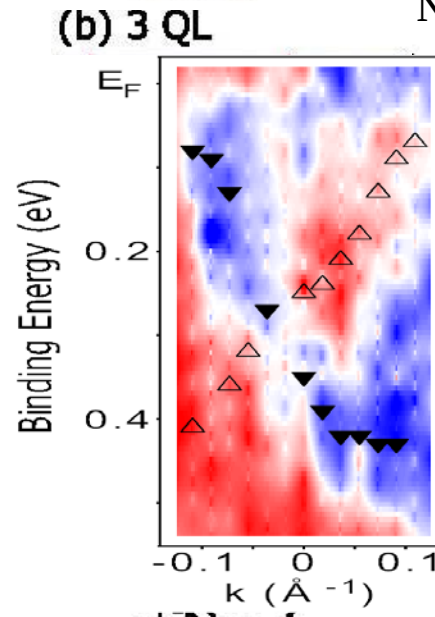
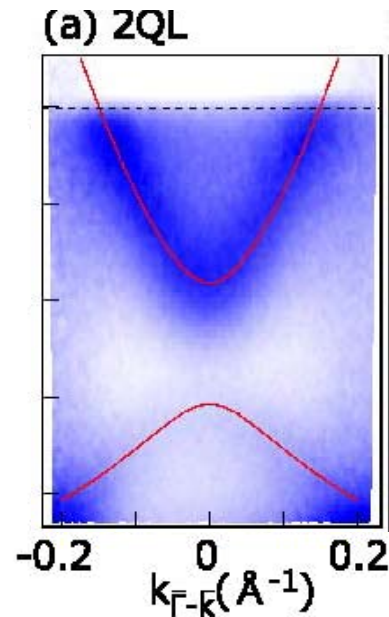
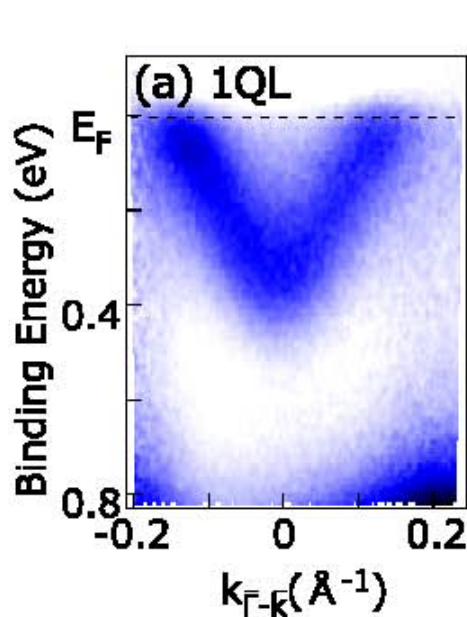


Growth and Band Structure of Bi_2Se_3

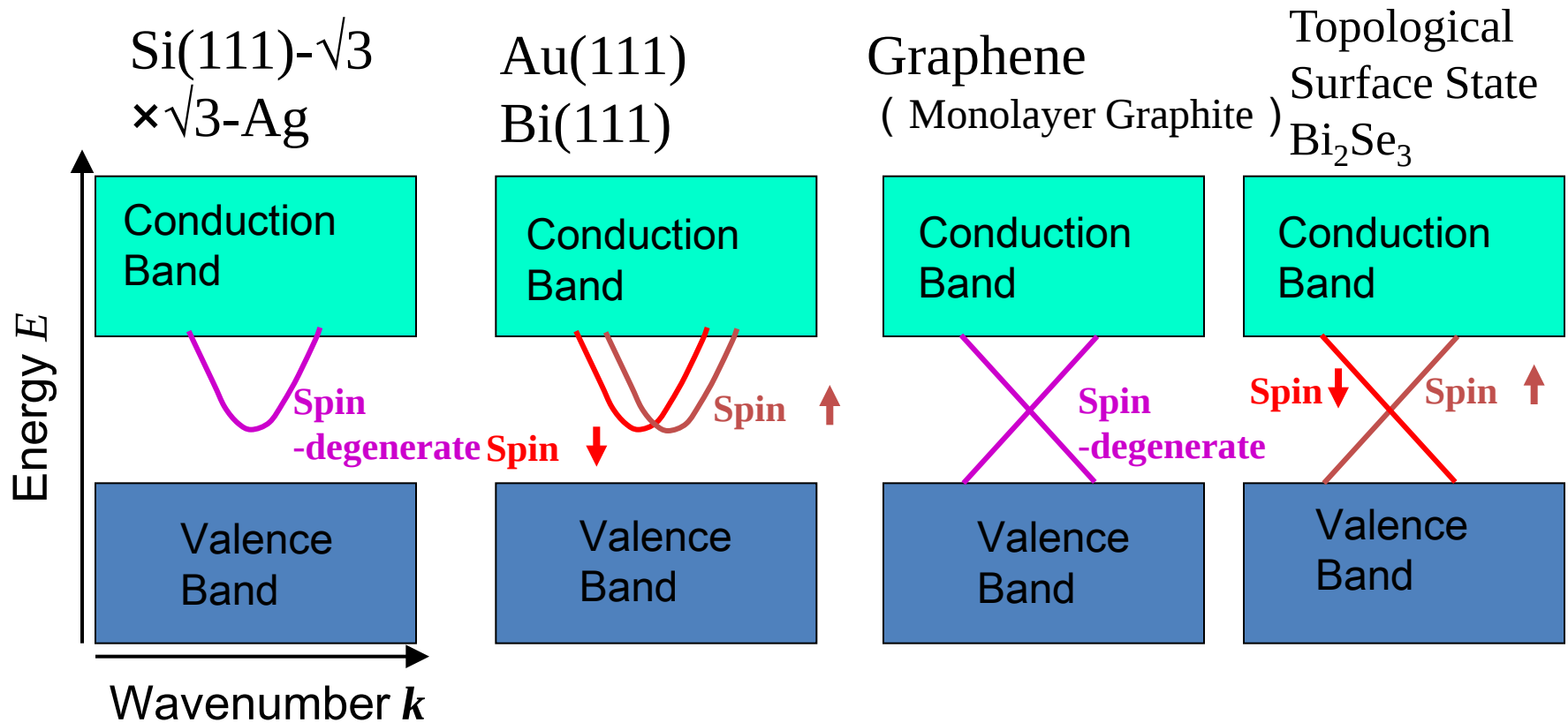
Y. Sakamoto, et al., Phys. Rev. B **81**,165432 (2010)



Bulk Crystal Y. Xia, et al.,
Nature Physics 2009 (May)



Various Surface States



$$E = \frac{p^2}{2m^*} = \frac{\hbar^2 k^2}{2m^*}$$

Free-Electron-like

$$E = \sqrt{(mc^2)^2 + (pc)^2}$$



$$m = 0$$

$$E = \pm pc = \pm c\hbar k$$

Massless Dirac Fermion

Summary: Compare $\text{Bi}_{1-x}\text{Sb}_x$, Bi_2Se_3 with Bi

Both of $\text{Bi}_{1-x}\text{Sb}_x$ and Bi show

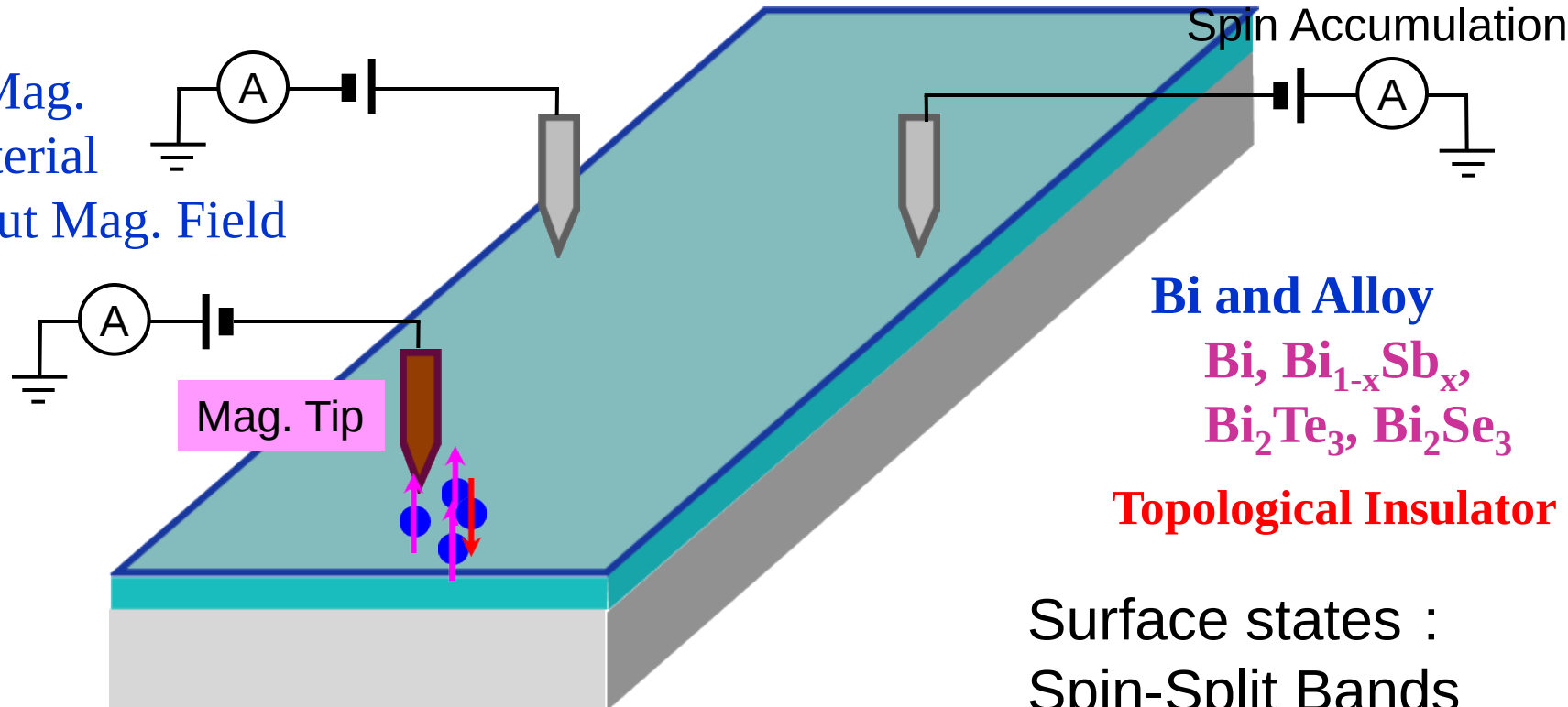
1. metallic spin-split surface state
2. chiral spin texture in Fermi surface
3. absence of back scattering in surface state
⇒ These are not unique properties of topological insulators.
Surface Rashba effect bring about them.
4. Chiral Dirac cone in surface state: Bi_2Se_3

The unique properties of topological insulators may be detected in **Spin flow**.

Spin Transport Measurements

3-tip STM

Non-Mag.
Material
Without Mag. Field



Strong Spin-Orbit Interaction

⇒ Electric field is seen to be
effect magnetic field for
flowing electrons

⇒ Spin flow perpendicular to
Current and spin :

Bi and Alloy

Bi, Bi_{1-x}Sb_x,

Bi₂Te₃, Bi₂Se₃

Topological Insulator

Surface states :
Spin-Split Bands
Due to Rashba Eff.

Tip Separation < Spin Relaxation Length

$$H = \frac{1}{2m} p^2 + V(x) + \frac{1}{4mc^2} \sigma \cdot (\text{grad} V(x) \times p)$$

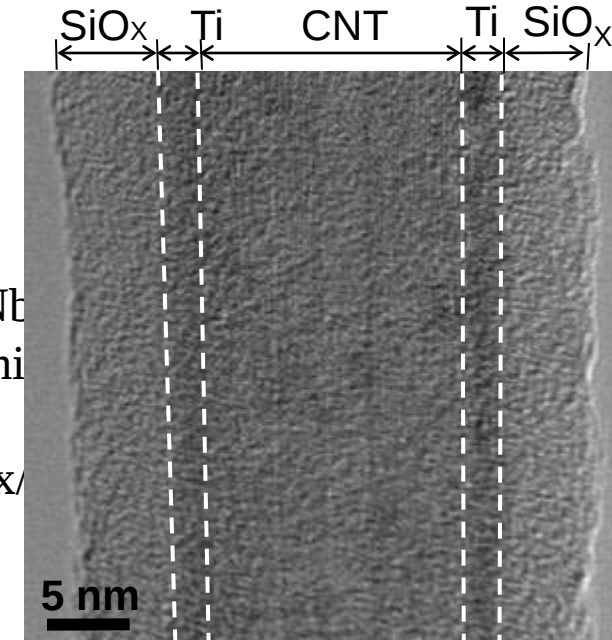
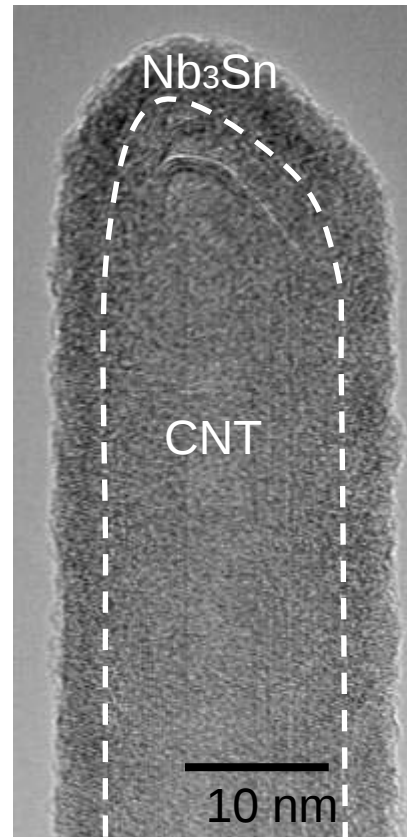
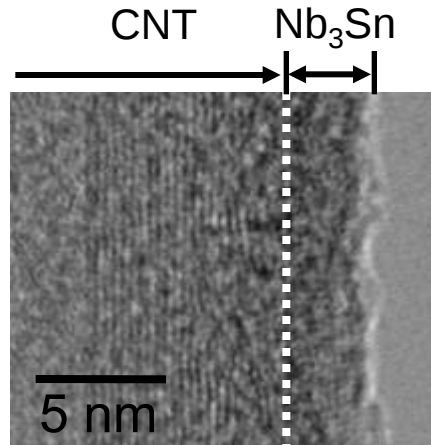
Functionalized CNT Tips with Coating

Coating CNT Tips with Compounds and Multi-Layers

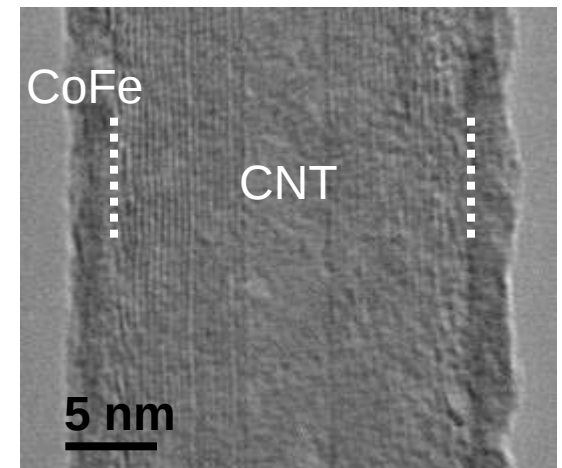
→ Various Measurements

- Metal → Ohmic or Schottky Contacts W, **PtIr**
- Dielectric (Insulator) → Nano-FET effect **SiO₂**
- Magnetic → Spintronics, MFM **CoFe**
- Superconducting → Andreev Ref., SC devices Nb₃Sn, Nb
- Insulator/Metal Multi-Layers → STM in liquid, Biochemi

Probes



CoFe



CNT Coating by Pulsed Laser Deposition (PLD)

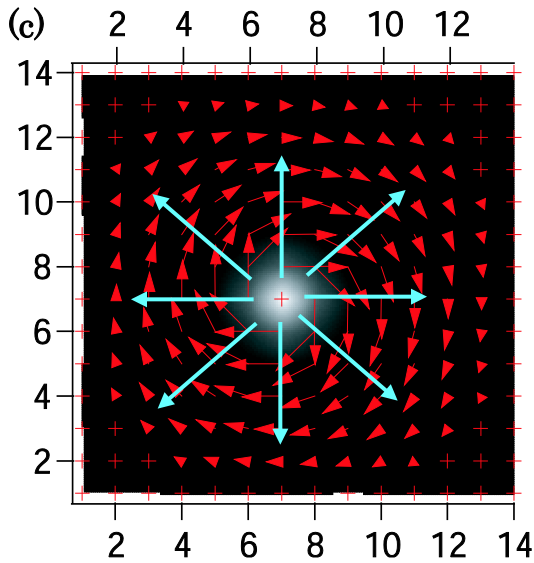
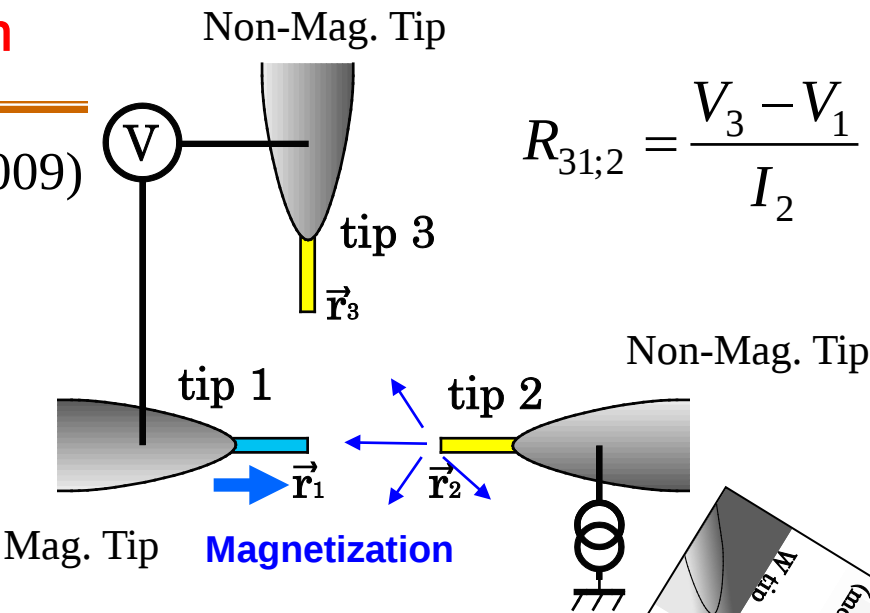
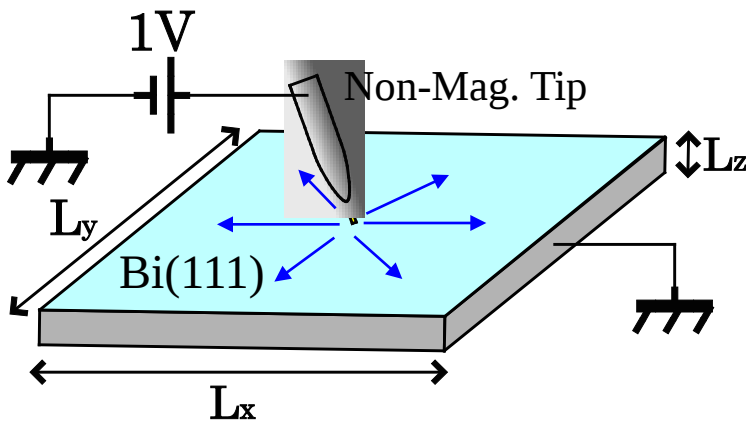
H. Konishi, et al., JJAP 45, 3690 ('06)

H. Konishi, et al., RSI 78, 013703('07)

Inverse Spin Hall Effect+Mag. Tip

⇒ Broken of Green's Reciprocal Theorem

T. Tono Master Thesis (2009)



Spin Distribution by Spin Hall Effect

